

Analytical Chemistry

References :

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Chapter one

Introduction to Analytical Chemistry :

Everything is made of chemicals. Analytical chemistry determine what and how much. In other words analytical chemistry is concerned with the separation, identification, and determination of the relative amounts of the components making up a sample.

Analytical chemistry is concerned with the chemical characterization of matter and the answer to two important questions what is it (qualitative) and how much is it (quantitative).

Analytical chemistry answering for basic questions about a material sample:

- What?
- Where?
- How much?
- What arrangement, structure or form?

Qualitative analysis: An analysis in which we determine the identity of the constituent species (the elements and compounds) in a sample.

Quantitative analysis: An analysis in which we determine how much of a constituent species is present in a sample.

Analytes: Are the components of a sample that are to be determined.

1.1 Classifying Analytical Techniques

A- Classical techniques

Mass, volume, and charge are the most common signals for classical techniques, and the corresponding techniques are:

- 1- Gravimetric techniques.

2- Volumetric techniques.

3- Coulometric techniques.

B- Instrumental techniques

1- Spectroscopic methods - measuring the interaction between the analyte and electromagnetic radiation (or the production of radiation by an analyte).

2- Electroanalytic methods - measure an electrical property (i.e., potential, current, resistance, amperes, etc.) chemically related to the amount of analyte.

1.2 Quantitative Analytical Methods

We compute the results of a typical quantitative analysis from two measurements. One is the mass or the volume of sample being analyzed. The second is the measurement of some quantity that is proportional to the amount of analyte in the sample such as mass, volume, intensity of light, or electrical charge. This second measurement usually completes the analysis, and we classify analytical methods according to the nature of this final measurement. Gravimetric methods determine the mass of analyte or some compound chemically related to it. In a volumetric method, the volume of a solution containing sufficient reagent to react completely with the analyte is measured.

1.3 Applications of Analytical Chemistry

Analytical chemistry used in many fields:

1, In **medicine**, analytical chemistry is the basis for clinical laboratory tests which help physicians diagnosis disease and chart progress in recovery.

2. In **industry**, analytical chemistry provides the means of testing raw materials and for assuring the quality of finished products whose chemical composition is critical. Many household products, fuels, paints, Pharmaceutical, etc. are analysed

by the procedures developed by analytical chemists before being sold to the consumer.

3. **Environmental quality** is often evaluated by testing for suspected contaminants using the techniques of analytical chemistry.

4. **The nutritional value of food** is determined by chemical analysis for major components such as protein and carbohydrates and trace components such as vitamins and minerals. Indeed, even the calories in a food are often calculated from the chemical analysis.

5. **Forensic analysis** - analysis related to criminology; DNA finger printing, finger print detection; blood analysis.

6. **Bioanalytical chemistry and analysis** - detection and/or analysis of biological components (i.e., proteins, DNA, RNA, carbohydrates, metabolites, etc.).

Atomic weight : It is the mass of an atom of that element based on a mass of exactly 12 to the carbon isotope C^{12} .

Molecular or Formula weight(M.wt): It is the sum of the atomic weights of the elements that constitute a molecule of the substance.

Examples :

M.wt of water (H_2O) = $2 \times (1.008) + 1 \times 16 = 18.02$ g/gmole

Note: it is possible to express the molecular weights in any unit of mass for example M.wt of $H_2 = 2.016$ g/gmole ,lb/lb mole , ton /ton mole.

the mole unit (n) : the mole (or g.mole) can be defined as the amount of the substance that contains number of molecules equal to that in exactly 12 gram of C^{12} .Hence number of moles is computed as

$$\text{No. of moles} = \frac{\text{Mass in g}}{\text{M.wt g/gmole}}$$

the term of g.atom can be defined as the amount of an element that contain the same number of atoms equal to that of carbon atoms in exactly 12 gm of C¹²

.Hence number of g.atoms is computed as

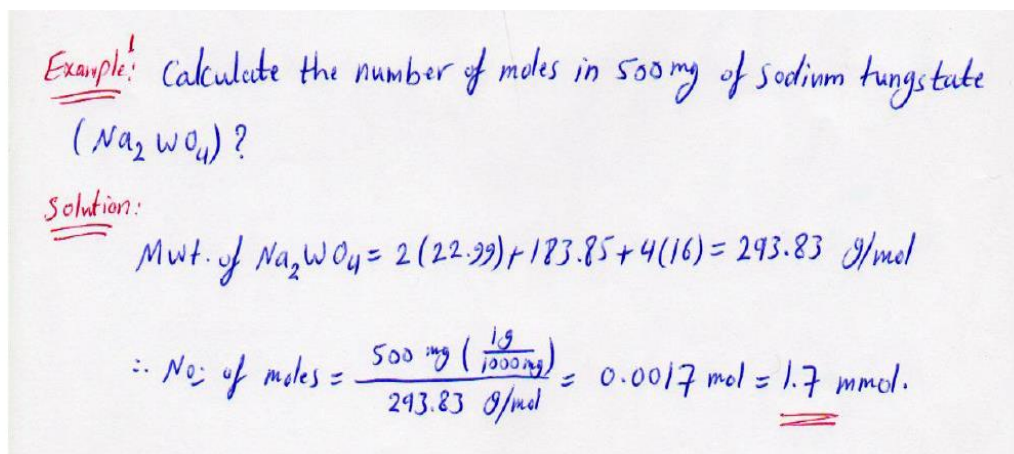
$$\text{No. of g.atoms} = \frac{\text{Mass of the element in g}}{\text{atomic weight}}$$

Note .Since we usually work in millimole,hence

$$\text{No. of mmol} = \frac{\text{Mass in mg}}{\text{M.wt}}$$

Calculating the Amount of a Substance in Moles or Millimoles

The two examples that follow illustrate how the number of moles or millimoles of a species can be determined from its mass in grams or from the mass of a chemically related species



Example 2: Calculate the mass in mg of 0.25mmol of ferric oxide (Fe_2O_3)?

Solution:

$$\text{Mwt of } \text{Fe}_2\text{O}_3 = 159.69 \text{ mg/mmol}$$

$$\therefore \text{mass} = 0.25 \text{ mmole} * 159.69 \frac{\text{mg}}{\text{mmol}} = \underline{\underline{39.9 \text{ mg}}}$$

Example 3:

- (a) Calculate the number of moles of K_2CO_3 that contains 117.3g of potassium.
- (b) Calculate the mass in grams of other elements in such compound.
Given that: atomic weight of K=39.1

Solution:

$$\text{(a) } g.\text{atoms of K} = \frac{117.3}{39.1} = 3 \text{ g.atoms}$$

Each mole of K_2CO_3 contains 2g.atoms of K

$$\therefore \text{No. of moles of } \text{K}_2\text{CO}_3 = \frac{3}{2} = \underline{\underline{1.5 \text{ mol}}}$$

$$\begin{aligned} \text{(b) Mass of oxygen} &= g.\text{atoms of oxygen} * \text{atomic wt.} \\ &= 1.5 * 3 * 16 = \underline{\underline{72 \text{ g}}} \end{aligned}$$

$$\begin{aligned} \text{Mass of Carbon} &= g.\text{atoms of Carbon} * \text{atomic wt.} \\ &= 1.5 * 1 * 12 = \underline{\underline{18 \text{ g}}} \end{aligned}$$

Example 5

Find the number of moles and millimoles of benzoic acid ($M = 122.1 \text{ g/mol}$) that are contained in 2.00 g of the pure acid.

Solution

If we use HBz to represent benzoic acid, we can write that 1 mole of HBz has a mass of 122.1 g. Therefore,

$$\begin{aligned} \text{Amount HBz} = n_{\text{HBz}} &= 2 \text{g HBz} \times \frac{1 \text{ mol HBz}}{122.1 \text{g HBz}} \\ &= 0.0164 \text{ mol HBz} \end{aligned}$$

To obtain the number of millimoles, we divide by the millimolar mass (0.1221 g/mmol), that is,

$$\begin{aligned} \text{Amount HBz} = n_{\text{HBz}} &= 2 \text{g HBz} \times \frac{1 \text{ mol HBz}}{0.1221 \text{g HBz}} \\ &= 16.4 \text{ mmol HBz} \end{aligned}$$

Example 6

What is the mass in grams of Na^+ (22.99 g/mol) in 25.0 g of Na_2SO_4 (142.0 g/mol)?

Solution

The chemical formula tells us that 1 mole of Na_2SO_4 contains 2 moles of Na^+ , that is,

$$\text{Amount Na}^+ = n_{\text{Na}^+} = \text{mol Na}_2\text{SO}_4 \times \frac{2 \text{ mol Na}^+}{\text{mol Na}_2\text{SO}_4}$$

To find the number of moles of Na_2SO_4 , we proceed as in Example 1-1:

$$\begin{aligned} \text{Amount Na}_2\text{SO}_4 = n_{\text{Na}_2\text{SO}_4} &= 25 \text{ g Na}_2\text{SO}_4 \times \frac{1 \text{ mol Na}_2\text{SO}_4}{142 \text{ g}} \\ &= 0.176 \text{ mol} \end{aligned}$$

$$\text{Amount Na}^+ = 2 * 0.176 = 0.352 \text{ mol}$$

$$\text{Mass Na}^+ = m_{\text{Na}^+} = \text{mol Na}^+ \times \frac{22.99 \text{ g}}{\text{mol Na}^+}$$

$$= 8.1 \text{ g}$$

Molar Methods : A solution containing 1 mole of solute per liter of solution is defined as a (Molar solution).

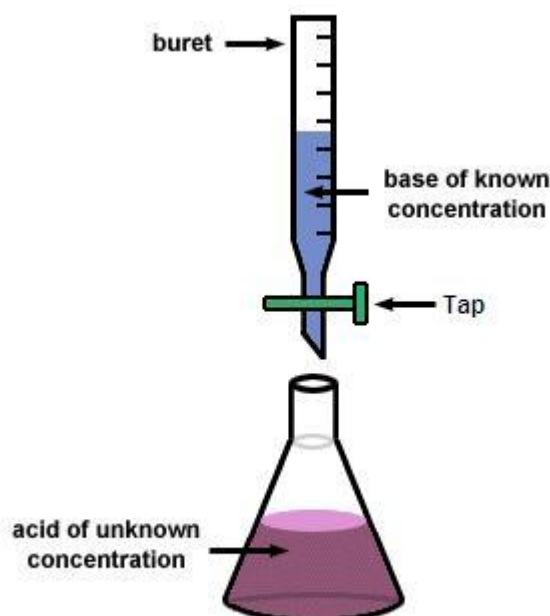
Molarity of solution : The number of moles of solute per liter of solution.

$$\text{Molarity}[M] = \frac{\text{number of moles solute}}{\text{liters of solution}}$$

$$\text{Molarity}[M] = \frac{\text{grams of solute}}{\text{molecular weight}} \times \frac{1}{\text{liters of solution}}$$

Moles of solute = molarity x liters of solution

Grams of solute = molarity x literes of solution x molecular weight.



Ex / Calculate the molar concentration of ethanol in an aqueous solution that contains 2.30 gm of C_2H_5OH (46.07 gm /mole) in 3.50 L of solution.

Solution /

$$[C_2H_5OH] = \frac{\text{number of moles}}{\text{liter of solution}}$$

$$\begin{aligned} \text{No. mol } C_2H_5OH &= 2.30 \text{ gm } C_2H_5OH \times \frac{1 \text{ mol } C_2H_5OH}{46.07 \text{ gm } C_2H_5OH} \\ &= 0.0499 \text{ mol } C_2H_5OH \end{aligned}$$

$$[C_2H_5OH] = \frac{0.0499 \text{ mol}}{3.5L} = 0.0143 \text{ mol / L} = 0.0143 \text{ M}$$

EX/Calculate the analytical and equilibrium molar concentration of the solute species in an aqueous solution that contains 285.0 mg of trichloroacetic acid , Cl_3CCOOH (163.4gm / mol) , in 10.0ml.

Solution/



$$\begin{aligned}\text{No. mol HA} &= 285.0 \text{ mg HA} \times \frac{1 \text{ gm HA}}{1000 \text{ mg HA}} \times \frac{1 \text{ mol HA}}{163.4 \text{ gm HA}} \\ &= 1.744 \times 10^{-3} \text{ mol HA} \\ [\text{HA}] &= \frac{1.744 \times 10^{-3} \text{ mol HA}}{10.0 \text{ ml}} \times \frac{1000 \text{ ml}}{1 \text{ L}} \\ &= 0.174 \text{ mol HA / L} = 0.174 \text{ M}\end{aligned}$$

EX/ How many grams of AgNO_3 (169.9 gm/mol) must be used to prepared 500.0 ml of 0.125 M?

Solution/

$$\begin{aligned}M &= \frac{\text{wt}}{M.\text{wt}} \times \frac{1000}{V\text{ml}} \\ \text{Wt} &= \frac{M \times M.\text{wt} \times V\text{ml}}{1000} \\ &= \frac{0.125 \text{ mmol/ml} \times 169.9 \text{ mg/mmol} \times 500 \text{ ml}}{1000} = \\ &10.62 \text{ mg}\end{aligned}$$

Equivalent Methods:

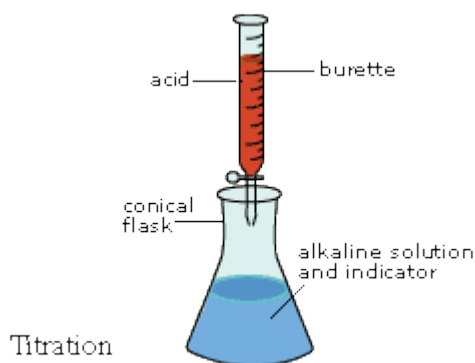
The equivalent weight (eq) is defined, for neutralization reactions, as the weight in grams that will furnish or react with one gram-atomic weight of hydrogen ion.

$$\text{Equivalent weight} = \frac{\text{molecular weight}}{n} = \frac{M.Wt}{n}$$

$n = \text{no. H}^+$ for acid

= no. OH^- for base

= no. electrons in the reaction.



A) Equivalent weight of atoms of element :

$$\text{Eq. wt} = \frac{\text{atomic weight}}{\text{valency}}$$

A) Equivalent weight of compounds:

1. Equivalent weight of Acids;

Equivalent weight of acid which contains one replaceable hydrogen

$$\text{Eq .wt of acid} = \frac{\text{molecular weight}}{\text{no.of hydrogen atom}}$$

2 Equivalent weight of a base;

Equivalent weight of base which contains one replaceable hydroxyl group

$$\text{Eq .wt of a base} = \frac{\text{molecular weight}}{\text{no.of hydroxyl groups}}$$

3 Equivalent weight of a salt;

Equivalent weight of a salt in grams which contains one weight of cat ion can react or replaced by one gram of hydrogen

4 Equivalent weight of Reducing and Oxidizing agent

$$\text{Eq .wt. of reducing agent} = \frac{\text{molecular weight}}{\text{no.of electrons losses in the reaction}}$$

$$\text{Eq .wt of oxidizing agent} = \frac{\text{molecular weight}}{\text{no.of electrons gains in the reaction}}$$

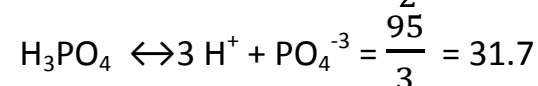
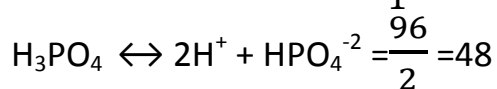
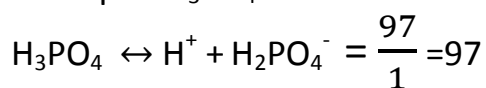
Example /

$$\text{Equivalent weight of HCl} = \frac{MHCl}{n} = \frac{36.5}{1} = 36.5$$

$$\text{For eq.wt NaOH} = \frac{MNaOH}{n} = \frac{40}{1} = 40$$

$$\text{For eq.wt Ba (OH)}_2 = \frac{MBa(OH)_2}{n} = \frac{171}{2} = 85.5$$

For eq.wt H₃PO₄



$$\text{Equivalent weight} = \frac{\text{molecular weight}}{\text{no. of valency}} = \frac{M.wt}{n}$$

$$\text{Normality(N)} = \frac{\text{Equivalent Solute}}{\text{liters of solution}}$$

$$\text{Normality(N)} = \frac{\frac{\text{grams solute}}{\text{molecular weight}}}{\text{hydrogen equivalents per mole}} \times \frac{1}{\text{liters of solution}}$$

liters of solution x normality = Equivalents of solute

liters of solution x normality x equivalent weight = grams solute

Preparation of solution

Most solution are prepared by dissolving a weighed amount of solid and adding sufficient water to make the desired volume.



Calculation of the Normality and Molarity of standard solution

Ex/How many grams of pure sodium hydroxide (M.wt 40.0g/mol) are needed for preparation of 500.0 ml 0.100N solution?



$$N = \frac{\text{Equivalents of solute}}{\text{liters of solution}}$$

Equivalents of solute = normality x volume in liters
 = 0.100 eq / liter x 0.500 liter
 = 0.0500 eq

Equivalents of solute = $\frac{\text{weight in grams}}{\frac{\text{molecular weight}}{\text{no. of valency}}}$

$$0.0500 \text{ eq} = \frac{Wt}{\frac{40.0 \text{ g/mol}}{1 \text{ eq/mol}}}$$

Wt = 2.00 gm

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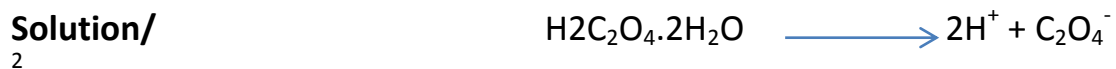
$$N = \frac{Wt}{\text{eq.wt}} \times \frac{1000}{Vml}$$

$$0.100 \text{ eq/L} = \frac{wt}{\frac{M.wt}{n}} \times \frac{1000}{500 \text{ ml}}$$

$$0.100 \text{ eq/L} = \frac{wt}{\frac{40.0 \text{ gm/mol}}{1 \text{ eq/mol}}} \times \frac{1000 \text{ ml/L}}{500 \text{ ml}}$$

Wt = 2.00 gm

Ex/ What is the normality of a solution prepared by dissolving 25.20 gm oxalic acid ($\text{H}_2\text{C}_2\text{O}_4 \cdot 2\text{H}_2\text{O}$) (126.1 gm/mol) in sufficient water to give 1.200 liters of solution? What is the molarity of this solution?



$$N = \frac{\text{Equivalents of solute}}{\text{liters of solution}}$$

Number of equivalents = $\frac{\text{weight of solute}}{\frac{\text{molecular weight}}{\text{no. of valency}}}$
 = $\frac{25.20 \text{ gm}}{\frac{126.1 \text{ gm/mol}}{2 \text{ eq/mol}}} = 0.3996 \text{ eq}$

The Normality is :

$$N = \frac{0.3996 \text{ eq}}{1.200 \text{ L}} = 0.3330 \text{ eq/liter}$$

The Molarity is:

$$M = \frac{N}{n} = \frac{0.3330 \text{ eq/liter}}{2 \text{ eq/mol}} = 0.1665 \text{ mol/liter}$$

Relation between Molarity and Normality:

$$M = \frac{wt_1}{Mwt} * \frac{1}{L} \Rightarrow wt_1 = M * Mwt * L$$

$$N = \frac{wt_2}{eq. wt} * \frac{1}{L} \Rightarrow wt_2 = N * eq. wt * L$$

$$wt_1 = wt_2$$

$$M * Mwt * \cancel{L} = N * eq. wt * \cancel{L}$$

$$M * Mwt = N * \frac{Mwt}{n}$$

$$\therefore \boxed{N = nM}$$

Where:

n : no. of H^+ , OH^- & cation valency.

Ex/How many grams of pure sodium sulfate Na_2SO_4 (M.wt 142.0g/mol) are needed for preparation of 200.0 ml 0.500N solution?

Solution/ $\text{Na}_2\text{SO}_4 \longrightarrow 2\text{Na}^+ + \text{SO}_4^{-2}$

$$N = \frac{wt}{eq.wt} \times \frac{1000}{Vml}$$

$$0.500\text{eq/L} = \frac{wt}{\frac{142\text{gm/mol}}{2\text{eq/mol}}} \times \frac{1000\text{ml/L}}{200\text{ml}}$$

$$Wt = 7.1 \text{ gm}$$

Ex/Describe the preparation of 5.000 L of 0.1000M Na_2CO_3 (105.99g/mol) from the primary standard solid?

Solution/

$$\text{Molarity} = \frac{\text{number of moles solute}}{\text{liters of solution}}$$

$$\text{Moles of solute} = M \times V$$

$$= 0.1000\text{mol/L} \times 5.000\text{L} = 0.5000\text{mol}$$

$$\begin{aligned} \text{Grams of solute} &= 0.500\text{mol} \times \frac{105.999\text{gm}}{\text{mol}} \\ &= 53.00 \text{ gm Na}_2\text{CO}_3 \end{aligned}$$

Therefore the solution is prepared by dissolving 53.00 gm of Na_2CO_3 in water and diluting to exactly 5.00 L.

Ex/

A standard 0.0100 M solution of Na^+ is required for calibrating a flame photometric method for determining the element. Describe how 500.0 ml of this solution can be prepared from primary standard Na_2CO_3 ?

Solution/ $\text{Na}_2\text{CO}_3 \longrightarrow 2\text{Na}^+ + \text{CO}_3^{-2}$

$$\text{No. mol Na}^+ = 500.0\text{ml} \times \frac{0.01\text{mmol}}{\text{ml}} = 5\text{mmol}$$

$$\text{Moles of Na}_2\text{CO}_3 = 5 \text{ mmol Na}^+ \times \frac{1 \text{ mmol Na}_2\text{CO}_3}{2 \text{ mmol Na}^+} = 2.5 \text{ mmol}$$

$$\text{Grams of Na}_2\text{CO}_3 = 2.5 \text{ mmol} \times 0.10599 \text{ gm/mmol} = 0.265 \text{ gm}$$

The solution is therefore prepared by dissolving 0.265 gm of Na_2CO_3 in water and diluting to 500.0ml.

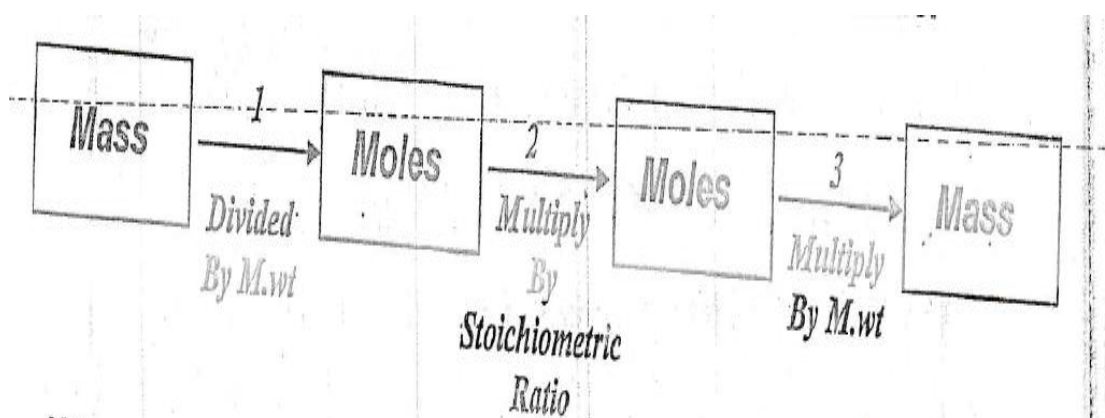
Density and specific gravity of solution

Density and specific gravity are terms of encountered in the analytical literature . The density of a substance is its mass per unit volume , where as its specific gravity is the ratio of its mass to the mass of an equal volume of water. Density has units of kilograms per liter or grams per milliliter in the metric system.

Chemical Stoichiometry :

The Stoichiometry of reaction is the quantitative relationship among the number of moles of reactants and products as shown by a balanced equation .

Flow diagram for making Stoichiometric Calculations



When the mass of reactant or product is given , the mass is first converted to the number of moles using molecular weight .

The stoichiometry ratio given by chemical equation for the reaction is then used to find the number of mole of another reactant. Finally ,the mass of the other reactant or the product is computed by multiply by molecular weight .

Example 8 : what mass of AgNO_3 is needed to convert 2.33 gm of Na_2CO_3 to Ag_2CO_3 ? What mass of Ag_2CO_3 will be formed ?

Solution: The chemical reaction eq. is:



$$\text{Mwt.}(\text{Na}_2\text{CO}_3) = 106 \frac{\text{g}}{\text{mol}}, \text{Mwt.}(\text{AgNO}_3) = 169.9 \frac{\text{g}}{\text{mol}}, \text{Mwt.}(\text{Ag}_2\text{CO}_3) = 275.7 \frac{\text{g}}{\text{mol}}$$

$$\text{no. moles of } \text{Na}_2\text{CO}_3 = \frac{\text{wt.}}{\text{Mwt.}} = \frac{2.33 \text{ gm}}{106 \frac{\text{g}}{\text{mol}}} = 0.02198 \text{ mol}$$

$$\therefore \text{no. mol } \text{AgNO}_3 = 0.02198 * \frac{2 \text{ mol } \text{AgNO}_3}{1 \text{ mol } \text{Na}_2\text{CO}_3} = 0.04396 \text{ mol}$$

$$\text{mass of } \text{AgNO}_3 = \text{mole} * \text{Mwt.} = 0.04396 * 169.9 = \underline{\underline{7.47 \text{ g } \text{AgNO}_3}}$$

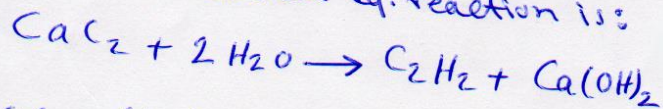
$$\text{no. moles of } \text{Ag}_2\text{CO}_3 = \text{no. moles of } \text{Na}_2\text{CO}_3 = 0.02198 \text{ mol}$$

$$\therefore \text{mass of } \text{Ag}_2\text{CO}_3 = 0.02198 * 275.7 = \underline{\underline{6.06 \text{ gm } \text{Ag}_2\text{CO}_3}}$$

Example 2: Calcium carbide, CaC_2 reacts with water to form acetylene.

- (a) How many grams of CaC_2 required to produce 23.6 gm acetylene.
(b) If 55.3 grams of $\text{Ca}(\text{OH})_2$ are formed, how many grams of water reacted.

Solution: The chemical eq. reaction is:



$$\text{Mwt. } \text{CaC}_2 = 64 \text{ g/mol}, \text{Mwt. } \text{C}_2\text{H}_2 = 26 \text{ g/mol}, \text{Mwt. } \text{Ca}(\text{OH})_2 = 74$$

$$n \text{ C}_2\text{H}_2 \text{ formed} = \frac{23.6 \text{ g}}{26 \frac{\text{g}}{\text{mol}}} = 0.908 \text{ mol}$$

$$n \text{ CaC}_2 \text{ reacted} = n \text{ C}_2\text{H}_2 \text{ produced} = 0.908 \text{ mol}$$

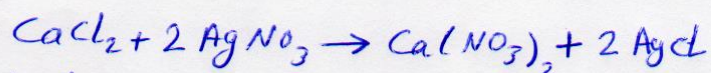
$$\therefore \text{mass of CaCl}_2 = n \times \text{Mwt} = 0.908 \times 64 = \underline{\underline{58.1 \text{ gm}}}$$

$$n_{\text{Ca(OH)}_2 \text{ formed}} = \frac{55.30}{74.09 \text{ mol}} = 0.747 \text{ mol}$$

$$\therefore n_{\text{H}_2\text{O reacted}} = 2 \times n_{\text{Ca(OH)}_2} = 2 \times 0.747 = 1.494 \text{ mol}$$

$$\therefore \text{mass of H}_2\text{O req.} = n \times \text{Mwt} = 1.494 \times 18 = \underline{\underline{26.89 \text{ gm}}}$$

Example 3: An impure sample of CaCl_2 is dissolved and titrated with a solution of AgNO_3 . The reaction is:



It is found that 46.35 ml, 0.1034 M AgNO_3 titrates a 0.2843 gm sample of CaCl_2 . Compute the percentage of CaCl_2 in the sample?

Solution:

$$\text{mmoles of AgNO}_3 = 46.35 \text{ ml} \times 0.1034 \frac{\text{mmol}}{\text{ml}} = 4.793 \text{ mmol}$$

The equation shows that 2 moles AgNO_3 reacts with 1 mole CaCl_2

$$\therefore \text{mmoles CaCl}_2 = 4.793 \times \frac{1 \text{ mole CaCl}_2}{2 \text{ mole AgNO}_3} = 2.397 \text{ mmol}$$

$$\text{wt. CaCl}_2 = 2.397 \times 111 = 266.1 \text{ mg}$$

$$\% \text{ CaCl}_2 = \frac{266.1 \text{ mg}}{284.3 \text{ mg}} \times 100 = 93.6 \%$$

Calculation based on Molarity:



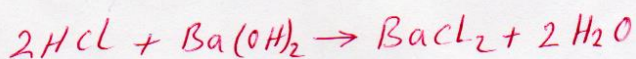
Where: $R = \frac{b}{a}$

$$\text{mmole of } A = M_A * V_A$$

$$\text{mmole of } B = \text{mmole of } A * R \Rightarrow \text{mmole of } B = M_A * V_A * R \quad [*Mwt_B]$$

$$\therefore \text{Wt of } B \text{ in mg} = \text{mmole of } A * R * Mwt_B$$

Example: Exactly 50 ml of HCl required 29.71 ml of 0.01963 M of $Ba(OH)_2$ to reach end point as following eq.:



What is the molarity of HCl?

Solution:

$$\text{mmole of } Ba(OH)_2 = 0.01963 * 29.71 = 0.5832 \text{ mmole.}$$

$$\text{mmole of HCl} = 2 * \text{mmole of } Ba(OH)_2 = 2 * 0.5832 = 1.1664 \text{ mmole.}$$

$$\therefore M_{HCl} = \frac{1.1664}{50} = \underline{\underline{0.0233}} \text{ mmole/ml.}$$

calculation based on Normality:

The basis of all computations dealing with normalities of solutions is the simple relation that the number of equivalents of one reactant is equal to the number for the other reactant.

If A reacts with B

$$\text{eq. A} = \text{eq. B}$$

$$\text{meq. A} = \text{meq. B}$$

$$N = \frac{\text{wt.}}{\text{eq. wt.}} * \frac{1}{L} \Rightarrow \frac{\text{wt.}}{\text{eq.}} = N * L$$

$$\therefore \boxed{\frac{\text{mg}}{\text{meq.}} = N * V}$$

Example: 25 ml of HCl sol. is required to react with 0.1854 gm of pure Na_2CO_3 . what is the normality of acid? if 32.16 ml of acid reacts with 29.65 ml of NaOH. What is the normality of NaOH sol.?

Solution:

$$\text{meq. HCl} = \text{meq. Na}_2\text{CO}_3$$

$$N_{\text{acid}} * 25 \text{ ml} = \frac{0.1854 \text{ gm} * \frac{1000 \text{ mg}}{1 \text{ gm}}}{\frac{106}{2} \text{ mg/meq.}} \Rightarrow N_{\text{acid}} = \underline{\underline{0.1394}} \text{ meq./ml}$$

$$N_{\text{acid}} * V_{\text{acid}} = N_{\text{base (NaOH)}} * V_{\text{base (NaOH)}}$$

$$0.1394 * 32.16 = N_{\text{NaOH}} * 29.65 \Rightarrow N_{\text{NaOH}} = \underline{\underline{0.1515}} \text{ meq./ml.}$$

Density and specific gravity of solution

Density and specific gravity are terms of encountered in the analytical literature . The density of a substance is its mass per unit volume it is expressed as (g/mL) or (gm/cm³) , where as its specific gravity (Spg)is the ratio of its mass to the mass of an equal volume of water. Density has units of kilograms per liter or grams per milliliter in the metric system.

$$\text{Density} = \frac{\text{mass in}}{\text{volume}}$$

$$\text{Specific gravity} = \frac{\text{density of substance}}{\text{density of water}}$$

Dilution of solution: A solution of known normality is frequently prepared from a more concentrated one of known strength by quantitative dilution.

$$(\text{Normality} * \text{volume}) \text{ conc} = (\text{Normality} * \text{volume}) \text{ dilute}$$

$$(N \times V) \text{ conc} = (N \times V) \text{ dil}$$

Or for concentration

$$(\text{Molarity} * \text{volume}) \text{ conc} = (\text{Molarlity} * \text{volume}) \text{ dilute}$$

$$(C \times V) \text{ conc} = (C \times V) \text{ dil}$$

Percentage methods:

$$\text{a - Weight percent (\%wt)} = \frac{\text{weight of solute}}{\text{weight of solution}} \times 100$$

$$\text{b - volume percent (\%vol) \%} = \frac{\text{volume of solute}}{\text{volume of solution}} \times 100$$

c – Weight/volume percent

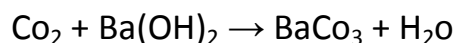
$$\text{(\%wt/vol)} = \frac{\text{weight of solute}}{\text{volume of solution}} \times 100$$

d- Part per million (ppm):

$$\text{ppm} = \frac{\text{weight of solute in (gm)}}{\text{volume of solution in (L)}} \times 10^6$$

Ex/A 0.2011gm sample of an organic compound was burned in a stream of oxygen, and CO₂ produced in a solution of barium hydroxide.

Calculate the percentage of carbon in the sample if 0.500gm BaCO₃ was formed.



Solution/

$$1 \text{ mol BaCO}_3 \equiv 197.0\text{gm}$$

$$\text{No. mol BaCO}_3 = 0.500 \text{ gm BaCO}_3 \times \frac{1 \text{ mol BaCO}_3}{197 \text{ gm BaCO}_3} = 2.538 \times 10^{-3}$$

mol BaCO₃

$$1 \text{ mol BaCO}_3 \equiv 1 \text{ mol CO}_2 = 2.538 \times 10^{-3} \text{ mol}$$

$$1 \text{ mol CO}_2 \equiv 44.0\text{gm}$$

$$\text{Mass CO}_2 = 2.538 \times 10^{-3} \text{ mol CO}_2 \times \frac{44.0 \text{ gm}}{1 \text{ mol CO}_2}$$

$$= 0.1116 \text{ gm CO}_2$$

$$\text{M CO}_2\% = \frac{m \text{ CO}_2}{m \text{ comp}} \times 100$$

$$\% = \frac{0.1116}{0.2011} \times 100 = 55.49 \%$$

Ex/A 0.3516 gm sample of a commercial phosphate detergent was ignited at a red heat to destroy the organic matter. The residue was then taken up in hot HCl, which converted the P to H₃PO₄. The phosphate was precipitated as MgNH₄PO₄·6H₂O by addition of Mg⁺² followed by aqueous NH₃. After being filtered and washed. The precipitate was converted to Mg₂P₂O₇ (222.57 gm mol) by ignition at 1000 C⁰. This residue weighed 0.2161 gm. Calculate the percent P (30.974 gm mol) in the sample.

Solution/

$$\text{No. mol MP} = 0.2161 \text{ gm MP} \times \frac{1 \text{ mol MP}}{222.57 \text{ gm MP}} = 9.71 \times 10^{-4} \text{ mol P}$$

1 mol MP \equiv 2 mol P

No. mol P = 30.774 gm

$$\text{Mass P} = 9.71 \times 10^{-4} \text{ mol} \times \frac{30.974 \text{ gm}}{\text{mol}} = 0.0301 \text{ gm P}$$

$$\text{Percent P\%} = \frac{0.0301}{0.174} \times 100 = 17.107 = 17.11\%$$

Ex/A 0.7151 gm sample of impure $\text{Al}_2(\text{CO}_3)_3$ decomposed with HCl. The liberated CO_2 was collected on calcium oxide and found to weight 0.0621 gm the percentage of (Al) in the sample ?

Solution/

1 mol $\text{CO}_2 \approx 44.0 \text{ gm}$

$$\text{No. mol } \text{CO}_2 = 0.0621 \text{ gm } \text{CO}_2 \times \frac{1 \text{ mol } \text{CO}_2}{44.0 \text{ gm } \text{CO}_2} = 1.411 \times 10^{-3} \text{ mol}$$

1 mol $\text{Al}_2(\text{CO}_3)_3 \equiv 3 \text{ mol}(\text{CO}_2)$

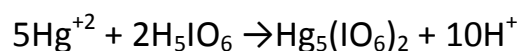
1 mol $\text{Al}_2(\text{CO}_3)_3 \equiv 2 \text{ mol}(\text{Al})$

$$\text{No. mol Al} = 1.411 \times 10^{-3} \text{ mol } \text{CO}_2 \times \frac{2 \text{ mol Al}}{3 \text{ mol } \text{CO}_2} = 0.941 \times 10^{-3} \text{ mol Al}$$

$$\text{Mass. Al} = 0.941 \times 10^{-3} \text{ mol} \times \frac{27 \text{ gm}}{1 \text{ mol}} = 0.0254 \text{ gm Al}$$

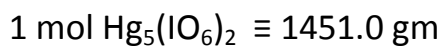
$$\% \text{ Al} = \frac{0.0254 \text{ gm}}{0.7151 \text{ gm}} \times 100 = 3.56 \%$$

Ex / the mercury in a 0.8142 gm sample was precipitated with an excess of paraper iodic acid H_2IO_6



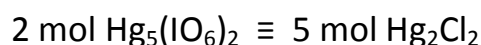
The precipitate was filtered free of precipitating agent, dried and weighed 0.4114 gm was recovered. Calculate the percentage of Hg_2Cl_2 in the sample.

Solution /



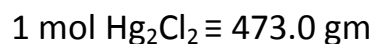
$$\text{No. mol Hg}_5(\text{IO}_6)_2 = 0.4114 \text{ gm Hg}_5(\text{IO}_6)_2 \times \frac{1 \text{ mol Hg}_5(\text{IO}_6)_2}{1451 \text{ gm Hg}_5(\text{IO}_6)_2}$$

$$= 2.84 \times 10^{-4} \text{ mol}$$



$$\text{No. mol Hg}_2\text{Cl}_2 = 2.84 \times 10^{-4} \text{ mol Hg}_5(\text{IO}_6)_2 \times \frac{5 \text{ mol Hg}_2\text{Cl}_2}{2 \text{ mol Hg}_5(\text{IO}_6)_2}$$

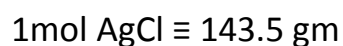
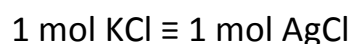
$$= 7.10 \times 10^{-4} \text{ mol}$$



$$\text{Mass of Hg}_2\text{Cl}_2 = 7.10 \times 10^{-4} \text{ mol} \times 473.0 \text{ gm / mol} = 0.3358 \text{ gm}$$

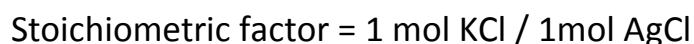
$$\% \text{ Hg}_2\text{Cl}_2 = \frac{0.3358 \text{ gm}}{0.8142 \text{ gm}} \times 100 = 41.24 \%$$

Ex / treatment of a 0.2500 gm sample of impure potassium chloride with an excess of AgNO_3 resulted in the formation of 0.2191 gm of AgCl . Calculate the percentage of KCl in the sample.



$$\text{No. mol AgCl} = 0.2191 \text{ gm AgCl} \times 1 \text{ mol AgCl} / 143.5 \text{ gm AgCl}$$

$$= 1.53 \times 10^{-3} \text{ mol AgCl}$$



$$\text{No. mol KCl} = 1.53 \times 10^{-3} \text{ mol AgCl} \times \frac{1 \text{ mol KCl}}{1 \text{ mol AgCl}} = 1.53 \times 10^{-3} \text{ mol KCl}$$

$$1 \text{ mol KCl} \equiv 74.5 \text{ gm KCl}$$

$$\text{Mass KCl} = 1.53 \times 10^{-3} \text{ mol KCl} \times 74.5 \text{ gm / mol KCl} = 0.114 \text{ gm KCl}$$

$$\% \text{ KCl} = 0.114 \text{ gm} / 0.2500 \text{ gm} \times 100 = 45.6 \%$$

Ex/ A sample of impure magnetite , Fe_3O_4 , weighing 1.542 gm is dissolved ; the iron is oxidized to Fe^+ and precipitated as $\text{Fe}(\text{OH})_3$. The precipitate is ignited to Fe_2O_3 , giving a weight of 1.485 gm . Calculate the percentage of Fe_3O_4 in the sample .

$$\text{No. mol Fe}_2\text{O}_3 = 1.485 \text{ gm Fe}_2\text{O}_3 \times \frac{\text{mol Fe}_2\text{O}_3}{159.7 \text{ gm Fe}_2\text{O}_3}$$

$$= 0.00930 \text{ mol Fe}_2\text{O}_3$$

This is equivalent to 2 / 3 as many moles of Fe_3O_4 , since 2 moles Fe_3O_4 will yield 3 moles Fe_2O_3 when oxidized.

$$2 \text{ moles Fe}_3\text{O}_4 \equiv 3 \text{ moles Fe}_2\text{O}_3$$

$$\text{No. mol Fe}_3\text{O}_4 = 0.00930 \text{ mole Fe}_2\text{O}_3 \times \frac{2 \text{ mole Fe}_3\text{O}_4}{3 \text{ mole Fe}_2\text{O}_3} = 0.00620 \text{ moles Fe}_3\text{O}_4$$

$$\text{Weight Fe}_3\text{O}_4 \text{ in sample} = 0.00620 \text{ mole} \times 231.55 \text{ gm / mole}$$

$$= 1.437 \text{ gm Fe}_3\text{O}_4$$

$$\text{Percentage Fe}_3\text{O}_4 = 1.437 \text{ gm} / 1.542 \text{ gm} \times 100 = 93.1 \%$$

Calculations involving concentrations of solutions

- 1- Physical methods :- the simplest ways of expressing the strength of a solution are in terms of the amount of solute present per unit amount of solvent or solution. Such methods are known as physical methods because they are based only on physical measurements of weight or volume and do not take into account the chemical reactions of the solute.

The more widely used physical methods are :

- 1- Grams solute per liter (or 1000ml) solution gm/L(solution)
gm/1000ml(solution).
- 2- Grams solute per liter (or 1000ml) solvent.
gm/L(solvent) gm/1000ml (solution).
- 3- Grams solute per unit weight of solution gm/gm (solution)
- 4- Grams solute per unit weight of solvent gm/gm(solvent)

1- Percentage methods.

$$\text{Weight percent (w/w)} = \frac{\text{mass solute}}{\text{mass solution}} \times 100\%$$

$$\text{Volume percent (v/v)} = \frac{\text{volume solute}}{\text{volume solution}} \times 100\%$$

$$\text{Weight / volume percent (w/v)} = \frac{\text{mass solute,g}}{\text{volume solution,ml}} \times 100\%$$

Ex/Express the concentration with weight percent of the solution weighting 25.0gm and contained in 200.0gm of sodium sulphate Na_2SO_4 .
Solution/

$$\begin{aligned} \%(w/w) &= \frac{\text{weight of solute}}{\text{weight of solution}} \times 100 \\ &= \frac{25.0\text{gm solute}}{200.0\text{gm solution}} \times 100 = 12.5\% \end{aligned}$$

Ex/Use the weight percent, calculate the concentration of the solution when 3gm AgNO_3 dissolve in 1L distilled water ?

Solution/1L H_2O → weight H_2O

$$\text{Density} = \frac{\text{weight}}{\text{volume}}$$

$$\text{Weight (H}_2\text{O)} = \text{density} \times \text{volume}$$

$$= \frac{1\text{gm}}{\text{cm}^3} \times 1\text{L} \times \frac{1000\text{ cm}^3}{\text{L}}$$

$$\text{Weight} = \text{weight} + \text{weight}$$

$$\text{(solution)} \quad \text{(solute)} \quad \text{(solvent)}$$

$$= 3\text{gm} + 1000\text{gm} = 1003\text{gm}$$

$$(w/w)\% = \frac{3\text{gm}}{1003\text{gm}} \times 100 = 0.299\% \rightarrow 0.3\%$$

Ex/Use the volume percent, calculate the concentration of the solution is prepared by addition 50.0ml methanol (CH₃OH) to 200.0ml water?

Solution/

$$\text{Volume(solution)} = 50.0\text{ml} + 200.0\text{ml} = 250.0\text{ml}$$

$$V/V \% = \frac{50 \text{ ml}}{250 \text{ ml}} \times 100 = 20.0 \%$$

$$\text{PPM (wt/wt)} = \frac{\text{mass of solute (g)}}{\text{mass of sample (g)}} * 10^6$$

Example 1: A sample with mass of 2.6 g contains 3.6 Mg of Zinc. Calculate the concentration of Zinc in ppm.

Solution:

$$\text{PPM (wt/wt)} = \frac{\text{mass of zinc}}{\text{mass of sample}} * 10^6$$

$$\text{Conc. of Zinc} = \frac{3.6 * 10^{-6} \text{ g}}{2.6 \text{ g}} * 10^6 = 1.4 \text{ ppm}$$

Example 2: A 25 mL serum sample was analyzed for glucose content and found to contain 26.7 Mg. Calculate the concentration of glucose in ppm and in mg/dL.

Solution:

$$\text{PPM (wt/vol)} = \frac{\text{mass of glucose (g)}}{\text{Vol. of sample (ml)}} * 10^6$$

$$\text{Conc. of glucose} = \frac{26.7 * 10^{-6} \text{ g}}{25 \text{ mL} * \frac{\text{ml}}{10^3 \text{ mL}}} * 10^6 = 1068 \text{ ppm}$$

$$\text{Conc. of glucose} = \frac{\text{mass of glucose (mg)}}{\text{Vol. of sample dL}}$$

$$= \frac{26.7 \text{ Mg} * \frac{\text{mg}}{10^3 \text{ Mg}}}{25 \text{ mL} * \frac{\text{L}}{10^6 \text{ mL}} * \frac{10 \text{ dL}}{\text{L}}} = 106.8 \text{ mg/dL}$$

Acid – base equilibria and PH of solutions

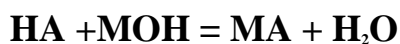
An acid is a substance that furnishes protons or H⁺ ions and a base a substance that accepts protons. In classical terminology the acid HA dissociates in aqueous solution according to the equation



And a base MOH dissociates to give M⁺ + OH⁻ ions. The reaction of HA with MOH is



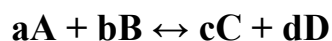
And a base MOH dissociates to give M⁺ + OH⁻ ions. The reaction of HA with MOH is



This reaction goes more or less to completion because the H₂O molecule is only slightly dissociated. To understand the limitations of acid-base titrations and the selection of proper indicators for such titrations, the student must understand the equilibrium relations involved in neutralization reactions.

Equilibrium constant :

A chemical reaction is at equilibrium when the rates of the forward and the concentrations of the reacting components are related by the equilibrium constant equation. For the reaction



We have the relation

$$K_e = \frac{[\text{D}]^d [\text{C}]^c}{[\text{A}]^a [\text{B}]^b}$$

In which the square brackets indicate the molar concentrations of the reacting species, and each molar concentration is raised to a power that is the coefficient of that substance in the chemical equation. The constant K_e is known as the equilibrium constant. Conventionally the products of the reaction are written in the numerator of the expression.

The equilibrium constant is experimentally determined for every reaction by measuring the concentrations of the reacting species after a condition of equilibrium has been attained. The constant is valid only at the temperature at which the determination is made, a change in temperature will change the equilibrium concentrations, there by changing the numerical value of K_e .

Factors effecting the equilibrium state:

Temperature , Pressure , Concentration, Time, Volume and Catalyst.

pH and Hydrogen ion concentration

Pure water dissociates slightly, forming equivalent amounts of hydronium and hydroxide ions , according to the equation



The H^+ ion formed by dissociation of one H_2O molecule unites with another H_2O molecule to form an hydronium ion. At room temperature the concentration of H_3O^+ and OH^- ions in pure water are each 1×10^{-7} molar.

The equilibrium expression for dissociation of water is :

$$K_e = [\text{H}_3\text{O}^+] [\text{OH}^-] / [\text{H}_2\text{O}]^2$$

Since $[\text{H}_2\text{O}]$ is constant, we have

$$[\text{H}_3\text{O}^+] [\text{OH}^-] = K_w$$

The constant K_w is evaluated by substituting known numerical values for the concentrations of the ions and solving this gives

$$K_w = (1 \times 10^{-7}) (1 \times 10^{-7}) = 1 \times 10^{-14}$$

This is the value for the constant at 25 °C .

The obvious simple solution is to use a related function , known as pH, to express hydronium ion concentrations .The function pH is defined by the equation

$$\text{pH} = - \log [\text{H}_3\text{O}^+]$$

which also gives corresponding values for the concentration of OH^- ion pOH, defined by

$$\text{pOH} = -\log [\text{OH}^-]$$

It will be noted that the sum $\text{pH} + \text{pOH}$ is always 14 when the solution is at room temperature

$$\text{pH} + \text{pOH} = 14$$

Ex/ What is the pH of a solution in which the hydronium ion concentration is 0.0002 M ?

Solution / $[\text{H}_3\text{O}^+] = \text{M} = 2 \times 10^{-4}$

$$\begin{aligned}\text{pH} &= -\log [\text{H}_3\text{O}^+] \\ &= -\log (2 \times 10^{-4}) = -\log 2 + 4 \log 10 \\ &= -0.30 + 4 \\ &= 3.7\end{aligned}$$

Ex/The pH of a solution is 5.40. What is the concentration hydronium ion?

Solution /

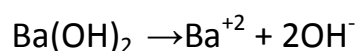
$$\begin{aligned}\text{pH} &= 5.40 \\ \text{pH} &= -\log [\text{H}_3\text{O}^+] \\ [\text{H}_3\text{O}^+] &= 10^{-\text{pH}} = 10^{-5.4} = 10^{-6} \times 10^{+0.6} \\ &= 3.98 \times 10^{-6} \approx 4 \times 10^{-6}\end{aligned}$$

Ex/ What is the OH^- concentration in 0.001 M of HCl solution? What is the H^+ concentration derived from the dissociates of the solvent ?

Solution /

$$\begin{aligned}K_w &= [\text{H}^+] [\text{OH}^-] \\ 1 \times 10^{-14} &= (0.001)[\text{OH}^-] \\ [\text{OH}^-] &= 1 \times 10^{-14} / 1 \times 10^{-3} = 1 \times 10^{-11} \text{M} \\ \text{H}_2\text{O} &\leftrightarrow \text{H}^+ + \text{OH}^- \\ [\text{OH}^-] &= [\text{H}^+] = 1 \times 10^{-11}\end{aligned}$$

Ex/ What are the concentration of H^+ and OH^- in 0.0030 M solution of $\text{Ba}(\text{OH})_2$?

Solution /

$$K_w = [\text{OH}^-] [\text{H}^+]$$

$$1 \times 10^{-14} = (2 \times 0.003) [\text{H}^+]$$

$$[\text{H}^+] = 1 \times 10^{-14} / 6 \times 10^{-3} = 1.6 \times 10^{-12}$$

$$[\text{OH}^-] 2 \times 0.003 = 6 \times 10^{-3}$$

Ex / A sample of blood found to have a pH 3.80. What were the H^+ and OH^- concentration in the blood?

Solution /

$$\text{pH} = -\log [\text{H}^+]$$

$$3.8 = -\log [\text{H}^+]$$

$$[\text{H}^+] = 10^{-3.8}$$

$$= 10^{-4} \times 10^{+0.2} = 1.58 \times 10^{-4}$$

$$= 1.6 \times 10^{-4}$$

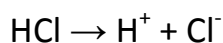
$$[\text{H}^+] [\text{OH}^-] = 1 \times 10^{-14}$$

$$[\text{OH}^-] = 1 \times 10^{-14} / 1.6 \times 10^{-4} = 6.25 \times 10^{-11}$$

Expression of equilibrium constant in acidic medium

For strong acid, such as HCl, we never need to write law of chemical equilibrium because the dissociation almost completely. However, is a weak acid and its reaction with water is an equilibrium law.

Ex / What is the pH of a 0.005 M solution of HCl at 25°C ?

Solution /

$$[\text{H}^+] = 0.005 \text{ M} = 5 \times 10^{-3} \text{ M}$$

$$\text{pH} = -\log [\text{H}^+] = -\log 5 \times 10^{-3}$$

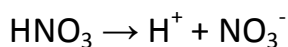
$$\text{pH} = -[\log 5 + \log 10^{-3}]$$

$$= -0.7 + 3$$

$$\text{pH} = 2.7$$

Ex / What is the pOH of a 2×10^{-4} M solution of HNO_3 ?

Solution /



$$[\text{H}^+] = 2 \times 10^{-4} \text{M}$$

$$\text{pH} = -\log [\text{H}^+] = -\log 2 \times 10^{-4}$$

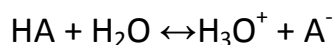
$$= -[\log 2 + \log 10^{-4}]$$

$$= -0.3 + 4 = 3.7$$

$$\text{pH} + \text{pOH} = \text{pK}_w = 14$$

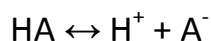
$$\text{pOH} = 14 - \text{pH} = 14 - 3.7 = 10.3$$

Expression of equilibrium constant for a weak acid in aqueous solution in the general equation:



$$K_a = \frac{[\text{H}_3\text{O}^+][\text{A}^-]}{[\text{HA}][\text{H}_2\text{O}]}$$

$[\text{H}_2\text{O}] = \text{constant}$

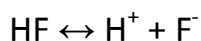


$$K_a = \frac{[\text{H}^+][\text{A}^-]}{[\text{HA}]}$$

K_a = acid dissociation constant for weak acid

Ex / Express the acid dissociation constant for weak acid HF is dissolved in water ?

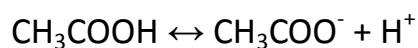
Solution /



$$K_a = \frac{[\text{H}^+][\text{F}^-]}{[\text{HF}]}$$

Ex / / What is the pH of 0.02M solution of acetic acid ? $K_a = 1.8 \times 10^{-5}$

Solution /



$$0.02 \quad 0 \quad 0$$

$$0.02 - X \quad X \quad X$$

$$K_a = [\text{CH}_3\text{COO}^-] [\text{H}^+] / [\text{CH}_3\text{COOH}]$$

$$1.8 \times 10^{-5} = (X)(X) / (0.02 - X)$$

Neglects

$$X^2 = 36 \times 10^{-8}$$

$$X = 6 \times 10^{-4} \text{ M} = [\text{H}^+]$$

$$\text{pH} - \log [\text{H}^+] = -\log 6 \times 10^{-4} = -0.78 + 4 = 3.22$$

ملاحظة : يهمل (x) في الحالة التي يكون فيها ثابت تفكك الحامض الضعيف (K_a) يساوي

10⁻⁵ , 10⁻⁶.....فما دون

طريقة اخرى للحل

$$\text{pH} = 1/2 (\text{pK}_a - \log M_a)$$

$$\text{pK}_a = -\log K_a \quad , \quad M_a = [\text{H}^+] = [\text{Acid}]$$

$$\text{pH} = 1/2 (-\log K_a - \log M_a)$$

$$= 1/2 (-\log 1.8 \times 10^{-5} - \log 0.02)$$

$$= 1/2(4.47 + 1.7) = 3.22$$

Example 1: Calculate the pH of a $2 \times 10^{-3} M$ of hydrochloric acid solution.

Solution: since HCl is a strong electrolyte and it is completely ionized.

$$[H^+] = 2 \times 10^{-3} M$$

$$pH = -\log[H^+] = -\log(2 \times 10^{-3}) = \underline{\underline{2.7}}$$

Example 2: Calculate the pOH and the pH of a $5 \times 10^{-2} M$ solution of NaOH.

Solution:

$$[OH^-] = 5 \times 10^{-2} M$$

$$pOH = -\log[OH^-] = -\log(5 \times 10^{-2}) = \underline{\underline{1.3}}$$

$$pH + pOH = 14$$

$$\therefore pH = 14 - 1.3 = \underline{\underline{12.7}}$$

Example 3: Calculate the hydrogen ion concentration of a solution with $pH = 9.67$.

Solution:

$$pH = -\log[H^+] = 9.67$$

$$[H^+] = 10^{-9.67} = \underline{\underline{2.14 \times 10^{-10} M}}$$

Acid - Base strength:

When an acid or base is dissolved in water, it will dissociate or ionize. The degree of ionization depends on the strength of the acid. A "strong" electrolyte is completely dissociated, while a "weak" electrolyte is partially dissociated. Hence, a weak acid has a relatively small dissociation constant (K_a), whereas a strong acid has a large dissociation constant.

Similarly, a strong base has a large (K_b) and a weak base has small (K_b).

A list of some common strong and weak electrolytes are shown in the following table.

strong Electrolytes

HCl, HI
HClO₄, HBr
H₂SO₄
HNO₃
NaOH, KOH
Ba(OH)₂, LiOH

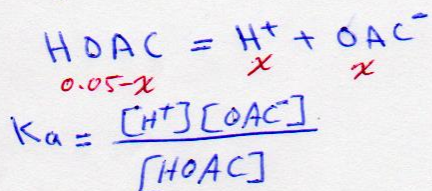
Weak Electrolytes

acetic acid CH₃COOH, HCOOH formic acid
HF, HNO₂, HCN hydrocyanic acid
H₂S, H₂SO₃
NH₃, C₆H₅OH phenol
C₆H₅NH₂ aniline
N₂H₄CO Urea

Example 1: calculate the pH of a 0.05 M solution of acetic acid? $K_a = 1.8 \times 10^{-5}$

Solution:

The acetic acid dissociates according to the equation:



Let concentration of $\text{H}^+ = x$

conc. of $\text{OAC}^- = x$

conc. of HOAC undissociation = $0.05 - x$

$$\frac{x^2}{0.05 - x} = 1.8 \times 10^{-5}$$

$0.05 - x \approx 0.05$ [that x is negligible in comparison with 0.05]

$$\frac{x^2}{0.05} = 1.8 \times 10^{-5} \Rightarrow x^2 = 9 \times 10^{-7} \Rightarrow x = 9.49 \times 10^{-4} \text{ M} = [\text{H}^+]$$

$$\text{pH} = -\text{Log}[\text{H}^+] = -\text{Log}[9.49 \times 10^{-4}] = \underline{\underline{3.02}}$$

The generalized approximate equation for the dissociation of a weak acid is:

$$[\text{H}^+] = \sqrt{K_a \cdot C}$$

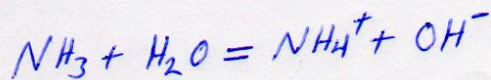
Where:

C is the concentration of the weak acid.

Example 2: what is the pH of a 0.1 M NH_3 solution?

$$K_b = 1.75 \times 10^{-5}$$

Solution:



$$0.1 - x \qquad \qquad x \qquad \qquad x$$

$$\frac{x^2}{0.1 - x} = 1.75 \times 10^{-5} \Rightarrow x^2 = 1.75 \times 10^{-6} \Rightarrow x = 1.32 \times 10^{-3} \text{ M} = [\text{OH}^-]$$

negligible

$$\text{pOH} = -\text{Log} [\text{OH}^-] = -\text{Log} (1.32 \times 10^{-3}) = 2.87$$

$$\text{pH} = 14 - \text{pOH} = \underline{11.12}$$

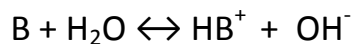
The generalized approximate equation for the dissociation of a weak base is:

$$[\text{OH}^-] = \sqrt{K_b \cdot C}$$

Expression of equilibrium constant in basic medium

For strong base, such as , NaOH , we never need to write law of chemical equilibrium because the dissociation almost completely. However, is a weak base and its reaction with water is an equilibrium law.

in the general quation:



$$K_a = [HB^+] [OH^-] / [B]$$

Ex/ What is the pH of a 0.0005 M solution of NaOH at 25 °C ?

Solution /



$$[OH^-] = 0.0005 \text{ M} = 5 \times 10^{-4} \text{ M}$$

$$pOH = -\log [OH^-]$$

$$= -\log 5 \times 10^{-4}$$

$$= -\log 5 + 4 \log 10$$

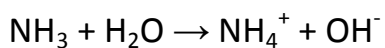
$$= -0.699 + 4$$

$$= 3.301$$

$$pH = 14 - 3.401 = 10.7$$

Ex/ What is the pH of a 0.1 M NH₃ solution ? K_b 1.8 x 10⁻⁵

Solution /



$$0.1 \qquad \qquad 0 \qquad 0$$

$$0.1 - X \qquad \qquad X \qquad X$$

$$K_b = [NH_4^+] [OH^-] / [NH_3]$$

$$1.8 \times 10^{-5} = (X)(X) / 0.1 - X$$

$$1.8 \times 10^{-5} = X^2 / 0.1$$

$$X^2 = 1.8 \times 10^{-6}$$

$$X = 1.34 \times 10^{-3} = [OH^-]$$

$$\text{pOH} = -\log [\text{OH}^-] = -\log 1.34 \times 10^{-3} = 2.87$$

$$\text{pOH} + \text{pH} = 14$$

$$\text{pH} = 14 - 2.87 = 11.12$$

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$$\text{pOH} = 1/2 [\text{pKb} - \log \text{Mb}]$$

$$\text{pKb} = -\log \text{Kb} \quad , \quad \text{Mb} = [\text{OH}^-] = [\text{Base}]$$

$$\text{pOH} = 1/2 [\text{pKb} - \log \text{Mb}]$$

$$= 1/2 [-\log 1.8 \times 10^{-5} - \log 0.1]$$

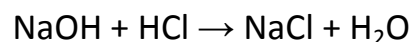
$$= 2.87$$

$$\text{pH} = 14 - 2.87 = 11.12$$

Calculation of pH of aqueous solution

Ex/ What is the pH of the resulting solution when 50 ml 0.1 M NaOH has been added to 75 ml 0.1 M HCl ?

Solution / Each mol of NaOH added neutralizes mole of HCl



$$\text{No. mmol HCl} = 75 \text{ ml} \times 0.1 \text{ mmol / ml} = 7.5 \text{ mmol}$$

$$\text{No. mmol NaOH} = 50 \text{ ml} \times 0.1 \text{ mmol / ml} = 5.0 \text{ mmol}$$

$$\text{No. mmol HCl remaining} = 7.5 - 5.0 = 2.5 \text{ mmol}$$

(unneutralized)

$$\text{Total volume} = 75 \text{ ml} + 50 \text{ ml} = 125 \text{ ml}$$

$$[\text{HCl}] = [\text{H}^+] = \text{no. mmol} / \text{volume ml} = 2.5 \text{ mmol} / 125 \text{ ml} = 0.02 \text{ M}$$

$$\text{pH} = -\log 0.02 = -\log 2 \times 10^{-2} = 1.7$$

Ex/ What is the pH of solution obtained by adding 85 ml 0.1 M NaOH to 75 ml 0.1 M HCl ?

Solution /

$$\text{No. mmol HCl} = 75 \text{ ml} \times 0.1 \text{ mmol / ml} = 7.5 \text{ mmol}$$

$$\text{No. mmol NaOH} = 85 \text{ ml} \times 0.1 \text{ mmol / ml} = 8.5 \text{ mmol}$$

$$\text{No. mmol NaOH an excess} = 8.5 - 7.5 = 1.0 \text{ mmol}$$

$$\text{Total volume} = 75 \text{ ml} + 85 \text{ ml} = 160 \text{ ml}$$

$$[\text{NaOH}] = [\text{OH}^-] = \text{no. mmol} / \text{volume ml} = 1.0 \text{ mmol} / 160 \text{ ml} = 6.25 \times 10^{-3} \text{ M}$$

$$\text{pOH} = -\log [\text{OH}^-] = -\log 6.25 \times 10^{-3} = 2.21$$

$$\text{pH} = 14 - \text{pOH} = 14 - 2.21 = 11.79$$

Weak acid plus its salt

If a salt that contains the same anion is added to solution of a weak acid, the effect is to decrease the concentration of hydronium ion. The salt, completely ionized, increases the concentration of the anion, thereby displacing the chemical equilibrium.

In the titration of a weak acid by a strong base, each mole of base added gives a mole of salt. The effect of this salt must be considered in computing the pH of the solution.

Ex/ What is the pH of an acetic acid solution when 85 ml 0.15 M NaOH have been added to 50 ml 0.1 M HOAc? $K_a = 1.8 \times 10^{-5}$, $\text{p}K_a = 4.74$



$$\text{No. mmol HOAc} = 50 \text{ ml} \times 0.1 \text{ mmol / ml} = 5.0 \text{ mmol}$$

$$\text{No. mmol NaOH} = 30 \text{ ml} \times 0.15 \text{ mmol / ml} = 4.5 \text{ mmol}$$

$$\text{No. mmol HOAc remaining} = 5.0 - 4.5 = 0.5 \text{ mmol}$$

$$\text{pH} = \text{p}K_a - \log \text{mmoles acid remaining} + \log \text{mmoles salt}$$

$$\text{pH} = 4.74 - \log 0.5 + \log 4.5$$

$$\text{pH} = 4.74 - (-0.3) + 0.65 = 5.7$$

Weak base plus salt with common ion

The treatment is similar to that for the weak acid.

Ex / What is the pH of a solution containing 0.535 gm NH_4Cl in 50ml 0.1M NH_3 ? $K_b = 1.8 \times 10^{-3}$

Solution / $\text{NH}_3 + \text{H}_2\text{O} \leftrightarrow \text{NH}_4^+ + \text{OH}^-$

No. mol $\text{NH}_4\text{Cl} = 0.535 \text{ gm} \times 1 \text{ mol} / 53.5 \text{ gm} = 0.01 \text{ mol}$

No. mmol = $0.01 \text{ mol} \times 1000 \text{ mmol} / \text{mol} = 10 \text{ mmol } \text{NH}_4\text{Cl}$

No. mmol $\text{NH}_3 = 50 \text{ ml} \times 0.1 \text{ mmol} / \text{ml} = 5.0 \text{ mmol}$

$\text{pOH} = \text{pK}_b - \log \text{ mmoles base} + \log \text{ mmoles salt}$

$\text{pOH} = 4.74 - \log 5.0 + \log 10$

$\text{pOH} = 4.74 - 0.699 + 1.0 = 5.04$

$\text{pH} = 14 - 5.04 = 8.96$

salt of weak acid and strong base

when an equivalent amount of NaOH has been added to a solution of a weak acid (such as HOAc), the solution is not neutral, as it is when an equivalent amount of strong base has been added to a strong acid. The reason is that two bases, the OAc^- and the OH^- ions, are competing for the protons. At the equivalence point we have added a mole of OH^- ion for each mole of HOAc originally present. But, since a small fraction of the total number of protons is still held by the OAc^- ion, as undissociated HOAc molecules, we have an excess of OH^- ions present.

The pH of the solution is computed from the equilibrium constant of the two competing reaction.

Ex / What is the pH at the equivalence point when 50 ml 0.1 M NaOH is titrated with 0.1 M NaOH ? $K_a = 1.8 \times 10^{-5}$

Solution /

$\text{pH} = 1/2 (\text{pK}_w + \text{pK}_a + \log M_s)$

$\text{pK}_w = - \log K_w = - \log 1 \times 10^{-14} = 14$

$\text{pK}_a = - \log K_a = - \log 1.8 \times 10^{-5} = 4.74$

$M_s = [\text{salt}] = \text{no of moles salt} / \text{total volume}$

No.mmol HOAc = 50 ml x 0.1 mmol / ml = 5.0 mmol

At equivalent point:

mmoles of acid = mmols of base

no.mmolNaOH = 50 ml x 0.1 mmol / ml = 5.0 mmol

Total volume = (50 + 50)ml = 100 ml

$M_s = 5.0 \text{ mmol} / 100 \text{ ml} = 0.05 \text{ M}$

$\text{pH} = 1/2 (\text{pK}_w + \text{pK}_a + \log M_s)$

$= 1/2(14 + 4.74 + \log 0.05)$

$= 8.71$

The general expression for the concentration of OH^- ion in a solution of a salt of a weak acid and strong base is

$$[\text{OH}^-] = \sqrt{\frac{C_s K_w}{K_a}}$$

$$[\text{H}^+] = \sqrt{\frac{K_w K_a}{C_s}}$$

Where C_s is the salt concentration , neglecting the small amount which **reacts**.

Salt of weak base with strong acid

The equilibrium expression is treated exactly the same as for a weak acid

Ex / What is the pH of a solution containing 10mmol NH_4Cl in a volume of 100ml ? $K_b = 1.8 \times 10^{-5}$

Solution /

$\text{pH} = 1/2 (\text{pK}_w - \text{pK}_b - \log M_s)$

$M_s = [\text{salt}] = \text{no.moles salt} / \text{total volume} = 10 \text{ mmol} / 100 \text{ ml} = 0.1 \text{ M}$

$\text{pH} = 1/2(14-4.74 +1)=5.13$

$$\begin{aligned}
[\text{H}^+] &= \sqrt{[\text{CS}] \frac{K_w}{K_b}} \\
&= \sqrt{\frac{0.1 \times 10^{-14}}{1.8 \times 10^{-5}}} = \sqrt{\frac{1 \times 10^{-10}}{1.8}} \\
&= 0.7 \times 10^{-5}
\end{aligned}$$

$$\begin{aligned}
\text{pH} &= -\log [\text{H}^+] = -\log [0.7 \times 10^{-5}] \\
&= -\log 0.7 + 5\log 1 \\
&= -(-0.127 - 5) = 5.127
\end{aligned}$$

Buffers solution

A buffer solution is one that contains a weak acid and its salt or a weak base and its salt. The name is based on the fact that an acid or base added to a buffer solution causes less change in pH than an acid or base added to pure water or to an unbuffered solution. To illustrate the buffer effect, we shall consider a solution containing acetic acid and a salt, sodium acetate or ammonium hydroxide and ammonium chloride.

Expression of the general equation for buffer solution is:

$$\text{pH} = \text{pK}_a + \log \frac{[\text{salt}]}{[\text{acid}]}$$

$$\text{pOH} = \text{pK}_b + \log \frac{[\text{salt}]}{[\text{base}]}$$

calculation of the pH of buffer solution

Ex / What is the pH of a solution that is 0.40 M in formic acid and 1.00 M in sodium formate? $K_b = 1.8 \times 10^{-4}$



$$\text{pH} = \text{pK}_a + \log \frac{[\text{salt}]}{[\text{acid}]}$$

$$\text{pK}_a = -\log 1.8 \times 10^{-4} = 3.75$$

$$\text{pH} = 3.75 + \log 1.00 / 0.40$$

$$= 3.75 + 0.39 = 4.14$$

Ex / Calculate the pH change that takes place when a 1.0 mole of HCl is added to 5.0 m each of acetic acid and sodium acetate? $K_a = 1.8 \times 10^{-5}$

Solution / Befor addation

$$\begin{aligned} \text{pH}_1 &= \text{pK}_a + \log \frac{[\text{salt}]}{[\text{acid}]} \\ &= 4.74 + \log 5.0 / 5.0 \\ &= 4.74 \end{aligned}$$

After addation HCl

$$\begin{aligned} \text{pH}_2 &= \text{pK}_a + \log \frac{\text{salt} - [\text{H}^+]}{\text{acid} + [\text{H}^+]} \\ &= 4.74 + \log \frac{5-1}{5+1} = 4.58 \end{aligned}$$

$$\Delta \text{pH} = \text{pH}_2 - \text{pH}_1$$

$$= 4.58 - 4.74 = -0.16$$

Ex / A mixture of NH_3Cl and 1.0 M NH_3 solution is prepared to give a buffer of pH 9.0. What quantities of each are required? if we use 100 ml NH_3 solution, $K_b = 1.8 \times 10^{-5}$

Solution / $\text{pH} + \text{pOH} = 14$

$$\text{pOH} = 14 - \text{pH} = 14 - 9.0 = 5$$

$$[\text{OH}^-] = 10^{-\text{pOH}} = 10^{-5}$$

$$[\text{OH}^-] = K_b \times \frac{nb}{ns}$$

$$10^{-5} = 1.8 \times 10^{-5} \times \frac{nb}{ns}$$

$$\frac{nb}{ns} = \frac{10^{-5}}{1.8 \times 10^{-5}}$$

$$\frac{nb}{ns} = \frac{1}{1.8} \Rightarrow \frac{ns}{nb} = 1.8$$

$$nb = 1.0 \text{ mmol / ml} \times 100 \text{ ml} = 100 \text{ mmol}$$

$$\frac{ns}{100 \text{ mmol}} = 1.8 \Rightarrow ns = 1.8 \times 100 \text{ mmol} = 180 \text{ mmol}$$

$$\text{Weight} = 180 \text{ mmol} \times 53.5 \text{ mg / mmol} = 9600 \text{ mg} = 9.6 \text{ gm}$$

Ex / Calculate the pH change that takes place when a 100.0 ml portion
 (a) 0.0500 M NaOH and (b) 0.0500 M HCl is added to 400.0 ml of
 the buffer solution that contains 0.3M ammonium chloride and 0.2 M
 NH₃ ? pK_b = 4.74 , K_b = 1.8 x 10⁻⁵

Solution / before add.

$$\text{pOH} = \text{pK}_b + \log \frac{[\text{salt}]}{[\text{base}]}$$

$$\text{pOH} = 4.74 + \log \frac{0.3}{0.2} = 4.92$$

$$\text{pH}_1 = 14 - 4.92 = 9.08$$

After addition 0.0500 M NaOH

$$[\text{NH}_3] = (0.20 \times 400 + 0.0500 \times 100) / 500 = 85.0 / 500 = 0.170 \text{ M}$$

$$[\text{NH}_4\text{Cl}] = (0.30 \times 400 - 0.0500 \times 100) / 500 = 115.0 / 500 = 0.230 \text{ M}$$

$$\text{pOH} = 4.74 + \log 0.230 / 0.170$$

$$= 4.74 + 0.13 = 4.87$$

$$\text{pH}_2 = 14 - 4.87 = 9.12$$

$$\Delta \text{pH} = \text{pH}_2 - \text{pH}_1 = 9.12 - 9.08 = 0.04$$

b- After addition 0.0500M HCl

$$[\text{NH}_3] = (0.20 \times 400 - 0.0500 \times 100) / 500 = 75.0 / 500 = 0.150 \text{ M}$$

$$[\text{NH}_4\text{Cl}] = (0.30 \times 400 + 0.0500 \times 100) / 500 = 125.0 / 500 = 0.250 \text{ M}$$

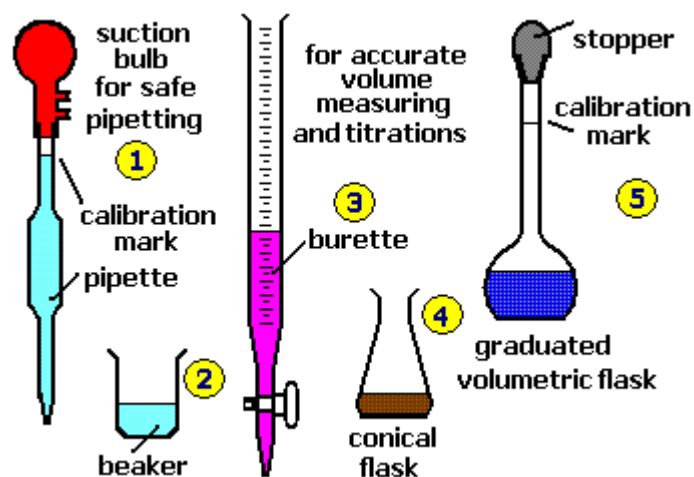
$$\text{pOH} = 4.74 + \log 0.250 / 0.150$$

$$= 4.74 + 0.22 = 4.96$$

$$\text{pH}_2 = 14 - 4.96 = 9.04$$

$$\Delta \text{pH} = \text{pH}_2 - \text{pH}_1 = 9.04 - 9.08 = -0.04$$

Dilution of solutions



A solution of known normality is frequently prepared from a more concentrated one of known strength by quantitative dilution.

$$N_{\text{conced}} \times V_{\text{conced}} = N_{\text{dil.}} \times V_{\text{dil.}}$$

Ex/What volume of 0.1500 N reagent is needed for the preparation of 500.0 ml ,0.100 N solution?

Solution/

$$N_{\text{conced}} \times V_{\text{conced}} = N_{\text{dil.}} \times V_{\text{dil}}$$

$$V_{\text{conced}} = \frac{N_{\text{dil}} \times V_{\text{dil}}}{N_{\text{conced}}} = \frac{0.100N \times 500.0 \text{ ml}}{0.1500N} = 333.3 \text{ ml}$$

Ex/ Describe the preparation of 100 ml 6.0 M HCl from a concentrated solution that has a specific gravity of 1.18 and is 37%(w/w)HCl?

Solution/

$$[\text{HCl}] = \frac{\text{sp.gr} \times \% \times 1000}{M.wt}$$

$$= \frac{1.18 \times 1000 \text{ gm reagent} \times 37 \text{ gm HCl} \times 1 \text{ mol HCl}}{L \text{ reagent} \times 100 \text{ gm reagent} \times 36.5 \text{ gm HCl}}$$

$$M = 12.0 \text{ mol/L} = 12.0 \text{ M}$$

$$\text{No. mol HCl} = 100 \text{ ml} \times 6.0 \text{ mmol/ml}$$

$$= 600.0 \text{ mmol} \times \frac{1 \text{ mol}}{1000 \text{ mmol}} = 0.6 \text{ mol}$$

$$V_{\text{conced reagent}} = 0.6 \text{ mol} \times \frac{1 \text{ l reagent}}{12.0 \text{ mol}} = 0.05 \text{ l} \times 1000 \text{ ml/l} \\ = 50 \text{ ml}$$

Thus dilute 50 ml of the concentrated reagent to 100 ml.

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$$M_{\text{conced}} \times V_{\text{conced}} = M_{\text{dil.}} \times V_{\text{dil.}}$$

$$12.0 \text{ M} \times V_{\text{conced}} = 6.0 \text{ M} \times 100 \text{ ml}$$

$$V_{\text{conced}} = \frac{6.0 \text{ M} \times 100 \text{ ml}}{12.0 \text{ M}} = 50 \text{ ml}$$

Ex/ What volume of H_2SO_4 reagent is needed for the preparation of 200.0 ml, 0.3 N solution that has a specific gravity of 1.84 and is 98%(w/w) H_2SO_4 ?

Solution/

$$[\text{H}_2\text{SO}_4] = \frac{1.84 \times 1000 \text{ gm reagent} \times 98 \text{ gm H}_2\text{SO}_4 \times 1 \text{ eq H}_2\text{SO}_4}{\text{L reagent} \times 100 \text{ gm reagent} \times 49.0 \text{ gm H}_2\text{SO}_4} \\ = 36.8 \text{ eq / L} = 36.8 \text{ N}$$

$$\text{No. eq H}_2\text{SO}_4 = 200.0 \text{ ml} \times 0.3 \text{ meq / ml} \\ = 60.0 \text{ meq}$$

$$V_{\text{conced reagent}} = 60.0 \text{ meq} \times \frac{1 \text{ ml}}{36.8 \text{ meq H}_2\text{SO}_4} = 1.63 \text{ ml}$$

Dilute 1.63 ml of the concentrated reagent to 200.0ml

Analysis of samples by titration with standard solution

Titrimetric methods include a large and powerful group of quantitative procedures that are based upon measuring the amount of a reagent of known concentration that is consumed by the analyte.

Volumetric titrimetry involves measuring the volume of a solution of known concentration that is needed to react essentially completely with the analyte.

Standard solution (standard titrant) : is a reagent of known concentration that is used to carry out a titrimetric analysis.

The equivalence point in titration is reached the amount of added titrant is chemically equivalent to the amount of analyte in the sample.

For example: the equivalence point in the titration of sodium chloride with silver nitrate occurs after exactly 1 mol of silver ion has been added for each mol of chloride ion in the sample.

The equivalence point in the titration of sulfuric acid with sodium hydroxide is reached after introduction of 2 mol of base for each mol of acid.

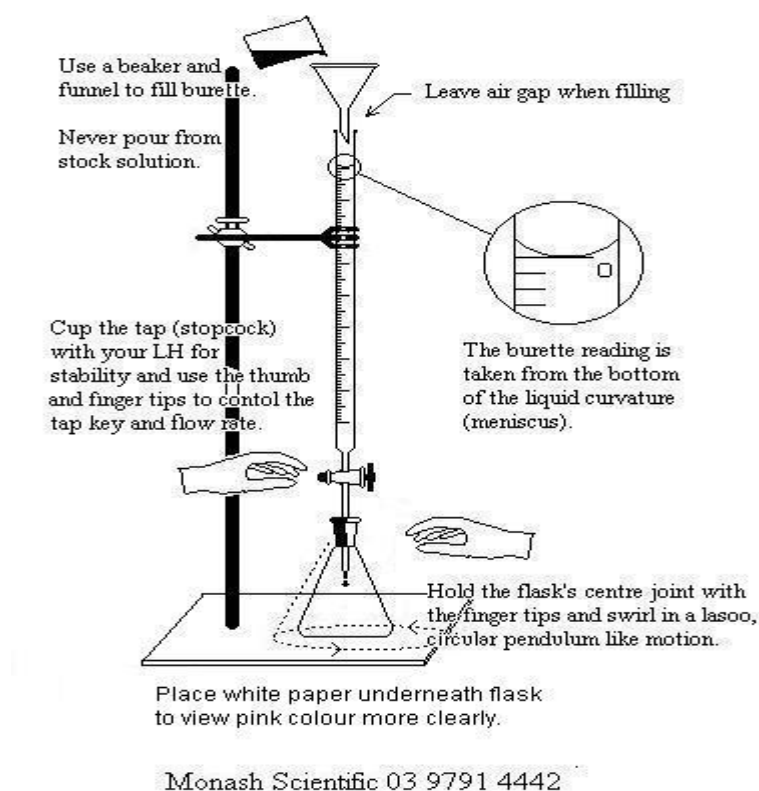
Acid and base samples are analyzed by titration with a standard solution. A weighed portion of sample is dissolved in water and standard acid or base is added to the proper end point. From the volume of reagent used and the weight of sample, the percentage purity of the sample is computed.

The basis for all computations dealing with normalities of solutions is the simple relation that the number of equivalents or milliequivalents of one reaction is equal to the number for the other reactant thus

A reacts with B

Equivalents A = Equivalents B

Milliequivalents A = Milliequivalents B



Ex/A sample of impure calcite (CaCO_3)(100.1 gm /mol) which weighs 0.4950 gm is dissolved in 50.00 ml of standard acid and the excess acid is titrated with 5.25 ml standard base; 1.00 ml of acid is equivalent to 0.005300 gm sodium carbonate; 1.050 ml acid = 1.00 ml base. Calculate the percentage of calcium carbonate in the sample.

Solution/

1 ml of acid \equiv 0.005300 gm Na_2CO_3

$$\text{N of acid} = \frac{5.300 \text{ mg}}{53.00 \text{ mg / meq}} \times \frac{1}{1 \text{ ml}} = 0.1000 \text{ meq / ml}$$

$$\begin{aligned} \text{Net volume acid required for titration of sample} &= 50.00 - \left(5.25 \times \frac{1.050}{1.000} \right) \\ &= 44.49 \text{ ml} \end{aligned}$$

$$\begin{aligned} \text{Milliequivalents acid} &= \text{Milliequivalents CaCO}_3 \\ &= 44.49 \text{ ml} \times 0.100 \text{ meq / ml} = 4.449 \text{ meq} \end{aligned}$$

$$\text{Milliequivalents CaCO}_3 = \frac{\text{weight of solute}}{\text{eq.wt}}$$

$$\begin{aligned} \text{Weight CaCO}_3 &= \text{Milliequivalents} \times \text{eq.wt} \\ &= 4.449 \text{ meq} \times \frac{100.1 \text{ mg/mmol}}{2 \text{ meq / mmol}} \\ &= 222.7 \text{ mg} \end{aligned}$$

$$\text{Percentage CaCO}_3 \text{ in sample} = \frac{222.7}{495.0} \times 100 = 44.99\%$$

Ex/ What must be the normality of sodium hydroxide solution if the volume in milliliters used for the titration of a 0.500 gm sample represents that percentage of acetic acid in the sample?

Solution/

$$1 \text{ eq acid} \equiv 1 \text{ eq base}$$

$$1 \text{ ml of NaOH} \equiv 0.5 \text{ gm \% acetic acid}$$

$$1 \text{ ml of NaOH} \equiv \frac{0.5 \text{ gm} \times 1000 \text{ mg/gm}}{100}$$

$$1 \text{ ml of NaOH} \equiv 5.00 \text{ mg acetic acid}$$



$$\text{N of NaOH} = \frac{5.00 \text{ mg/ml}}{60.05 \text{ mg/meq}} = 0.0833 \text{ meq/ml}$$

Ex/ What is the normality of hydrochloric acid solution having a sodium carbonate titer of a 5.00 mg per milliliter?

Solution/

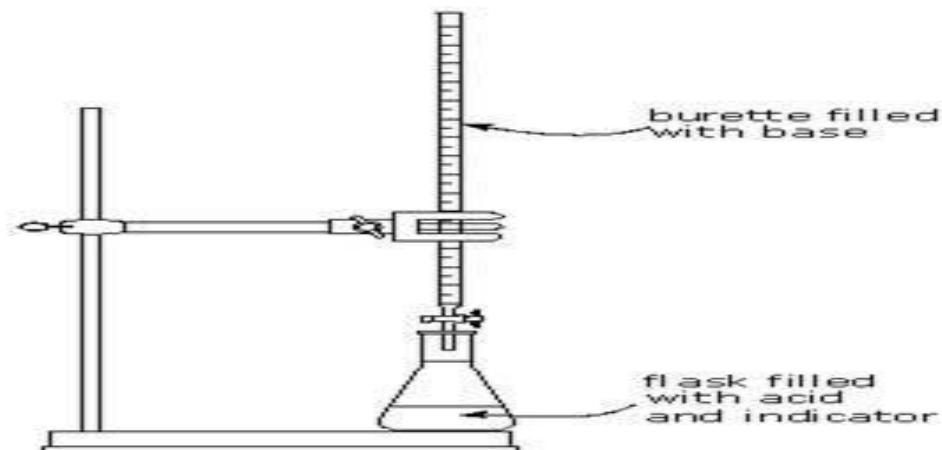
$$\text{N of base} \equiv \text{N of acid}$$

$$1 \text{ ml of acid} \equiv 5 \text{ mg Na}_2\text{CO}_3$$

$$N = \frac{wt}{eq.wt} \times \frac{1}{volume(ml)}$$

$$N = \frac{50\text{-}mg}{\frac{106\text{ }mg/mmol}{2\text{ }meq/mmol}} \times \frac{1}{1ml} = 0.094\text{ }meq/ml$$

Titration in the volumetric analysis



Titration : is an analytical procedure that allows us to measure the amount of a solution reagent of known concentration that is consumed by the analyte.

Titrant : is the solution reagent in buret.

Titrand : is the analyte in beaker.

End point : is the point in which the color of the indicator changes.

Indicator : is a substance (acid or base organic compound) that has one

Calculation of molarities from neutralization reaction (acid-base)

Ex/ Exactly 50.00 ml of an HCl solution required 29.71 ml of 0.0193M Ba(OH)₂ to reach an end point with bromocresol green indicator. Calculate the molarity of the HCL.

Solution:



1mmole of $\text{Ba(OH)}_2 \equiv 2\text{mmole of HCl}$

$$\text{Stoichiometric ratio} = \frac{2\text{mmole HCl}}{1\text{mmol Ba(OH)}_2}$$

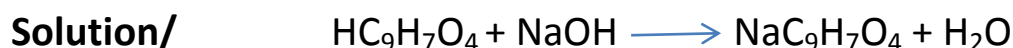
$$\begin{aligned}\text{No. moles Ba(OH)}_2 &= 29.71 \cancel{\text{ml}} \times 0.01963 \text{ mmol} / \cancel{\text{ml}} \\ &= 0.583 \text{ mmol}\end{aligned}$$

$$\begin{aligned}\text{No. mmoles HCl} &= 0.583 \cancel{\text{mmol Ba(OH)}_2} \times \frac{2\text{mmol HCl}}{1\text{mmol Ba(OH)}_2} \\ &= 1.166 \text{ mmol HCl}\end{aligned}$$

$$M_{\text{HCl}} = \frac{1.166\text{mmol HCl}}{50.0 \text{ ml HCl}} = 0.0233 \text{ mmol} / \text{ml} = 0.0233 \text{ M}$$

Ex/ Titration of a sample of a drug was analyzed for aspirin a monoprotic acid ($\text{HC}_9\text{H}_7\text{O}_4$) of 0.500 gm sample of the drug required 21.50 ml of 0.100M NaOH for complete neutralization.

What percentage by mass of the drug was aspirin?



1mmol of $\text{HC}_9\text{H}_7\text{O}_4 \equiv 1\text{mmol of NaOH}$

$$\begin{aligned}\text{No. mmoles NaOH} &= 21.50 \cancel{\text{ml}} \times 0.100 \text{ mmol} / \cancel{\text{ml}} \\ &= 2.15 \cancel{\text{mmol}} \times 10^{-3} \text{ mol} / \cancel{\text{mmol}} = 2.15 \times 10^{-3}\end{aligned}$$

mol

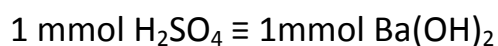
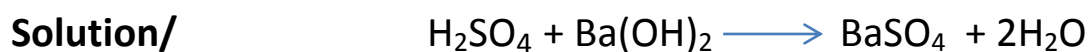
$$1 \text{ mol of HC}_9\text{H}_7\text{O}_4 \equiv 1 \text{ mol NaOH}$$

$$1 \text{ mol HC}_9\text{H}_7\text{O}_4 \equiv 180 \text{ gm}$$

$$\begin{aligned}\text{Mass of aspirin} &= 2.15 \times 10^{-3} \cancel{\text{mol}} \times 180 \text{ gm} / \cancel{\text{mol}} \\ &= 0.387 \text{ gm}\end{aligned}$$

$$\% \text{ Aspirin} = \frac{0.387 \text{ gm}}{0.500 \text{ gm}} \times 100 = 77.4 \%$$

Ex/ Calculate the molarity of the Ba(OH)₂ solution if 31.76 ml were needed to neutralize 46.25 ml of 0.1280 M H₂SO₄.



$$\text{Stoichiometric ratio} = \frac{1 \text{ mmol Ba}(\text{OH})_2}{1 \text{ mmol H}_2\text{SO}_4}$$

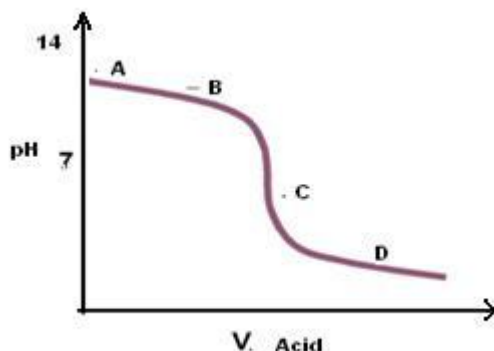
$$\begin{aligned} \text{No. mmoles H}_2\text{SO}_4 &= 46.25 \text{ ml H}_2\text{SO}_4 \times 0.1280 \text{ mmol H}_2\text{SO}_4 / \text{ml H}_2\text{SO}_4 \\ &= 5.92 \text{ mmol H}_2\text{SO}_4 \end{aligned}$$

$$\begin{aligned} \text{No. mmoles Ba}(\text{OH})_2 &= 5.92 \text{ mmol H}_2\text{SO}_4 \times \frac{1 \text{ mmol Ba}(\text{OH})_2}{1 \text{ mmol H}_2\text{SO}_4} \\ &= 5.92 \text{ mmol Ba}(\text{OH})_2 \end{aligned}$$

$$M_{\text{Ba}(\text{OH})_2} = \frac{5.92 \text{ mmol}}{31.76 \text{ ml}} = 0.1864 \text{ mmol / ml} = 0.1864 \text{ M}$$

Titration curves

Graphs of PH versus the volume of reagent added in a titration are known as titration curves.



Strong acid- strong base:

Note the following features of the titration:

1-The PH changes slowly at first ,until the equivalence point is approached.

2-In the region of the equivalence point there is a rapid change in PH. There is a nearly vertical rise in the region from pH 4 to 10.

3- After the equivalence point is passed, the curve flattens out, as excess of NaOH is added.

The curve will become as :

EX/ compute the pH for additions of 0,10,20, and 30ml 0.1M NaOH to 100 ml 0.025 M HCl . Use the computed values and the pH of 7.00 at the equivalence point to plot the titration curve.

Solution /

1-Before any NaoH added or initial pH

[acid] = 0.025 M

pH = $-\log [\text{acid}] = -\log [\text{H}^+] = -\log 0.025 = -(-1.6) = 1.6$

2-After addition of 10.0ml of NaOH

$$\text{No. mmols acid} = 0.025 \text{ mmol/ml} \times 100 \text{ ml} = 2.5 \text{ mmol}$$

$$\text{No. mmols acid (reacted)} = n. \text{ moles NaOH} = 10.0 \text{ ml} \times 0.1 \text{ mmole/ml} = 1.0 \text{ mmol}$$

$$\text{No. mmols acid (unreacted)} = 2.5 - 1.0 = 1.5 \text{ mmol}$$

$$\text{Volume (solution)} = 100 + 10 = 110 \text{ ml}$$

$$[\text{acid}] \text{ unreacted} = [\text{H}^+] = 1.5 \text{ mmol} / 110 \text{ mmol} = 0.0136 \text{ M}$$

$$\text{pH} = -\log [\text{H}^+] = -\log 0.0136$$

$$= -(-1.866) = 1.866$$

3- At equivalence point after addition 25 ml of NaOH

At the equivalence point:

$$[\text{H}_3\text{O}^+] = [\text{OH}^-] = 10^{-7}$$

$$n_{\text{HCl}} - n_{\text{NaOH}} = 0 \rightarrow \text{eq. point}$$

pH=7 → Bromothymol blue

4- After addition excess of NaOH , 30 ml NaOH added

$$\text{no. mmols NaOH (react)} = \text{no. mmols acid} = 2.5 \text{ mmol}$$

$$\text{no. mmols NaOH (added)} = 30.0 \text{ ml} \times 0.1 \text{ mmol/ml} = 3.0 \text{ mmol}$$

$$\text{no. mmols (NaOH) unreacted (excess)} = 3.0 - 2.5 = 0.5 \text{ mmol}$$

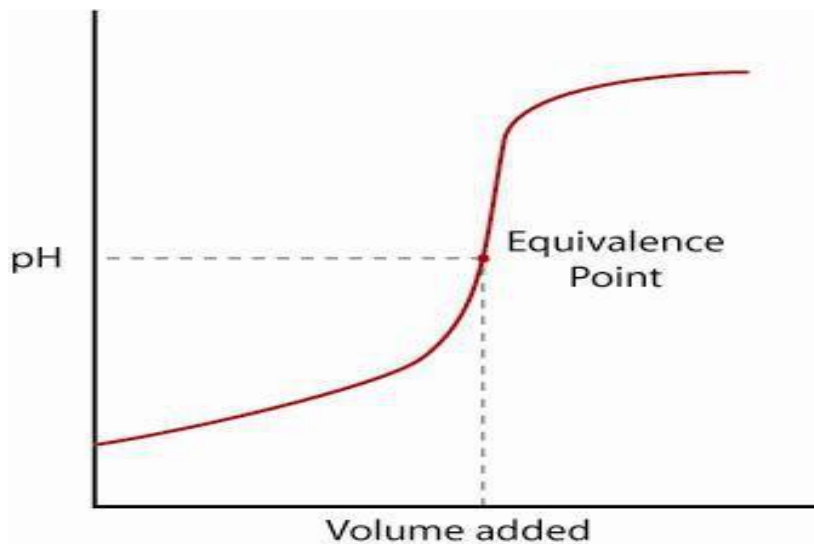
$$\text{volume of solution} = 100 + 30 = 130 \text{ ml}$$

$$[\text{base}] \text{ excess} = [\text{OH}^-] = 0.5 \text{ mmol} / 130 \text{ ml} = 0.0038$$

$$\text{pOH} = -\log [\text{OH}^-] = -\log 0.0038$$

$$= -(-2.415) = 2.415$$

$$\text{pH} = 14 - 2.415 = 11.585$$



Weak acid – strong base

The curve will be become as :

EX/ compute the pH of 25.0 ml 0.1 M acetic acid at addition of 0,5,10,12.5,20,25,and 30 ml 0.1 M NaOH ? $K_a = 1.8 \times 10^{-5}$, $pK_a = 4.76$

Solution /

1-before added any NaOH or initial pH

$$pH = 1/2 (pK_a - \log M_a)$$

$$pH = 1/2 (4.76 - \log 0.1)$$

$$pH = 1/2 (4.76 + 1) = 1/2 (5.76)$$

$$= 2.88$$

2-After addition 5.0 ml NaOH

$$pH = pK_a - \log \text{mmoles acid (unreacted)} + \log \text{mmoles salt/NaOH}$$

$$\text{No. mmoles HCl} = 25.0 \text{ ml} \times 0.1 \text{ mmol/ml} = 2.5 \text{ mmol}$$

$$\text{No. mmoles NaOH} = 5.0 \text{ ml} \times 0.1 \text{ mmol/ml} = 0.5 \text{ mmol}$$

$$\text{No. mmoles HCl (unreacted)} = 2.5 - 0.5 = 2.0 \text{ mmol}$$

$$pH = 4.76 - \log 2.0 + \log 0.5$$

$$= 4.76 - 0.30 - 0.30 = 4.16$$

3- After addition of 12.5 ml of NaOH

في هذه الحالة يتم معادلة نصف الحامض وان تركيز الحامض يصبح مساويا الى تركيز الملح لذلك فان :

$$pH = pka$$

$$pH = 4.76$$

$$\text{No. mmols HCl} = 25 \text{ ml} \times 0.1 \text{ mmol/ml} = 2.5 \text{ mmol}$$

$$\text{No. mmols NaOH (salt)} = 12.5 \text{ ml} \times 0.1 \text{ mmol/ml} = 1.25 \text{ mmol}$$

$$\text{No. mmol HCl (unreacted)} = 2.5 - 1.25 = 1.25 \text{ mmol}$$

$$pH = pka - \log \text{ mmols acid unreacted} + \log \text{ mmols salt (NaOH)}$$

$$= 4.76 - \log 1.25 + \log 1.25$$

$$pH = 4.76$$

4- At eq .point (after addition of 25.0 ml of NaOH)

$$\text{No. mmols acid} = 2.5 \text{ mmol}$$

$$\text{No. mmols NaOH} = 25.0 \text{ ml} \times 0.1 \text{ mmol/ml} = 2.5 \text{ mmol}$$

$$\text{No .mmols acid (unreacted)} = 2.5 - 2.5 = 0 \quad \text{this is eq . point}$$

ملاحظة:- عندما يكون عدد مولات القاعدة المضافة مساوية لعدد مولات الحامض الاصلي فان تلك هي نقطة التكافؤ ، والمحلول في هذه الحالة يحتوي على خلاص الصوديوم فقط لذلك يمكن حساب pH بالشكل التالي :

$$pH = 1/2 (pkw + pka + \log Ms)$$

$$pkw = 14 \quad \text{from } kw = 1 \times 10^{-14}$$

$$pka = 4.76 \quad \text{from } ka = 1.8 \times 10^{-5}$$

$$Ms = [\text{salt}] = (\text{no. mmols NaOH}) / (\text{total volume}) = (25.0 \text{ ml} \times 0.1 \text{ M}) / 25 + 25$$

$$= 2.5 / 50 = 0.05 \text{ M}$$

$$pH = 1/2 (14 + 4.76 + \log 0.05)$$

$$= 1/2 (14 + 4.76 - 1.30)$$

$$= 8.73 \rightarrow \text{phenolphthalein}$$

5- After eq . point (excess of NaOH) addition of 25.1 of NaOH

No.mmoles HCl = 25 ml \times 0.1 mmol/ml = 2.5 mmol

No.mmoles NaOH = 25.1 ml \times 0.1 mmol/ml = 2.51 mmol

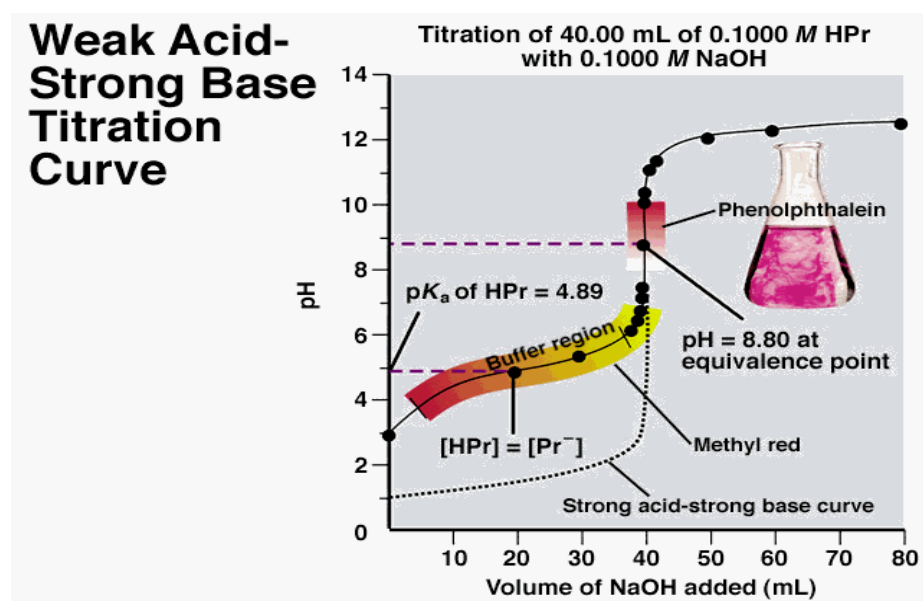
No.mmol NaOH excess = 2.51 – 2.5 = 0.01 mmol

Volume =(25 + 25.1)ml = 50.1ml

$[\text{OH}^-] = 0.01 \text{ mmol} / 50.1 \text{ ml} = 0.0001996\text{M}$

$\text{pOH} = -\log [\text{OH}^-] = -\log 1.996 \times 10^{-4} = 3.7$

$\text{pH} = 14 - 3.7 = 10.3$



Gravimetric analysis

Gravimetric analysis describes a set of methods used in analytical chemistry for the quantitative determination of an analyte (the ion being analyzed) based on its mass. The principle of this type of analysis is that once an ion's mass has been determined as a unique compound, that known measurement can then be used to determine the same analyte's mass in a mixture, as long as the relative quantities of the other constituents are known.

The four main types of this method of analysis are

- 1-precipitation
- 2- volatilization
- 3-electro-analytical
- 4- miscellaneous physical method.

The methods involve changing the phase of the analyte to separate it in its pure form from the original mixture and are quantitative measurements.

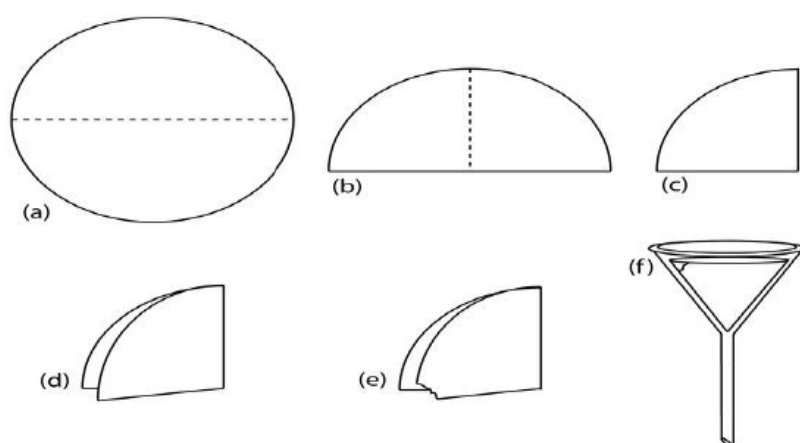
Step of gravimetric analysis

1. The sample is dissolved (water ,acid and base), if it is not already in solution.

2. The solution may be treated to adjust the pH (so that the proper precipitate is formed, or to suppress the formation of other precipitates).



3. The precipitating reagent is added at a concentration that favors the formation of a "good" precipitate . This may require low concentration, extensive heating, or careful control of the pH. Digestion can help reduce the amount of coprecipitation.
4. After the precipitate has formed and been allowed to "digest", the solution is carefully filtered. The [filter](#) is used to collect the precipitate; smaller particles are more difficult to filter.



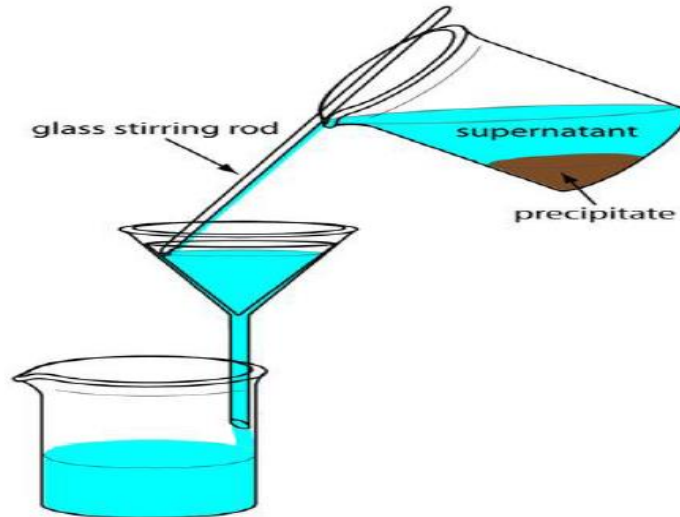


Figure 2 Proper procedure for transferring the supernatant to the filter paper cone.

5. After filtration, the precipitate – including the filter paper or crucible – is heated, or charred. This accomplishes the following:
6. After the precipitate is allowed to cool (preferably in a **desiccator** to keep it from absorbing moisture), it is weighed (in the crucible). To calculate the final mass of the analyte, the starting mass of the empty crucible is subtracted from the final mass of the crucible containing the sample. Since the composition of the precipitate is known, it is simple to calculate the mass of analyte in the original sample.

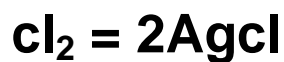
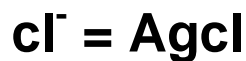
$$\% \text{ analyte} = \frac{\text{weight of analyte}}{\text{weight of sample}} \times 100$$

Gravimetric Factor(G.F)

$$\mathbf{G.F} = \frac{\text{equivalent weight of unknown substance}}{\text{equivalent weight of known substance}} \times \frac{a}{b}$$

Where a/b : is the stoichiometric ratio between the element and the precipitate

For example ,if is required to determine the percentage of chloride in sample ,then chloride ion is converted by precipitating reagent to AgCl



a b

$$\frac{g\text{Cl}_2}{g\text{AgCl}} = \frac{M.\text{wt Cl}_2}{M.\text{wt AgCl}} \times \frac{1 \text{ mole Cl}_2}{2 \text{ mole AgCl}}$$

Similarity $\text{Cl}_2 = \text{PbCl}_2$:

$$\frac{g\text{Cl}_2}{g\text{PbCl}_2} = \frac{M.\text{wt Cl}_2}{M.\text{wt PbCl}_2} \times \frac{1 \text{ mole Cl}_2}{1 \text{ mole PbCl}_2}$$

$$\% \text{ substance A} = \frac{\text{G.F} * \text{wt.of substance B}}{\text{wt.of sample}} \times 100$$

The following some some common examples of the gravimetric factor

<u>sought sub.</u>	<u>weighted ppt.</u>	<u>G.F.</u>
SO_4^{-2}	BaSO_4	$\frac{\text{Mwt. SO}_4}{\text{Mwt. BaSO}_4}$
Fe	Fe_2O_3	$\frac{2 \text{Mwt. Fe}}{\text{Mwt. Fe}_2\text{O}_3}$
CO_3^{-2}	CaCO_3	$\frac{\text{Mwt. CO}_3}{\text{Mwt. CaCO}_3}$
P	$\text{Mg}_2\text{P}_2\text{O}_7$	$\frac{2 \text{Mwt. P}}{\text{Mwt. Mg}_2\text{P}_2\text{O}_7}$

Example 2: The phosphate in a 0.68 gm mineral sample was precipitated as MgNH_4PO_4 . This yield 0.435 gm of $\text{Mg}_2\text{P}_2\text{O}_7$ by ignition, Calculate the percentage of P in the sample?

Solution:

$$\% \text{P} = \frac{\text{wt. of P}}{\text{wt. of sample}} * 100$$

$$\text{wt. of P} = \text{wt. of Mg}_2\text{P}_2\text{O}_7 * \text{G.F.} \quad \left(\frac{2 \text{Mwt. P}}{\text{Mg}_2\text{P}_2\text{O}_7} \right)$$

$$= 0.435 * \frac{2 * 30.9}{222.4}$$

$$= 0.1209 \text{ gm}$$

$$\% \text{P} = \frac{0.1209 \text{ gm}}{0.68 \text{ gm}} * 100 = 17.8\%$$

Example 18 1.5 gm sample contain Cl^- . If we added AgNO_3 to solution produced precipitate from silver chloride weighted 0.9214 gm. compute percentage of chloride in the sample?

Solution:

$$G.F = \frac{\text{Mwt. } \text{Cl}^-}{\text{Mwt. AgCl}}$$

$$\text{wt. of } \text{Cl}^- = \text{wt. of AgCl} \times G.F$$

$$= 0.9214 \times \frac{35.5}{143.4} = 0.2282 \text{ gm } \text{Cl}^-$$

$$\% \text{ Cl} = \frac{0.2282 \text{ gm}}{1.5 \text{ gm}} \times 100 = \underline{\underline{15.2\%}}$$