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## Lecture 1-04/05/2020

## Pavement Structural Design

## Introduction

Pavement Design (Highway and Airport):- Involves a study of soils and paving materials, their behaviour under load and the design of pavement to carry that load under all climatic conditions.

## Pavement Structure $\boldsymbol{=}$ Subgrade $\boldsymbol{+}$ Subbase $\boldsymbol{+}$ Base $\boldsymbol{+}$ Surfacing

The purpose of the pavement system is to provide a smooth surface over which vehicles may safely pass under all climatic conditions for the specific performance period of the pavement.

## Pavement Types:-

1) Flexible Pavement (Asphalt Pavement)

الثبليط المرن او التبليط الاسفلتي
The flexible pavement is a multi-layered system has different materials in different layers (better materials on the top and cannot be represented by a homogeneous mass). Multi-layer system consist of:-



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2) Rigid Pavement (Concrete Pavement- Slab)


## 3) Composite Pavement

a- Flexible over rigid.

b- Rigid over flexible.


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4) Block Pavement



NOTES

1. PAVERS MUST ALWAYS BE LAID ACROSS THE TRAFFIC FLOW.
2. PAVERS ARE NOT TO BE LAID IN THE "STACL BOND" PATTERN because the pavers don't LOCK OR BOND TOGETHER.
3. IT IS RECOMMENDED THAT PAVERS BE LAID IN A HERRINGBONE PATTERN.

## Wheel loads and Axle Loads:

|  | Front axle | Single axle with single tire at each end |  |
| :--- | :--- | :--- | :--- |
|  |  |  | Single axle with dual tire at each end |
|  |  |  |  |

## Wheel configuration and distribution of axle load



The load (from a vehicle) is transferred to the pavement through loadbearing axles and pressurized tires. The resulting pressure or stress on the pavement, at any depth, is dependent on many factors, such as total load, the number of axles and tires, and the condition of the tires.

The stress on the surface of the pavement gets distributed in an inverted V form the surface downward. In other words, the stress intensity decreases along the depth of the pavement.


## Tire Pressure, contact Pressure and the Imprint:-



Contact Pressure $(\mathrm{P})=$ Load on wheel $\backslash$ Contact area

## Calculate Contact Area

1) Elliptical Tire Contact Area


Contact area = area of ellipse $A=\pi^{*} a^{*} b$
2) Circular Shape: most conmen assumptions for contact area ( $b=a$ )

Contact Area $=\pi \mathrm{a}^{2}$
3) Rectangular Contact area with semi-circular ends

$$
\mathrm{A}=0.4 \mathrm{~L} * 0.6 \mathrm{~L}+\pi(0.3 \mathrm{~L})^{2}
$$

$$
\mathrm{A}=0.52274 \mathrm{~L}^{2}
$$

PSI = Pound per Square inch


Example :- Wheel load 40 kips and tire pressure $=150$ psi. Calculate contact area and "L"?.

## Pavement Distresses (Failure)

## 1) Structural Distress (Structural Failure):-

A collapse of pavement structure or a breakdown of one or more pavement components of such magnitude to make pavement incapable sustaining the loads imposed upon it's surface which needs then complete rebuilding.

## 2) Functional Distress (Functional Failure):-

Is a distress such that the pavement will not carry out it intended function without causing discomfort to passenger or vehicle due to it's roughness.

## Causes of Pavement Distresses

## 1) Over Load

a. Excessive loads (excessive axle load).
b. High number of reputations of axle loads.
c. High tire pressure.

## 2) Climatic and Environmental Conditions

a. Frost heaving (frost action)
b. Volume change of soil due wetting and drying breakup resulting from freezing and thawing or improper drainage.

## 3) Disintegration the paving materials

The rate at which a patch deteriorates is influenced by compaction, materials selection, and the quality of the surrounding or underlying pavement. Disintegration is the breakup of a pavement into small pieces that are lost with time and traffic. Ravelling and potholes are the most common types of disintegration.
4) Use dirty aggregate or insufficient during constriction.

## 5) Lack of maintenance

## 6) Inadequate structured design

## Comparison between Flexible \& Rigid Pavements

| Flexible Pavement | Rigid Pavement |
| :--- | :--- |
| Flexible pavement consists of a series of <br> layers with the highest quality at or near <br> the surface. | Rigid pavement consists of a Portland cement <br> concrete slabs resting either directly on subgrade <br> or on base course. |
| Surface |  |

## Lecture 2-11/05/2020

## Layers Function

## Subgrade (Prepared Road Bed)

The subgrade is usually the natural material located along the horizontal alignment of the pavement and serves as the foundation of the pavement structure. It also may consist of a layer of selected borrow materials, well compacted to prescribed specifications. It may be necessary to treat the subgrade material to achieve certain strength properties required for the type of pavement being constructed.

## Required number of passes for rolling compactors in soil compaction

- Compactor speed is generally in range of $6-12 \mathrm{~km} / \mathrm{hr}$.
- Heavy compactor requires less number of passes
- Light compactor is about 20 Ton, (For about 15 cm thickness)
- High capacity compactor is about 40-50 Ton, (For about 30 cm thickness)


## Compactor speed $(\mathrm{m} / \mathrm{s})=1.065+0.033(\%$ W.C. $)+0.084($ N.P. $)$

Where:
W.C. : Water content \& N.P. : Number of passes

Ex: Compactor speed is $7.2 \mathrm{~km} / \mathrm{hr}$, W.C. is $12 \%$, what is the required number of passes?

## Answer:

$7.2 \mathrm{~km} / \mathrm{hr}=2 \mathrm{~m} / \mathrm{s}$
$2=1.065+0.033(12)+0.084$ (N.P.)
N.P. $=6.4$ that should $\mathrm{be}=7$ passes

## Subbase Course

Located immediately above the subgrade, the subbase component consists of material of a superior quality which is generally used for subgrade construction. The requirements for subbase materials usually are given in terms of the gradation and strength. In some cases, the subbase may be treated with Portland cement, asphalt, lime, flyash, or combinations of these admixtures to increase its strength and stiffness. A subbase layer is not always included, especially with rigid pavements. A subbase layer is typically included when the subgrade soils are of very poor quality and/or suitable material for the base layer is not available locally, and is, therefore, expensive. This process of treating soils to improve their engineering properties is known as stabilization.

## Base Course

The base is a layer or layers of specified or select material of designed thickness placed on a subbase or subgrade (if a subbase is not used) to provide a uniform and stable support for binder and surface courses. The base layer typically provides a significant portion of the structural capacity in a flexible pavement system and improves the foundation stiffness for rigid pavements. This course usually consists of granular materials such as crushed stone, crushed or uncrushed gravel, and sand. The specifications for base course materials usually include more strict requirements than those for subbase materials, particularly with respect to their gradation, and strength. Materials that do not have the required properties can be used as base materials if they are properly stabilized with Portland cement, asphalt, or lime.

## Surface course

The surface course is one or more layers of a pavement structure designed to accommodate the traffic load, the top layer of which resists skidding, traffic abrasion, and the disintegrating effects of climate. The surface layer may consist of asphalt (also called bituminous) concrete,
resulting in "flexible" pavement, or Portland cement concrete (PCC), resulting in "rigid" pavement. It was shown that the quality of the surface course of a flexible pavement depends on the mix design of the asphalt concrete used.

## Properties of Highway Materials:

## Soil Characteristics

The distribution of particle size in soils can be determined by conducting a sieve analysis (sometimes known as mechanical analysis) on a soil sample if the particles are sufficiently large. This is done by shaking a sample of air-dried soil through a set of sieves with progressively smaller openings. The smallest practical opening of these sieves is 0.075 mm ; this sieve is designated No. 200. Other sieves include:

No. 140 ( 0.106 mm ), No. 100 ( 0.15 mm ), No. 60 ( 0.25 mm ), No. 40 ( 0.425 mm ), No. $20(0.85 \mathrm{~mm})$, No. $10(2.0 \mathrm{~mm})$, No. $4(4.75 \mathrm{~mm})$.

Gravel: > 2 mm
$\square$ Sand size: 2.0-0.06 mm
$\square$ Silt: 0.06-0.002
Clay: less than 0.002
For soils containing particle sizes smaller than the lower limit, the hydrometer analysis is used.

## Atterberg Limits

Clay soils with very low moisture content will be in the form of solids. As the water content increases, however, the solid soil gradually becomes plastic-that is, the soil easily can be molded into different shapes without breaking up. Continuous increase of the water content will eventually bring the soil to a state where it can flow as a viscous liquid. The stiffness or
consistency of the soil at any time therefore depends on the state at which the soil is, which in turn depends on the amount of water present in the soil.

The water content levels at which the soil changes from one state to the other is the Atterberg limits. They are the shrinkage limit (SL), plastic limit (PL), and liquid limit (LL), as illustrated in Figure below. Atterberg limits are important limits of engineering behaviour, because they facilitate the comparison of the water content of the soil with those at which the soil changes from one state to another. They are used in the classification of fine-grained soils and are extremely useful, since they correlate with the engineering behaviours of such soils.

## Shrinkage Limit (SL)

When a saturated soil is slowly dried, the volume shrinks, but the soil continues to contain moisture. Continuous drying of the soil, however, will lead to moisture content at which further drying will not result in additional shrinkage. The volume of the soil will stay constant, and further drying will be accompanied by air entering the voids. The moisture content at which this occurs is the shrinkage limit, or SL, of the soil.

## Plastic Limit (PL)

The plastic limit, or PL, is defined as the moisture content at which the soil crumbles when it is rolled down to a diameter of one-eighth of an inch. The moisture content is higher than the PL if the soil can be rolled down to diameters less than one-eighth of an inch, and the moisture content is lower than the PL if the soil crumbles before it can be rolled to one-eighth of an inch diameter.

## Liquid Limit (LL)

The liquid limit, or LL, is defined as the moisture content at which the soil will flow and close a groove of one-half inch within it after the standard LL equipment has been dropped 25 times. The equipment used for LL determination is shown in Figure below.


This device was developed by Casagrande, who worked to standardize the Atterberg limits tests. It is difficult in practice to obtain the exact moisture content at which the groove will close at exactly 25 blows. The test is therefore conducted for different moisture contents and the number of blows required to close the groove for each moisture content recorded. A graph of moisture content versus the logarithm of the number of blows (usually a straight line
known as the flow curve) is then drawn. The moisture content at which the flow curve crosses 25 blows is the LL.

The range of moisture content over which the soil is in the plastic state is the difference between the LL and the PL and is known as the plasticity index (PI).

$$
\mathrm{PI}=\mathrm{LL}-\mathrm{PL}
$$

where
PI $=$ plasticity index
$\mathrm{LL}=$ liquid limit
PL = plastic limit

## Classification of Soils for Highway Use

The most commonly used classification system for highway purposes is

- The American Association of State Highway and Transportation Officials (AASHTO) Classification System.
- The Unified Soil Classification System (USCS)


## AASHTO Soil Classification System

The system has been described by AASHTO as a means for determining the relative quality of soils for use in embankments, subgrades, subbases, and bases. Soils are classified into seven groups, A-1 through A-7, with several subgroups, as shown in Table 17.1. The classification of a given soil is based on its particle size distribution, LL, and PI. Soils are evaluated within each group by using an empirical formula to determine the group index (GI) of the soils, given as

$$
\begin{equation*}
\mathrm{GI}=(F-35)[0.2+0.005(\mathrm{LL}-40)]+0.01(F-15)(\mathrm{PI}-10) \tag{17.18}
\end{equation*}
$$

where
GI = group index
$F=$ percent of soil particles passing 0.075 mm (No. 200) sieve in whole number based on material passing 75 mm ( 3 in .) sieve
$\mathrm{LL}=$ liquid limit expressed in whole number
$P I=$ plasticity index expressed in whole number
The GI is determined to the nearest whole number. A value of zero should be recorded when a negative value is obtained for the GI. Also, in determining the GI for A-2-6 and A-2-7 subgroups, the LL part of Eq. 17.18 is not used-that is, only the second term of the equation is used.

Under the AASHTO system, granular soils fall into classes A-1 to A-3. A-1 soils consist of well-graded granular materials, A-2 soils contain significant amounts of silts and clays, and A-3 soils are clean but poorly graded sands.

Classifying soils under the AASHTO system will consist of first determining the particle size distribution and Atterberg limits of the soil and then reading Table 17.1 from left to right to find the correct group. The correct group is the first one from the left that fits the particle size distribution and Atterberg limits and should be expressed in terms of group designation and the GI. Examples are A-2-6(4) and A-6(10).

In general, the suitability of a soil deposit for use in highway construction can be summarized as follows.

1. Soils classified as A-1-a, A-1-b, A-2-4, A-2-5, and A-3 can be used satisfactorily as subgrade or subbase material if properly drained. In addition, such soils must be properly compacted and covered with an adequate thickness of pavement (base and/or surface cover) for the surface load to be carried.
2. Materials classified as A-2-6, A-2-7, A-4, A-5, A-6, A-7-5, and A-7-6 will require a layer of subbase material if used as subgrade.
3. When soils are properly drained and compacted, their value as subgrade material decreases as the GI increases. For example, a soil with a GI of zero (an indication of a good subgrade material) will be better as a subgrade material than one with a GI of 20 (an indication of a poor subgrade material).

| Group Index (GI) | Subgrade Rating <br> 0 |
| :--- | :--- |
| $0-1$ | Excellent |
| $2-4$ | Good |
| $5-9$ | Foir |
| $10-20$ | Very poor |

Note (1): Plasticity index of A-7-5 subgroup is equal to or less than the LL - 30. Plasticity index of A-7-6 subgroup is greater than LL - 30

| General Classification | Granular Materials ( $35 \%$ or less passing the 0.075 mm sieve) |  |  |  |  |  |  | Silt-Clay Materials (>35\% passing the 0.075 mm sieve) |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Group Classification | A-1 |  | A-3 | A-2 |  |  |  | A-4 | A-5 | A-6 | A-7 |
|  | A-1-a | A-1-b |  | A-2-4 | A-2-5 | A-2-6 | A-2-7 |  |  |  | A-7-5 A-7-6 |
| Sieve Analysis, \% passing |  |  |  |  |  |  |  |  |  |  |  |
| 2.00 mm (No. 10) | 50 max | ... | ... | ... | ... | ... | ... | ... | ... | ... | ... |
| 0.425 (No. 40) | 30 max | 50 max | 51 min | ... | ... | $\ldots$ | ... | ... | ... | ... | ... |
| 0.075 (No. 200) | 15 max | 25 max | 10 max | $\begin{aligned} & 35 \\ & \max \end{aligned}$ | $\begin{aligned} & 35 \\ & \max \end{aligned}$ | $\begin{aligned} & 35 \\ & \max \end{aligned}$ | 35 <br> max | 36 min | 36 min | 36 min | 36 min |
| Characteristics of fraction passing 0.425 mm (No. 40) |  |  |  |  |  |  |  |  |  |  |  |
| Liquid Limit | ... |  | $\ldots$ | $\begin{array}{\|l\|} 40 \\ \max \end{array}$ | $\begin{array}{\|l\|} \hline 41 \\ \mathrm{~min} \end{array}$ | $\begin{aligned} & 40 \\ & \max \end{aligned}$ | 41 min | 40 max | 41 min | 40 max | 41 min |
| Plasticity Index | 6 max |  | N.P. | $\begin{array}{\|l\|l\|} 10 \\ \max \end{array}$ | $\begin{aligned} & 10 \\ & \max \end{aligned}$ | $\begin{aligned} & 11 \\ & \min \end{aligned}$ | $\begin{aligned} & 11 \\ & \text { min } \end{aligned}$ | 10 max | 10 max | 11 min | $11 \mathrm{~min}^{1}$ |
| Usual types of significant constituent materials | stone fragments, gravel and sand |  | fine sand | silty or clayey gravel and sand |  |  |  | silty soils |  | clayey soils |  |
| General rating as a subgrade | excellent to good |  |  |  |  |  |  | fair to poor |  |  |  |



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Example 17.3 Classifying a Soil Sample Using the AASHTO Method
The following data were obtained for a soil sample.

| Mechanical Analysis |  |  |
| :---: | :---: | :---: |
| Sieve No. | Percent Finer | Plasticity Tests: |
| 4 | 97 | LL $=48 \%$ |
| 10 | 93 | PL $=26 \%$ |
| 40 | 88 |  |
| 100 | 78 |  |
| 200 | 70 |  |

Using the AASHTO method for classifying soils, determine the classification of the soil and state whether this material is suitable in its natural state for use as a subbase material.

## Lecture 3-18/05/2020

## Special Tests for Pavement Design

## 1- California Bearing Ratio (CBR) Test

This test is commonly known as the CBR test and involves the determination of the loaddeformation curve of the soil in the laboratory using the standard CBR testing. The test is conducted on samples of soil compacted to required standards and immersed in water for four days, during which time the samples are loaded with a surcharge that simulate the estimated weight of pavement material the soil will support. The objective of the test is to determine the relative strength of a soil with respect to crushed rock, which is considered an excellent coarse base material. This is obtained by conducting a penetration test on the samples still carrying the simulated load and using a standard CBR equipment. The CBR is defined as the penetration resistance of a subgrade soil relative to a standard crushed rock.

( unit load for 0.1 piston penetration in test

$$
\begin{gather*}
\mathrm{CBR}=\frac{\text { specimen })\left(\mathrm{lb} / \mathrm{in}^{2} .\right)}{\text { (unit load for } 0.1 \text { piston penetration in standard }}  \tag{17.24}\\
\text { crushed rock })\left(\mathrm{lb} / \mathrm{in}^{2} .\right)
\end{gather*}
$$

The unit load for 0.1 piston in standard crushed rock is usually taken as $1000 \mathrm{lb} / \mathrm{in}^{2}$, which gives the CBR as

$$
\begin{equation*}
\mathrm{CBR}=\frac{\text { (unit load for } 0.1 \text { piston penetration in test sample) }}{1000} \times 100 \tag{17.25}
\end{equation*}
$$

Load a piston $\left(\right.$ area $\left.=3 \mathrm{in}^{2}\right)$ at a constant rate $(0.05 \mathrm{in} / \mathrm{min})$

- Record Load every 0.1 in penetration
- Total penetration not to exceed 0.5 in .
- Draw Load-Penetration Curve.

flun Animation


## CBR Curves



## CBR Calculation

$$
C B R=100\left(\frac{\text { Load or Stress of Soil }}{\text { Load or Stress of Standard Rocks }}\right)
$$

## Loads and Stresses Corresponding to 0.1 and 0.2 inches Penetration for the Standard Rocks

| Penetration | 0.1 " (2.5 mm) | 0. '" $^{\prime \prime}(5.0 \mathrm{~mm})$ |
| :--- | :---: | :---: |
| Load of Standard Rocks (lb) | 3000 | 4500 |
| Load of Standard Rocks (kN) | 13.24 | 19.96 |
| Stress of Standard Rocks (KPa) | 6895 | 10342 |
| Stress of Standard Rocks (psi) | 1000 | 1500 |

Calculate CBR at $0.1 \mathrm{in}(2.5 \mathrm{~mm})$ and 0.2 in $(5.0 \mathrm{~mm})$ deformation then use the Maximum value as the design CBR.

## 2- Resistance Value (R-Value) ASTM D2844

The Resistance Value (R-value) is a test value, which measures the ability of a soil to resist lateral flow due to vertically applied load. This test is developed by California Division of Highways in 1940.

At the completion of the expansion test, the specimen is put into a flexible sleeve and placed in the stabilometer as shown in the figure. Vertical pressure is applied gradually on the specimen at a speed of $0.05 \mathrm{in} / \mathrm{min}$ until a pressure of $160 \mathrm{lb} / \mathrm{in}^{2}$ is attained. The corresponding horizontal pressure is immediately recorded.

$$
\begin{equation*}
R=100-\frac{100}{\frac{2.5}{D}\left(\frac{P_{v}}{P_{h}}-1\right)+1} \tag{17.26}
\end{equation*}
$$

where
$R=$ resistance value
$P_{v}=$ vertical pressure ( $160 \mathrm{lb} / \mathrm{in} .^{2}$ )
$P_{h}=$ horizontal pressure at $P_{v}$ of $160 \mathrm{lb} / \mathrm{in} .^{2}\left(\mathrm{lb} / \mathrm{in} .{ }^{2}\right)$

$D=$ number of turns of displacement pump

## 3- Resilient Modulus (MR)

The Resilient Modulus (MR) is a measure of subgrade material stiffness. A material's resilient modulus is actually an estimate of its modulus of elasticity (E). While the modulus of elasticity is stress divided by strain for a slowly applied load, resilient modulus is stress divided by strain for rapidly applied loads - like those experienced by pavements. MR is ability of material to absorb energy within the elastic range. Resilient modulus is determined using the triaxial test. The test applies a repeated axial cyclic stress of fixed magnitude, load duration and cycle duration to a cylindrical test specimen. While the specimen is subjected to this dynamic cyclic stress, it is also subjected to a static confining stress provided by a triaxial pressure chamber. It is essentially a cyclic version of a triaxial compression test; the cyclic load application is thought to more accurately simulate actual traffic loading.

Resilient modulus test can be conducted on all types of pavement materials ranging from cohesive to stabilized materials. The test is conducted in a triaxial device equipped for repetitive load conditions.

- Measures "stiffness" of the material under repeated load.
- Determines the load carrying capacity of the material.
- Used for HMA as well as unbound materials.
- Uses a repeated load triaxial test.
- Used in most modern methods of pavement design.


Figure 27:2: Recoverable strain under repeated loads

$$
M_{R}=\frac{\text { Deviator stress }}{\text { Recoverable strain }}=\frac{\sigma_{1}-\sigma_{3}}{\varepsilon_{r}}
$$


$M_{R}=1500(C B R) \quad$ Fine-grained materials with soaked CBR $\leq 8$
$M_{R}=1000+555(\mathrm{R}$ Value)
Origin: 1993 AASHTO Guide
Limitation: Fine-grained non-expansive soils with $\mathrm{R} \leq 20$
$\mathrm{R}-$ Value $=\frac{1500(C B R)-1155}{555}$
Origin: HDOT
Limitation: Fine-grained non-expansive soils with soaked CBR $\leq 8$

Elastic modulus is sometimes called Young's modulus, an elastic modulus (E) can be determined for any solid material and represents a constant ratio of stress and strain (a stiffness): $\mathrm{E}=$ stress/ strain

A material is elastic if it is able to return to its original shape or size immediately after being stretched or squeezed. The modulus of elasticity for a material is basically the slope of its stress-strain plot within the elastic range as shown in Figure:


## 4- Plate Loading Test



- Measure supporting power of subgrades, subases, bases and a complete pavement.
- Field test.
- Data from the test are applicable for design of both flexible and rigid pavements.
- Results might need some corrections.
- The test site is prepared and loose material is removed so that the 75 cm diameter plate rests horizontally in full contact with the soil sub-grade. The plate is seated accurately and then a seating load equivalent to a pressure of $0.07 \mathrm{~kg} / \mathrm{cm}^{2}$ ( 320 kg for 75 cm diameter plate) is applied and released after a few seconds. The settlement dial gauge is now set corresponding to zero load.
- A load is applied by means of jack, sufficient to cause an average settlement of about 0.25 cm . When there is no noticeable increase in settlement or when the rate of settlement is less than 0.025 mm per minute (in the case of soils with high moisture content or in clayey soils) the load dial reading and the settlement dial readings are noted.
- Deflection of the plate is measured by means of deflection dials; placed usually at onethird points of the plate near its outer edge.
- To minimize bending, a series of loaded plates should be used.
- Average of three or four settlement dial readings is taken as the settlement of the plate corresponding to the applied load. Load is then increased till the average settlement increase to a further amount of about 0.25 mm , and the load and average settlement readings are noted as before.

'Required for rigid pavement design.

$$
\mathrm{K}=\frac{\mathrm{P}}{\Delta}
$$

$K=$ modulus of subgrade reaction $\mathbf{P}=$ unit load on the plate (stress) (psi)
$\Delta=$ deflection of the plate (in)


Deformation, in

- For design use stress $P=10$ psi $\left(68.95 \mathrm{kN} / \mathrm{m}^{2}\right)$

The 1993 AASHTO Guide offers the following relationship between k-values from a plate bearing test and resilient modulus (MR):

$$
K=M R / 19.4
$$

## Serviceability

It is the ability of pavement at time to serve high speed and high traffic volume. To quantify pavement performance, a concept known as the serviceability performance was developed. Under this concept, a procedure was developed to determine the Present Serviceability Index (PSI) of the pavement, based on its roughness and distress, which were measured in terms of extent of cracking, patching, and rut depth for flexible pavements. The scale PSI ranges from 0 to 5 , where 0 is the lowest PSI and 5 is the highest.

Two serviceability indices are used in the design procedure:

The Initial Serviceability Index ( $\mathbf{p}_{\mathbf{i}}$ ), which is the serviceability index immediately after the construction of the pavement; and the Terminal Serviceability Index $\left(\mathbf{p}_{\mathbf{t}}\right)$, which is the minimum acceptable value before resurfacing or reconstruction is necessary. Recommended values for the terminal serviceability index are 2.5 or 3.0 for major highways and 2.0 for highways with a lower classification.

1) Express ways, Major highways $\mathrm{P}_{\mathrm{t}}=3.0$
2) Primary Roads $\mathrm{Pt}_{\mathrm{t}}=2.5$
3) Secondary Roads $\mathrm{P}_{\mathrm{t}}=2.0$



## For Flexible Pavement

$$
P S I=5.03-1.91 \log _{10}(1+S V)-1.38 \times R D^{2}-0.01(C+P)^{0.5}+\text { error }
$$

## Where:-

SV: Slope variance
RD: Rut depth (inch)
C \& P: Cracking \& Patching area $\mathrm{ft}^{2} / 1000 \mathrm{ft}^{2}$ of pavement area

## For Rigid Pavement

$$
P S I=5.41-1.80 \log _{10}(1+S V)-0.09(C+P)^{0.5}+\text { error }
$$



Ex: Calculate the PSI of a flexible pavement on a section of a highway with the following field data:

Mean slope variance $=4.2$ in .
Mean rut depth $=0.35$ in.
Cracking of 80 ft per $1000 \mathrm{ft}^{2}$

## Answer:

$$
\begin{aligned}
& \mathrm{PSI}=5.03-1.91 \log _{10}(1+\mathrm{SV})-1.38 \times \mathrm{RD}^{2}-0.01(\mathrm{C}+\mathrm{P})^{0.5} \\
& \mathrm{PSI}=5.03-1.368-0.169-0.089 \\
& \mathrm{PSI}=\mathbf{3 . 4 0 4}
\end{aligned}
$$

## Lecture 4-01/06/2020

## Traffic Loads

Pavement structural design requires a quantification of all expected loads that pavements will encounter over its design life. This quantification is usually done using Equivalent Single

Axle Loads (ESALs). This converts wheel loads of various magnitudes and repetitions (mixed traffic) to an equivalent number of "standard" or "equivalent" loads.

## ESAL

The traffic load is determined in terms of the number of repetitions of an 18,000-lb (80 kilo newton ( kN )) single-axle load applied to the pavement on two sets of dual tires. This is usually referred to as the equivalent single-axle load (ESAL). The dual tires are represented as two circular plates, each 4.51 in . radius, spaced 13.57 in . apart. This representation corresponds to a contact pressure of $70 \mathrm{lb} / \mathrm{in}^{2}$.


To determine the ESAL, the number of different types of vehicles such as cars, buses, singleunit trucks, and multiple-unit trucks expected to use the facility during its lifetime must be known. The distribution of the different types of vehicles expected to use the proposed highway can be obtained from results of classification counts that are taken by state highway
agencies at regular intervals. These can then be converted to equivalent $18,000-\mathrm{lb}$ loads using the equivalency factors.

Flexible highway pavements are usually designed for a 20 -year period. Since traffic volume does not remain constant over the design period of the pavement, it is essential that the rate of growth be determined and applied when calculating the total ESAL. Annual growth rates can be obtained based on traffic volume counts over several years. The overall growth rate in the United States is between 3 and $5 \%$ per year, although growth rates of up to $10 \%$ per year have been suggested for some interstate highways. The growth factors $\left(\mathrm{G}_{\mathrm{rn}}\right)$ for different growth rates and design periods can be obtained from the Equation below:


Where : $g=i / 100, \quad i=$ growth rate,$\quad n=$ design life, years
OR $G_{r n}$ can be obtained using the table below:

| Analysis Period Years ( $n$ ) | Annual Growth Rate, Percent (g) |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | No Growth | 2 | 4 | 5 | 6 | 7 | 8 | 10 |
| 1 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| 2 | 2.0 | 2.02 | 2.04 | 2.05 | 2.06 | 2.07 | 2.08 | 2.10 |
| 3 | 3.0 | 3.06 | 3.12 | 3.15 | 3.18 | 3.21 | 3.25 | 3.31 |
| 4 | 4.0 | 4.12 | 4.25 | 4.31 | 4.37 | 4.44 | 4.51 | 4.64 |
| 5 | 5.0 | 5.20 | 5.42 | 5.53 | 5.64 | 5.75 | 5.87 | 6.11 |
| 6 | 6.0 | 6.31 | 6.63 | 6.80 | 6.98 | 7.15 | 7.34 | 7.72 |
| 7 | 7.0 | 7.43 | 7.90 | 8.14 | 8.39 | 8.65 | 8.92 | 9.49 |
| 8 | 8.0 | 8.58 | 9.21 | 9.55 | 9.90 | 10.26 | 10.64 | 11.44 |
| 9 | 9.0 | 9.75 | 10.58 | 11.03 | 11.49 | 11.98 | 12.49 | 13.58 |
| 10 | 10.0 | 10.95 | 12.01 | 12.58 | 13.18 | 13.82 | 14.49 | 15.94 |
| 11 | 11.0 | 12.17 | 13.49 | 14.21 | 14.97 | 15.78 | 16.65 | 18.53 |
| 12 | 12.0 | 13.41 | 15.03 | 15.92 | 16.87 | 17.89 | 18.98 | 21.38 |
| 13 | 13.0 | 14.68 | 16.63 | 17.71 | 18.88 | 20.14 | 21.60 | 24.52 |
| 14 | 14.0 | 15.97 | 18.29 | 19.16 | 21.01 | 22.55 | 24.21 | 27.97 |
| 15 | 15.0 | 17.29 | 20.02 | 21.58 | 23.28 | 25.13 | 27.15 | 31.77 |
| 16 | 16.0 | 18.64 | 21.82 | 23.66 | 25.67 | 27.89 | 30.32 | 35.95 |
| 17 | 17.0 | 20.01 | 23.70 | 25.84 | 28.21 | 30.84 | 33.75 | 40.55 |
| 18 | 18.0 | 21.41 | 25.65 | 28.13 | 30.91 | 34.00 | 37.45 | 45.60 |
| 19 | 19.0 | 22.84 | 27.67 | 30.54 | 33.76 | 37.38 | 41.45 | 51.16 |
| 20 | 20.0 | 24.30 | 29.78 | 33.06 | 36.79 | 41.00 | 45.76 | 57.28 |
| 25 | 25.0 | 32.03 | 41.65 | 47.73 | 54.86 | 63.25 | 73.11 | 98.35 |
| 30 | 30.0 | 40.57 | 56.08 | 66.44 | 79.06 | 94.46 | 113.28 | 164.49 |
| 35 | 35.0 | 49.99 | 73.65 | 90.32 | 111.43 | 138.24 | 172.32 | 271.02 |

A general equation for the accumulated ESAL for each category of axle load is obtained as:

$$
E S A L_{i}=f_{d} \times G_{r n} \times A A D T_{i} \times 365 \times N_{i} \times F_{E i}
$$

Where:
$E S A L_{i}=$ equivalent accumulated $18000 \mathrm{Ib}(80 \mathrm{KN})$ single axle load for the axle category i
$f_{d}=$ lane distribution factor (Table 8-6)
$G_{r n}=$ growth factor for a given growth rate and design period n
$A A D T_{i}=$ first year annual average daily traffic for axle category i
$N_{i}=$ number of axles on each vehicle in category i
$F_{E i}=$ load equivalency factor for axle category i

TABLE 8.6 Lane Distribution Factor (AASHTO, 1993)

| No. of Lanes in <br> Each Direction | \% of 18 -kip ESAL in <br> the Design Lane |
| :--- | :--- |
| 1 | 100 |
| 2 | $80-100$ |
| 3 | $60-80$ |
| 4 | $50-70$ |

## Example:

Calculate the Accumulated Equivalent Single-Axle Load for a Proposed Eight-Lane Highway Using Load Equivalency Factors. An eight-lane divided highway is to be constructed on a new alignment. Traffic volume forecasts indicate that the average annual daily traffic (AADT) in both directions during the first year of operation will be 12,000 with the following vehicle mix and axle loads.

Passenger cars (2000 lb/axle) 50\%

2-axle single-unit trucks ( $6000 \mathrm{lb} / \mathrm{axle}$ ) $33 \%$
3 -axle single-unit trucks ( $10,000 \mathrm{lb} / \mathrm{axle}$ ) $17 \%$
The vehicle mix is expected to remain the same throughout the design life of the pavement. If the expected annual traffic growth rate is $4 \%$ for all vehicles, determine the design ESAL, given a design period of 20 years. The pavement has a terminal serviceability index $\left(\mathrm{p}_{\mathrm{t}}\right)$ of 2.5 and Structural Number (SN) of 5.

## Answer:

ESAL $=f_{d} \times G_{r n} \times A A D T \times 365 \times N_{i} \times \mathrm{FE}_{i}$

## ESAL for Passenger cars:

$\mathrm{f}_{\mathrm{d}}=0.6, \quad \mathrm{Grn}=29.78, \quad \mathrm{AADT}=1200 \times 0.5=6000, \quad \mathrm{~N}_{\mathrm{i}}=2, \quad \mathrm{FE}_{\mathrm{i}}=0.0002$
ESAL for Passenger cars $=0.6 \times 29.78 \times 6000 \times 365 \times 2 \times 0.0002=15653$

## ESAL for 2-axle single-unit trucks:

$\mathrm{f}_{\mathrm{d}}=0.6, \quad \mathrm{Grn}=29.78, \quad \mathrm{AADT}=1200 \times 0.33=3960, \quad \mathrm{~N}_{\mathrm{i}}=2, \quad \mathrm{FE}_{\mathrm{i}}=0.01$
ESAL for 2-axle single-unit trucks $=0.6 \times 29.78 \times 3960 \times 365 \times 2 \times 0.01=516529$

## ESAL for 3-axle single-unit trucks:

$\mathrm{f}_{\mathrm{d}}=0.6, \quad \mathrm{Grn}=29.78, \quad \mathrm{AADT}=1200 \times 0.17=2040, \quad \mathrm{~N}_{\mathrm{i}}=3, \quad \mathrm{FE}_{\mathrm{i}}=0.088$
ESAL for 2-axle single-unit trucks $=0.6 \times 29.78 \times 2040 \times 365 \times 3 \times 0.088=3512392$
$\mathbf{E S A L}_{\text {Total }}=15653+516529+3512392=4044574=4 \times 10^{6}$

## Lecture 5-08/06/2020

## Flexible Pavement Design:

## 1. AASHTO Design Method

The AASHTO method for design of highway pavements is based primarily on the results of the AASHTO road test that was conducted in Ottawa, USA. It was a cooperative effort carried out under the supports of 49 states, the District of Columbia, Puerto Rico, the Bureau of Public Roads, and several industry groups. Tests were conducted on short-span bridges and test sections of flexible and rigid pavements constructed on A-6 subgrade material. The pavement test sections consisted of two small loops and four larger ones with each being a four-lane divided highway. The tangent sections consisted of a successive set of pavement lengths of different designs, each length being at least 100 feet. The principal of flexible pavement sections were constructed of asphalt mixture surface, a well graded crushed limestone base, and a uniformly graded sand-gravel subbase. Three levels of surface thicknesses ranging from 1 to 6 inches were used in combination with three levels of base thicknesses ranging from 0 to 9 inches. Test traffic consisting of both single-axle and tandemaxle vehicles were then driven over the test sections until several thousand load repetitions had been made. Data were then collected on the pavement condition with respect to extent of cracking and amount of patching required to maintain the section in service. The longitudinal and transverse profiles also were obtained to determine the extent of rutting, surface deflection caused by loaded vehicles moving at very slow speeds. These data then were analyzed thoroughly, and the results formed the basis for the AASHTO method of pavement design.


## Design Considerations

The factors considered in the AASHTO procedure for the design of flexible pavement as presented in the 1993 guide are:

1. Pavement performance
2. Roadbed soils (subgrade material)
3. Materials of construction
4. Environment
5. Drainage
6. Reliability

## 1. Pavement performance

To quantify pavement performance, a concept known as the serviceability performance was developed. Under this concept, a procedure was developed to determine the present serviceability index (PSI) of the pavement, based on its roughness and distress, which were measured in terms of extent of cracking, patching, and rut depth for flexible pavements. The original expression developed gave the PSI as a function of the extent and type of cracking
and patching and the slope variance in the two wheel paths which is a measure of the variations in the longitudinal profile. The scale PSI ranges from 0 to 5 , where 0 is the lowest PSI and 5 is the highest.

## 2. Roadbed Soils (Subgrade Material):

The 1993 AASHTO guide also uses the resilient modulus (Mr) of the soil to define its property. However, the method allows for the conversion of the CBR or R value of the soil to an equivalent Mr value using the following conversion factors:
$\mathrm{Mr}\left(\mathrm{lb} / \mathrm{in}^{2}\right)=1500 \mathrm{CBR} \quad($ for $\mathrm{CBR} \leq 10)$
$\mathrm{Mr}\left(\mathrm{lb} / \mathrm{in}^{2}\right)=1000+555 \mathrm{R}$ value $\quad($ for $\mathrm{R} \leq 20)$

## 3. Materials of construction

A. Subbase Construction Materials: The quality of the material used is determined in terms of the layer coefficient, $a_{3}$, which is used to convert the actual thickness of the subbase to an equivalent SN . The sandy gravel subbase course material used in the AASHTO road test was assigned a value of 0.11 . Layer coefficients are usually assigned, based on the description of the material used. Charts correlating the layer coefficients with different soil engineering properties have been developed. Figure 19.3 shows one such chart for granular subbase materials.

${ }^{2}$ Scale derived from correlations from Illinois.
${ }^{6}$ Scale derived from correlations obtained from The Asphalt Institute, California, New Mexico, and Wyoming.
${ }^{\text {c }}$ Scale derived from correlations obtained from Texas.
${ }^{\text {d }}$ Scale derived on NCHRP project 128, 1972.
Figure (19.3) Variation in Granular Subbase Layer Coefficient, a3, with Various Subbase Strenoth Parameters
B. Base Course Construction Materials: Materials selected should satisfy the general requirements for base course materials. A structural layer coefficient, $\mathrm{a}_{2}$, for the material used also should be determined. This can be done using Figure 19.4.


Figure (19.4) Variation in Granular Base Layer Coefficient, a2, with Various Subbase Strength Parameters
C. Surface Course Construction Materials: The most commonly-used material is a hot plant mix of asphalt cement and dense-graded aggregates with a maximum size of 1 inch . The structural layer coefficient $\left(a_{1}\right)$ for the surface course can be extracted from Figure 19.5, which relates the structural layer coefficient of a dense grade asphalt concrete surface course with its resilient modulus at $68^{\circ} \mathrm{F}\left(20^{\circ} \mathrm{C}\right)$.


Figure (19.5) Chart for Estimating Structural Layer Coefficient of DenseGraded/Asphalt Concrete Based on the Elastic (Resilient) Modulus

## 4. Environment

Temperature and rainfall are the two main environmental factors used in evaluating pavement performance in the AASHTO method. The effects of temperature on asphalt pavements include stresses induced by thermal action, changes in the creep properties, and the effect of freezing and thawing of the subgrade soil. The effect of rainfall is due mainly to the penetration of the surface water into the underlying material. However, this effect is taken into consideration in the design procedure, and the methodology used is presented later under "Drainage."

Test results have shown that the normal modulus (that is, modulus during summer and fall seasons) of materials susceptible to frost action can reduce by 50 percent to 80 percent during the thaw period. Also, resilient modulus of a subgrade material may vary during the year, even when there is no specific thaw period. This occurs in areas subject to very heavy rains during specific periods of the year. It is likely that the strength of the material will be affected during the periods of heavy rains.


Effective Roadbed Soil Resilient Modulus, $M_{r}\left(\mathrm{lb} / \mathrm{in}^{2}\right)=\underline{7250}$ (corresponds to $\left.\bar{u}_{f}\right)$
Figure (19.6) Chart for Estimating Effective Roadbed Soil Resilient Modulus for Flexible Pavements Designed Using the Serviceability Criteria

## 5. Drainage

The effect of drainage on the performance of flexible pavements is considered by modifying the structural layer coefficient. The modification is carried out by incorporating a factor $\mathrm{m}_{\mathrm{i}}$ for the base and subbase layer coefficients ( $a_{2}$ and $a_{3}$ ). The $m_{i}$ factors are based both on the percentage of time during which the pavement structure will be nearly saturated and on the quality of drainage, which is dependent on the time it takes to drain the base layer to 50 percent of saturation.

Table 19.5 Definition of Drainage Quality

| Quality of Drainage | Water Removed Within* |
| :---: | :--- |
| Excellent | 2 hours |
| Good | 1 day |
| Fair | 1 week |
| Poor | 1 month |
| Very poor | (water will not drain) |

*Time required to drain the base layer to $50 \%$ saturation.
SOURCE: Adapted with permission from AASHTO Guide for Design of Pavement Structures, American Association of State Highway and Transportation Officials, Washington, D.C., 1993.

Table 19.6 Recommended $m_{i}$ Values

|  | Percent of Time Pavement Structure Is Exposed to <br> Moisture Levels Approaching Saturation |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
| Quality of | Less |  |  | Greater |
| Drainage | Than $1 \%$ | 1 to $5 \%$ | 5 to $25 \%$ | Than $25 \%$ |
| Excellent | $1.40-1.35$ | $1.35-1.30$ | $1.30-1.20$ | 1.20 |
| Good | $1.35-1.25$ | $1.25-1.15$ | $1.15-1.00$ | 1.00 |
| Fair | $1.25-1.15$ | $1.15-1.05$ | $1.00-0.80$ | 0.80 |
| Poor | $1.15-1.05$ | $1.05-0.80$ | $0.80-0.60$ | 0.60 |
| Very poor | $1.05-0.95$ | $0.95-0.75$ | $0.75-0.40$ | 0.40 |

SOURCE: Adapted with permission from AASHTO Guide for Design of Pavement Structures, American Association of State Highway and Transportation Officials, Washington, D.C., 1993.

## 6. Reliability

It has been noted that the cumulative ESAL is an important input to any pavement design method. However, the determination of this input is usually based on assumed growth rates which may not be accurate. 1993 AASHTO guide proposes the use of a reliability factor that considers the possible uncertainties in traffic prediction and performance prediction. Reliability design levels ( $\mathrm{R} \%$ ), which determine assurance levels that the pavement section designed using the procedure will survive for its design period, have been developed for different types of highways. For example, a 50 percent reliability design level implies a 50 percent chance for successful pavement performance- that is, the probability of design performance success is 50 percent.

Table 19.7 shows suggested reliability levels based on a survey of the AASHTO pavement design task force. Reliability factors, $\mathrm{R} \% \geq 1$, based on the reliability level selected and the overall variation, $\mathrm{So}^{2}$ also have been developed. $\mathrm{So}^{2}$ accounts for the chance variation in the traffic forecast and the chance variation in actual pavement performance for a given design period traffic, W18.

Table 19.7 Suggested Levels of Reliability for Various Functional Classifications

| Recommended Level of Reliability |  |  |
| :--- | :---: | :---: |
| Functional Classification | Urban | Rural |
| Interstate and other freeways | $85-99.9$ | $80-99.9$ |
| Other principal arterials | $80-99$ | $75-95$ |
| Collectors | $80-95$ | $75-95$ |
| Local | $50-80$ | $50-80$ |

Note: Results based on a survey of the AASHTO Pavement Design Task Force.
SOURCE: Adapted with permission from AASHTO Guide for Design of Pavement Structures, American Association of State Highway and Transportation Officials, Washington, D.C., 1993.

The reliability factor $\mathrm{R} \%$ is given as $\log 10 \mathrm{R} \%=-\mathrm{Z}_{\mathrm{R}} *$ So

Where $\mathrm{Z}_{\mathrm{R}}=$ standard normal deviation for a given reliability $(\mathrm{R} \%)$
$\mathrm{Z}_{\mathrm{R}}$ Represents the probability that serviceability will be maintained at adequate levels from a user's point of view throughout the design life of the facility.

So= estimated overall standard deviation

Table 19.8 values of $\mathrm{Z}_{\mathrm{R}}$ for different reliability levels R . Overall standard deviation ranges have been identified for flexible and rigid pavements as

## Standard Deviation, $S_{o}$

Flexible pavements

$$
\begin{aligned}
& 0.40-0.50 \\
& 0.30-0.40
\end{aligned}
$$

Rigid pavements

Table 19.8 Standard Normal Deviation $\left(Z_{R}\right)$ Values Corresponding to Selected Levels of Reliability

| Reliability $(\boldsymbol{R} \%)$ | Standard Normal <br> Deviation, $Z_{R}$ |
| :---: | :---: |
| 50 | -0.000 |
| 60 | -0.253 |
| 70 | -0.524 |
| 75 | -0.674 |
| 80 | -0.841 |
| 85 | -1.037 |
| 90 | -1.282 |
| 91 | -1.340 |
| 92 | -1.405 |
| 93 | -1.476 |
| 94 | -1.555 |
| 95 | -1.645 |
| 96 | -1.751 |
| 97 | -1.881 |
| 98 | -2.054 |
| 99 | -2.327 |
| 99.9 | -3.090 |
| 99.99 | -3.750 |

SOURCE: Adapted with permission from AASHTO Guide for Design of Pavement Structures, American Association of State Highway and Transportation Officials, Washington, D.C., 1993.

## Structural Design

The objective of the design using the AASHTO method is to determine a flexible pavement Structural Number (SN) adequate to carry the projected design ESAL. This design procedure is used for ESALs greater than 50,000 for the performance period. The design for ESALs less than this is usually considered under low volume roads. The 1993 AASHTO guide gives the expression for SN as

$$
\mathrm{SN}=\mathrm{a}_{1} \mathrm{D}_{1}+\mathrm{a}_{2} \mathrm{D}_{2} \mathrm{~m}_{2}+\mathrm{a}_{3} \mathrm{D}_{3} \mathrm{~m}_{3}
$$

where
$\mathrm{m}_{\mathrm{i}}=$ drainage coefficient for layer i
$a_{1}, a_{2}, a_{3}=$ layer coefficients representative of surface, base, and subbase course, respectively
$D_{1}, D_{2}, D_{3}=$ actual thickness in inches of surface, base, and subbase courses, respectively.
The basic design equation given in the 1993 guide is

$$
\begin{align*}
\log _{10} W_{18}= & Z_{R} S_{o}+9.36 \log _{10}(\mathrm{SN}+1)-0.20+\frac{\log _{10}[\Delta \mathrm{PSI} /(4.2-1.5)]}{0.40+\left[1094 /(\mathrm{SN}+1)^{5.19}\right]} \\
& +2.32 \log _{10} M_{r}-8.07 \tag{19.7}
\end{align*}
$$



Table 19.9 AASHTO-Recommended Minimum Thicknesses of Highway Layers

|  | Minimum Thickness (in.) |  |
| :---: | :---: | :---: |
| Traffic, ESALs | Asphalt Concrete | Aggregate Base |
| Less than 50,000 | 1.0 (or surface treatment) | 4 |
| $50,001-150,000$ | 2.0 | 4 |
| $150,001-500,000$ | 2.5 | 4 |
| $500,001-2,000,000$ | 3.0 | 6 |
| $2,000,001-7,000,000$ | 3.5 | 6 |
| Greater than $7,000,000$ | 4.0 | 6 |

## Example

## Designing a Flexible Pavement Using the AASHTO Method

A flexible pavement for an urban interstate highway is to be designed using the 1993 AASHTO guide procedure to carry a design ESAL of $2 * 10^{6}$. It is estimated that it takes about a week for water to be drained from within the pavement and the pavement structure will be exposed to moisture levels approaching saturation for $30 \%$ of the time. The following additional information is available:

Resilient modulus of asphalt concrete at $68^{\circ} \mathrm{F}=450,000 \mathrm{lb} / \mathrm{in}^{2}$
CBR value of base course material $=100, \mathrm{Mr}=31,000 \mathrm{lb} / \mathrm{in}^{2}$
CBR value of subbase course material $=22, \mathrm{Mr}=13,500 \mathrm{lb} / \mathrm{in}^{2}$
CBR value of subgrade material $=6$
Initial serviceability index $p_{i}=4.2$
Terminal serviceability index $p_{t}=2.2$
Determine a suitable pavement structure?


Solution: Since the pavement is to be designed for an interstate highway, the following assumptions are made:

$$
S N=a_{1} D_{1}+a_{2} D_{2} m_{2}+a_{3} D_{3} m_{3}
$$

Reliability level $(\mathbf{R})=\mathbf{9 9 \%}$ (range is 85 to 99.9 from Table 19.7)
Standard deviation $\left(\mathbf{S}_{\mathbf{o}}\right)=\mathbf{0 . 4 9}$ (range is 0.4 to 0.5 )
Initial serviceability index $p_{i}=4.5$
Terminal serviceability index $p_{t}=2.5$
$\mathbf{\Delta P S I}=4.5-2.5=\mathbf{2}$

## 1. To find $D_{1}$ :

$$
\mathrm{SN}_{1}=\mathrm{a}_{1} \mathrm{D}_{1} \quad \Rightarrow \mathrm{D}_{1}=\mathrm{SN}_{1} / \mathrm{a}_{1}
$$

Mr for base course $=31,000 \mathrm{lb} / \mathrm{in}^{2}$ from figure $\mathbf{S N}_{\mathbf{1}}=\mathbf{2 . 6}$


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Subject: Transportation Engineering


Determine the appropriate structure layer coefficient for each construction material:
Resilient value of asphalt $=450,000 \mathrm{lb} / \mathrm{in}^{2}$. From Figure 19.5, $\mathbf{a}_{\mathbf{1}}=\mathbf{0 . 4 4}$


Elastic Modulus, $E_{A C}\left(\mathrm{lb} / \mathrm{in} .^{2}\right.$ ), of Asphalt Concrete (at $68^{\circ} \mathrm{F}$ )
$D_{1}=2.6 / 0.44=5.9$ in $\square$ Use 6 in for the thickness of the surface course
$\mathrm{SN}_{1} *=\mathrm{a}_{1} \times \mathrm{D}_{1}=0.44 \times 6=2.64$

## 2. To find $D_{2}$ :

$\mathrm{SN}_{2}=\mathrm{a}_{1} \mathrm{D}_{1}+\mathrm{a}_{2} \mathrm{D}_{2} \mathrm{~m}_{2} \quad$ OR $\quad \mathrm{SN}_{2}=\mathrm{SN}_{1}{ }^{*}+\mathrm{a}_{2} \mathrm{D}_{2} \mathrm{~m}_{2}$
Using the appropriate values for Mr in the Figure, $\mathrm{SN}_{2}=3.8$
CBR of base course material $=100$, From Figure 19.4, $a_{2}=0.14$
Determine appropriate drainage coefficient mi. Since only one set of conditions is given for both the base and subbase layers, the same value will be used for $\mathrm{m}_{2}$ and $\mathrm{m}_{3}$. The time required for water to drain from within pavement=1week, and from Table 19.5, drainage quality is fair. The percentage of time pavement structure will be exposed to moisture levels approaching saturation $=30 \%$, and from Table 19.6, $\mathbf{m}_{2}=\mathbf{m}_{3}=\mathbf{0 . 8 0}$.
$\mathrm{SN}_{2}=\mathrm{a}_{1} \mathrm{D}_{1}+\mathrm{a}_{2} \mathrm{D}_{2} \mathrm{~m}_{2} \Rightarrow 3.8=0.44 \times 6+0.14 \times \mathrm{D}_{2} \times 0.8 \Rightarrow 3.8=2.64+0.112 \mathrm{D}_{2}$
$\mathrm{D}_{2}=10.36$ in $\Rightarrow$ Use 11 in for the thickness of the base course
$\mathrm{SN}_{2}{ }^{*}=\mathrm{a}_{1} \mathrm{D}_{1}+\mathrm{a}_{2} \mathrm{D}_{2} \mathrm{~m}_{2}=0.44 \times 6+0.14 \times 11 \times 0.8=3.872$

## 3. To find $D_{3}$ :

$\mathrm{SN}_{3}=\mathrm{a}_{1} \mathrm{D}_{1}+\mathrm{a}_{2} \mathrm{D}_{2} \mathrm{~m}_{2}+\mathrm{a}_{3} \mathrm{D}_{3} \mathrm{~m}_{3} \quad$ OR $\quad \mathrm{SN}_{3}=\mathrm{SN}_{2} *+\mathrm{a}_{3} \mathrm{D}_{3} \mathrm{~m}_{3}$
Using the appropriate values for Mr in the Figure, $\mathrm{SN}_{3}=4.4$
CBR of subbase course material $=22$, From Figure 19.3, $a_{3}=0.10$
$\mathrm{SN}_{3}=\mathrm{SN}_{2} *+\mathrm{a}_{3} \mathrm{D}_{3} \mathrm{~m}_{3} \Rightarrow 4.4=3.872+0.1 \times \mathrm{D}_{3} \times 0.8$
$\mathrm{D}_{3}=6.6$ in Use 7 in for the thickness of the subbase course
$\mathrm{SN}_{3}{ }^{*}=\mathrm{SN}_{2}{ }^{*}+\mathrm{a}_{3} \mathrm{D}_{3} \mathrm{~m}_{3}=3.872+0.1 \times 7 \times 0.8=4.432$

Table 19.9 AASHTO-Recommended Minimum Thicknesses of Highway Layers

|  | Minimum Thickness (in.) |  |
| :---: | :---: | :---: |
| Traffic, ESALs | Asphalt Concrete | Aggregate Base |
| Less than 50,000 | 1.0 (or surface treatment) | 4 |
| $50,001-150,000$ | 2.0 | 4 |
| $150,001-500,000$ | 2.5 | 4 |
| $500,001-2,000,000$ | 3.0 | 6 |
| $2,000,001-7,000,000$ | 3.5 | 6 |
| Greater than $7,000,000$ | 4.0 | 6 |

The pavement will therefore consist of 6 in asphalt concrete surface, 11 in granular base, and 7 in subbase.

## Lecture 6-15/06/2020

## Asphalt Institute Design Method

The Asphalt Institute's component analysis design approach (termed "effective thickness" by the Asphalt Institute) uses relationships between subgrade strength, pavement structure, and traffic (Asphalt Institute, 1983). The existing structural integrity of the pavement is converted to an equivalent thickness of HMA, which is then compared to that required for a new design. The structural evaluation procedure developed by the Asphalt Institute allows for either determining the required thickness of asphalt concrete overlay or estimating the length of time until an overlay is required. The essential parts of this overlay design procedure will be briefly described:

- Traffic loading (volume) in terms of ESAL.
- Material Properties in terms of Subgrade properties.


## Example:

Subgrade MR $=11,000 \mathrm{psi}$
Traffic $=1.1 \times 10^{6}$ ESAL
Thickness = ?
Answer:
From the figure: Thickness is about 9.5 in .

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Subgrade Resilient Modulus, $M_{\text {r }}$, psi
Mाท
完


:


$$
\begin{aligned}
& \circ \\
& \\
& \\
& \\
& 0
\end{aligned}
$$


dosLIVVW

## California Design Method

Elements to be Defined/Identified for Design

1. Traffic loading (volume) in terms of ESAL.
2. Strength of subgrade.
3. Strength of construction materials.

## 1. Traffic loading:

$$
T_{I}=9.0 \times\left(\frac{E S A L}{10^{6}}\right)^{0.119}
$$

$T_{I}=$ Traffic Index.

## 2. Strength of subgrade:

In terms of R value of subgrade.

## 3. Strength of construction materials

$$
G E=0.975 \times T_{I}(100-R)
$$

$G E=$ Gravel Equivalent Thickness (mm)
$R=$ California R -value of the material below the layer or layers for which the GE is being calculated

Example: Determine the layers thickness of a flexible pavement with the following data using California Design Method assume a subgrade with a California R-value of 10 , R -value for the subbase AS layer is $50, \mathrm{R}$-value for the base AB layer is 78 . ESAL is $3 \times 10^{6}$

Answer: $T_{I}=10.26=10.5$
$G E($ surface $)=225 \mathrm{~mm}$ thickness of equivalent gravel
From the table: Surface thickness is 132 mm of HMA.
$G E$ (base) $=512 \mathrm{~mm}$ thickness of equivalent gravel
From the table: Base thickness is 315 mm of AB - Aggregate Base.
$G E($ subbase $)=922 \mathrm{~mm}$ thickness of equivalent gravel
From the table: Subbase thickness is 390 mm of AS - Aggregate Subbase.

| Gravel Equivalents (GE) and Thickness of Structural Layers (mm) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Actual Layer Thickness $(\mathrm{mm})^{(5)}$ | $\mathrm{HMA}^{(1),(2)}$ |  |  |  |  |  |  |  |  |  |  | Base and Subbase ${ }^{(3)}$ |  |  |  |  |  |
|  | Traffic Index (TI) |  |  |  |  |  |  |  |  |  |  | TI is not a factor |  |  |  |  |  |
|  | $\begin{gathered} 5.0 \\ \& \\ \text { below } \end{gathered}$ | $\begin{aligned} & 5.5 \\ & 6.0 \end{aligned}$ | $\begin{aligned} & 6.5 \\ & 7.0 \end{aligned}$ | 7.5 8.0 | $\begin{aligned} & 8.5 \\ & 9.0 \end{aligned}$ | 9.5 10.0 | $\begin{aligned} & 10.5 \\ & 11.0 \end{aligned}$ | $\begin{aligned} & 11.5 \\ & 12.0 \end{aligned}$ | $\begin{aligned} & 12.5 \\ & 13.0 \end{aligned}$ | $\begin{aligned} & 13.5 \\ & 14.0 \end{aligned}$ | 14.5 15.0 | HMAB LCB | $\begin{gathered} \text { CTPB; } \\ \text { CTB } \\ \text { (Cl. A) } \\ \hline \end{gathered}$ | ATPB | $\begin{gathered} \text { CTB } \\ \text { (Cl. B) } \end{gathered}$ | AB | AS |
|  | $\mathrm{G}_{\mathrm{f}}$ (For HMA thickness equal to or less than 150 mm , Gf decreases with TI$)^{(4)}$ |  |  |  |  |  |  |  |  |  |  | $\mathrm{G}_{\mathrm{f}}$ (constant for any base or subbase material irrespective of TI or thickness) |  |  |  |  |  |
|  | GE for HMA layer (mm) |  |  |  |  |  |  |  |  |  |  | GE for Base or Subbase layer (mm) |  |  |  |  |  |
|  | 2.54 | 2.32 | 2.14 | 2.01 | 1.89 | 1.79 | 1.71 | 1.64 | 1.57 | 1.52 | 1.46 | 1.9 | 1.7 | 1.4 | 1.2 | 1.1 | 1.0 |
|  | GE for HMA layer (mm) |  |  |  |  |  |  |  |  |  |  | GE for Base or Subbase layer (mm) |  |  |  |  |  |
| 45 | 114 | 104 | 96 | 90 | 85 | 81 | 77 | 74 | 71 | 68 | 66 | -- | -- | -- | -- | -- | -- |
| 60 | 152 | 139 | 128 | 121 | 113 | 107 | 103 | 98 | 94 | 91 | 88 | -- | -- | -- | -- | -- | -- |
| 75 | 191 | 174 | 161 | 151 | 142 | 134 | 128 | 123 | 118 | 114 | 110 | -- | -- | 105 | -- | -- | -- |
| 90 | 229 | 209 | 193 | 181 | 170 | 161 | 154 | 148 | 141 | 137 | 131 | -- | -- | 126 | -- | -- | -- |
| 105 | 267 | 244 | 225 | 211 | 198 | 188 | 180 | 172 | 165 | 160 | 153 | 200 | 180 | 147 | 126 | 116 | 105 |
| 120 | 305 | 278 | 257 | 241 | 227 | 215 | 205 | 197 | 188 | 182 | 175 | 228 | 204 | 168 | 144 | 132 | 120 |
| 135 | 343 | 313 | 289 | 271 | 255 | 242 | 231 | 221 | 212 | 205 | 197 | 257 | 230 | 189 | 162 | 149 | 135 |
| 150 | 381 | 348 | 321 | 302 | 284 | 269 | 257 | 246 | 236 | 228 | 219 | 285 | 255 | 210 | 180 | 165 | 150 |
| 165 | 421 | 392 | 362 | 338 | 318 | 301 | 287 | 275 | 264 | 254 | 247 | 314 | 281 | 231 | 198 | 182 | 165 |
| 180 | 473 | 441 | 407 | 380 | 357 | 338 | 322 | 308 | 296 | 285 | 278 | 342 | 306 | 252 | 216 | 198 | 180 |
| 195 | 526 | 490 | 453 | 422 | 397 | 377 | 359 | 343 | 329 | 317 | 309 | 371 | 332 | 273 | 234 | 215 | 195 |
| 210 | -- | 541 | 500 | 466 | 439 | 416 | 396 | 379 | 363 | 350 | 341 | 399 | 357 | -- | 252 | 231 | 210 |
| 225 | -- | 593 | 548 | 511 | 481 | 456 | 434 | 415 | 399 | 384 | 374 | 428 | 383 | -- | 270 | 248 | 225 |
| 240 | -- | 647 | 597 | 557 | 524 | 497 | 473 | 452 | 434 | 418 | 407 | 456 | 408 | -- | 288 | 264 | 240 |
| 255 | -- | -- | 647 | 604 | 568 | 538 | 513 | 491 | 471 | 453 | 442 | 485 | 434 | -- | 306 | 281 | 255 |
| 270 | -- | -- | 698 | 652 | 613 | 581 | 553 | 529 | 508 | 489 | 477 | 513 | 459 | -- | 324 | 297 | 270 |
| 285 | -- | -- |  | 701 | 659 | 625 | 595 | 569 | 546 | 526 | 512 | 542 | 485 | -- | 342 | 314 | 285 |
| 300 | -- | -- | -- | 750 | 706 | 669 | 637 | 609 | 585 | 563 | 548 | 570 | 510 | -- | 360 | 330 | 300 |
| 315 | -- | -- | -- | 801 | 753 | 714 | 680 | 650 | 624 | 601 | 585 | 599 | 536 | -- | 378 | 347 | 315 |
| 330 | -- | -- | -- | -- | 802 | 759 | 723 | 692 | 664 | 639 | 623 | -- | -- | -- | -- | -- | 330 |
| 345 | -- | -- | -- | -- | 851 | 806 | 767 | 734 | 705 | 679 | 661 | -- | -- | -- | -- | -- | 345 |
| 360 | -- | -- | -- | -- | 900 | 853 | 812 | 777 | 746 | 718 | 699 | -- | -- | -- | -- | -- | 360 |
| 375 | -- | -- | -- | -- | -- | 901 | 858 | 820 | 787 | 758 | 738 | -- | -- | -- | -- | -- | 375 |
| 390 | -- | -- | -- | -- | -- | 949 | 904 | 864 | 830 | 799 | 778 | -- | -- | -- | -- | -- | 390 |
| 405 | -- | -- | -- | -- | -- | 998 | 950 | 909 | 873 | 840 | 818 | -- | -- | -- | -- | -- | -- |
| 420 | -- | -- | -- | -- | -- | -- | 997 | 954 | 916 | 882 | 859 | -- | -- | -- | -- | -- | -- |
| 435 | -- | -- | -- | -- | -- | -- | 1045 | 1000 | 960 | 924 | 900 | -- | -- | -- | -- | -- | -- |
| 450 | -- | -- | -- | -- | -- | -- | 1094 | 1046 | 1004 | 967 | 942 | -- | -- | -- | -- | -- | -- |
| 465 | -- | -- | -- | -- | -- | -- | -- | 1093 | 1049 | 1010 | 984 | -- | -- | -- | -- | -- | -- |
| 480 | -- | -- | -- | -- | -- | -- | -- | 1140 | 1094 | 1054 | 1026 | -- | -- | -- | -- | -- | -- |
| 495 | -- | -- | -- | -- | -- | -- | -- | 1188 | 1140 | 1098 | 1069 | -- | -- | -- | -- | -- | -- |
| 510 | -- | -- | -- | -- | -- | -- | -- | -- | 1187 | 1143 | 1113 | -- | -- | -- | -- | -- | -- |
| 525 | -- | -- | -- | -- | -- | -- | -- | -- | 1233 | 1188 | 1156 | -- | -- | -- | -- | -- | -- |
| 540 | -- | -- | -- | -- | -- | -- | -- | -- | 1280 | 1233 | 1201 | -- | -- | -- | -- | -- | -- |
| 555 | -- | -- | -- | -- | -- | -- | -- | -- | -- | 1279 | 1245 | -- | -- | -- | -- | -- | -- |
| 570 | -- | -- | -- | -- | -- | -- | -- | -- | -- | 1325 | 1290 | -- | -- | -- | -- | -- | -- |
| 585 | -- | -- | -- | -- | -- | -- | -- | -- | -- | 1372 | 1336 | -- | -- | -- | -- | -- | -- |
| 600 | -- | -- | -- | -- | -- | -- | -- | -- | -- | -- | 1382 | -- | -- | -- | -- | -- | -- |

## Notes:

(1) Open Graded Friction Course (conventional and rubberized) is a non-structural wearing course and provides no structural value.
(2) Top portion of HMA surface layer (maximum 60 mm ) may be replaced with equivalent RHMA-G thickness. See Topic 631.3 for additional details.
(3) See Table 663.1B for additional information on Gravel Factors $\left(\mathrm{G}_{f}\right)$ and California R -values for base and subbase materials.
(4) These $\mathrm{G}_{\mathrm{f}}$ values are for TIs shown and HMA thickness equal to or less than 150 mm only. For HMA thickness greater than 150 mm , appropriate $\mathrm{G}_{\mathrm{f}}$ should be determined using the equation in Index 633.1(1)(c).
(5) For HMA layer, select TI range, then go down to the appropriate GE and across to the thickness column. For base or subbase layer, select material type, then go down to the appropriate GE and across to the thickness column.
CTB-A - Cement Treated Base Class A
CTB-B - Cement Treated Base Class B
CTP-B - Cement Treated Permeable Base
AB - Aggregate Base
AS - Aggregate Subbase
ATPB - Asphalt Treated Permeable Base
LCB - Lean Concrete Base

## Lecture 7-22/06/2020-

## Rigid Pavement

## Function of Base or Subbase if used:

1) Drainage purpose
2) Reduce the effect of subgrade volume change on concrete layer
3) Prevent pumping of fines through joints \& edges

4) Increase " $K$ " modulus of subgrade reaction

## Rigid Pavement Characteristics:

- Can resist unlimited loading.
- More skid resistance, safe.
- More economical for some projects at certain location.
- Concrete layer is less thickness than other layers.


## Rigid Pavement Types:

## a) Plain concrete pavement:

1. No reinforcement except of using tie bars for longitudinal joints and dowel bars for transverse joints.



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2. Closer spacing between contractions joint as transverse joints, 3-6 m.


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3. Inclined joints may be used (for better load transfer)
4. Very limited use
b) Simply reinforced concrete pavement:


1. Temperature (wire-mesh, B. R. C.) reinforcement between joints to control cracking (close to the upper surface).


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2. Longer slabs
3. Dowel bars across transverse joints


## EFFECT OF DOWEL BARS ON CONCRETE PAVEMENT



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pavement quality concrete (POQ)

3. Tie bars across longitudinal joints to control warping
4. Wider spacing between joints (from $3-6 \mathrm{~m}$ to $7-14 \mathrm{~m}$ )
5. Widely used
c) Continuously reinforced concrete pavement:

(b) Transwerse and konciludinal bars

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1. No joints except some expansion joints \& may be some contraction joints
2. Heavy reinforcement $(\approx>0.6 \%$ of cross section area)
3. High cost
4. Used in very-weak subgrade \& high traffic load

## d) Pre-stressed concrete pavement:



## 1. More expensive

## Rigid Pavements

For all conventional rigid pavement types, a concrete slab is usually poured directly on a subgrade, base, or subbase. The base or subbase could be a bonded or unbonded material that provides adequate support and drainage.

## Materials used in Rigid Pavements

The Portland cement concrete commonly used for rigid pavements consists of Portland cement, coarse aggregate, fine aggregate, and water. Steel reinforcing rods may or may not be used, depending on the type of pavement being constructed.

## Reinforcing Steel

Steel reinforcing used in concrete pavements for

- reduce the amount of cracking that occurs,
- as a load transfer mechanism at joints,
- as a means of tying two slabs together.

Types of steel reinforcement can be classified as follows:

- Steel reinforcement used to control cracking is usually referred to as temperature steel,
- steel rods used as load transfer mechanisms are known as dowel bars,
- and those used to connect two slabs together are known as tie bars.


## A) Temperature Steel

Temperature steel is provided in the form of a bar mat or wire mesh consisting of longitudinal and transverse steel wires welded at regular intervals. The mesh usually is placed about 3 in. below the slab surface. The cross-sectional area of the steel provided per foot width of the slab depends on the size and spacing of the steel wires forming the mesh. The amount of steel required depends on the length of the pavement between expansion joints, the maximum stress desired in the concrete pavement, the thickness of the pavement, and the moduli of elasticity of the concrete and steel. Temperature steel does not prevent cracking of the slab, but it does control the crack widths because the steel acts as a tie holding the edges of the cracks together.

## B) Dowel Bars

Dowel bars are used mainly as load-transfer mechanisms across joints. They provide flexural, shearing, and bearing resistance. The dowel bars must be of a much larger diameter than the wires used in temperature steel. Diameters of 1 to 1.5 in . and lengths of 2 to 3 ft have been
used, with the bars usually spaced at 1 ft centers across the width of the slab. At least one end of the bar should be smooth and lubricated to facilitate free expansion.

## C) Tie Bars

Tie bars are used to tie two sections of the pavement together, and therefore they should be either deformed bars or should contain hooks to facilitate the bonding of the two sections of the concrete pavement with the bar. These bars are usually much smaller in diameter than the dowel bars and are spaced at larger centers. Typical diameter and spacing for these bars are $3 / 4 \mathrm{in}$. and 3 ft , respectively.

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## Type of Joints in Rigid Pavement:

1) Contraction joints: to relieve excessive tensile stress due to drop in temperature. It is a joint that is put in the concrete to control cracking. For example, when they sawcut joints into the concrete pavement, these are control joints. These are necessary, because we know the concrete will crack. We just need to try to control where it cracks. These are called contraction joints, because concrete tends to contract when it is curing.

2) Expansion Joints: provide a clear spacing along the depth to relieve excessive compressive stresses due to rise in temperature. It is used in concrete and steel. An expansion joint allows the concrete or steel to expand or contract with daily temperature variations. If you don't allow this, you may get buckling, or spalling, or total failures.

3) Warping joints: are provided along the longitudinal direction to prevent warping of the concrete slab due to temperature and subgrade moisture variation


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ONE STEP PATENTED JOINT STAKE INTERLOCK! ELIMINATES JOINT FLOATING!

13 ga MRPO
STEE STAKES FOR NEY-IOC JONT SYSTEM. $12^{*}, 15^{*}, 18^{*}, 21^{*}$, or $24^{*}$ LeNGTHS WITH NALL HOLES ON 1* CENTERS,

RADIUS FORMED KEY TO MINIMIZE SHARP ANGLES AND ACHIEVE MAXIMUM LOAD TRANSFER
POOR DESIGNAFEA SUENECT TO SPALLING


4) Construction joints: A construction joint is a type of concrete joint that is used when a new section of concrete is poured adjacent to another concrete section that has already set. The purpose of a construction joint is to allow for some horizontal movement, while being rigid against rotational and vertical movement.


## BRC (British Reinforcement Company) Design:

There are 3 three reasons for using BRC reinforcement in concrete pavements. To prevent cracking under traffic load by providing most of the tensile strength required in the concrete slab. To prevent the cracking that normally occurs when a large slab of concrete cures and shrinks. To minimise the width of any cracks (that form in the concrete, for whatever reason) and to hold the slab together as an entity for as long as possible

$\mathrm{L}=$ Allowable spacing for contraction joint (for longitudinal reinforcement), (ft)
$\mathrm{b}=$ Slab width, (ft)
$\mathrm{C}=$ Coefficient of friction (1-2 use 1.5)
$\gamma=$ Unit wt. of concrete (pcf)
$\mathrm{d}=$ Slab thickness (ft)

Friction resistance $=$ Allowable tensile strength
Friction resistance $=$ Concrete tensile strength + Steel tensile strength
$(\mathrm{L} / 2 * \mathrm{~b} * \mathrm{~d}) * \gamma * \mathrm{C}=\mathrm{b} * \mathrm{~d} * \mathrm{f}_{\mathrm{tc}}+\mathrm{A}_{\mathrm{s}} * \mathrm{f}_{\mathrm{s}}$
For one unit of width use $b=1 \mathrm{ft}$
For safety assume concrete tensile strength $\left(b * d * f_{t c}\right)=0$
$\mathrm{f}_{\mathrm{tc}}=$ Allowable tensile strength of concrete
$\mathrm{f}_{\mathrm{s}}=$ Allowable tensile strength of steel
$\mathrm{A}_{\mathrm{s}}=$ Area of steel $\left(\mathrm{in}^{2} / \mathrm{ft}\right)$ in longitudinal direction
$\mathrm{W}=\mathrm{d} * \gamma\left(\mathrm{Ib} / \mathrm{ft}^{2}\right)$
where: $\mathrm{W}=$ Weight of $1 \mathrm{ft}^{2}$ of slab
$\mathrm{L} / 2 * 1 * \mathrm{~W} * \mathrm{C}=\mathrm{A}_{\mathrm{s}} * \mathrm{f}_{\mathrm{s}}$

$$
\mathrm{As}=\frac{\mathrm{L} * \mathrm{~W} * \mathrm{C}}{2 \mathrm{~F}_{\mathrm{s}}}
$$

To calculate the area of steel in the transverse direction, use $b$ instead of $L$.

(a) Day (slab surface temp > bottom temp)

(b) Night (slab bottom temp > surface temp)

Example: A 2 lane highway rigid pavement is 24 ft wide with a longitudinal warping joint in the centre, transverse construction joints were placed at 50 ft intervals, calculate the amount of longitudinal and transverse reinforcement in the pavement if the slab thickness is 12 in , assume unit weight of concrete $(\gamma)=150 \mathrm{pcf}$, allowable tensile strength of steel $=43000 \mathrm{psi}$.

Lecture 9-06/07/2020

## Rigid Pavement Design

## Portland Cement Association (PCA) Method:

## Design Considerations

The basic factors considered in the PCA design method are:

- Flexural strength of the concrete
- Subgrade and subbase support
- Traffic load

Subgrade and Subbase Support: The modulus of subgrade reaction (k) is used to define the subgrade and subbase support. This can be determined by performing a loading plate test or by correlating with other test results.

Table 20.10 Design $k$ Values for Untreated and Cement-Treated Subbases
(a) Untreated Granular Subbases

| Subgrade $k$ Value (lb/in ${ }^{3}$ ) | Subbase k Value (lb/in ${ }^{3}$ ) |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | 4 in. | 6 in. | 9 in . | 12 in. |
| 50 | 65 | 75 | 85 | 110 |
| 100 | 130 | 140 | 160 | 190 |
| 200 | 220 | 230 | 270 | 320 |
| 300 | 320 | 330 | 370 | 430 |

(b) Cement-Treated Subbases

| Subgrade k Value (lb/in ${ }^{3}$ ) | Subbase $k$ Value (lb/in ${ }^{3}$ ) |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | 4 in. | 6 in. | 9 in. | 12 in. |
| 50 | 170 | 230 | 310 | 390 |
| 100 | 280 | 400 | 520 | 640 |
| 200 | 470 | 640 | 830 | - |

The design also incorporates a load safety factor (LSF) which is used to multiply each axle load. The recommended LSF values are:

- 1.2 for interstate and multilane projects with uninterrupted traffic flow and high truck volumes
- 1.1 for highways and arterials with moderate truck volume
- 1.0 for roads and residential streets with very low truck volume


## Design Procedure

The design procedure consists of two parts: fatigue analysis and erosion analysis. The objective of fatigue analysis is to determine the minimum thickness of the concrete required to control fatigue cracking. This is done by comparing the expected axle repetitions with the allowable repetitions for each axle load and ensuring that the cumulative repetitions are less than those allowable. Allowable axle repetitions depend on the stress ratio factor, which is the ratio of the equivalent stress of the pavement to the modulus of rupture of the concrete. The equivalent stress of the pavement depends on the thickness of the slab and the subbasesubgrade k. The chart in Figure 20.15 can be used to determine the allowable load repetitions based on the stress ratio factor. Tables 20.11 and 20.12 give equivalent stress values for pavements without concrete shoulders and with concrete shoulders, respectively. The objective of the erosion analysis is to determine the minimum thickness of the pavement required to control foundation and shoulder erosion, pumping, and faulting. These pavement distresses are related more closely to deflection, as will be seen later. The erosion criterion is based mainly on the rate of work expended by an axle load in deflecting a slab, as it was determined that a useful correlation existed between pavement performance and the product of the corner deflection and the pressure at the slab-subgrade interface.

The erosion analysis is similar to that of fatigue analysis, except that an erosion factor is used instead of the stress factor. The erosion factor is also dependent on the thickness of the slab and the subgrade-subbase k . Tables 20.13 through 20.16 give erosion factors for different types of pavement construction. Figures 20.16 and 20.17 are charts that can be used to determine the allowable load repetitions based on erosion. The minimum thickness that satisfies both analyses is the design thickness. Design thicknesses for pavements carrying light traffic and pavements with doweled joints carrying medium traffic will usually be based on fatigue analysis, whereas design thicknesses for pavements with undoweled joints carrying medium or heavy traffic and pavements with doweled joints carrying heavy traffic will normally be based on erosion analysis.

(20

0,000


Figure 20.16 Allowable Load Repetitions for Erosion Analysis Based on Erosion Factors
(Without concrete shoulder).


Figure 20.17 Allowable Load Repetitions for Erosion Analysis Based on Erosion Factors (With concrete shoulder).

Table 20.11 Equivalent Stress Values for Single Axles and Tandem Axles (without concrete shoulder)

|  | k of Subgrade-Subbase (lb/in ${ }^{3}$ ) (Single Axle/Tandem Axle) |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Slab <br> Thickness (in.) | 50 | 100 | 150 | 200 | 300 | 500 | 700 |
| 4 | $825 / 679$ | $726 / 585$ | $671 / 542$ | $634 / 516$ | $584 / 486$ | $523 / 457$ | $484 / 443$ |
| 4.5 | $699 / 586$ | $616 / 500$ | $571 / 460$ | $540 / 435$ | $498 / 406$ | $448 / 378$ | $417 / 363$ |
| 5 | $602 / 516$ | $531 / 436$ | $493 / 399$ | $467 / 376$ | $432 / 349$ | $390 / 321$ | $363 / 307$ |
| 5.5 | $526 / 461$ | $464 / 387$ | $431 / 353$ | $409 / 331$ | $379 / 305$ | $343 / 278$ | $320 / 264$ |
| 6 | $465 / 416$ | $411 / 348$ | $382 / 316$ | $362 / 296$ | $336 / 271$ | $304 / 246$ | $285 / 232$ |
| 6.5 | $417 / 380$ | $367 / 317$ | $341 / 286$ | $324 / 267$ | $300 / 244$ | $273 / 220$ | $256 / 207$ |
| 7 | $375 / 349$ | $331 / 290$ | $307 / 262$ | $292 / 244$ | $271 / 222$ | $246 / 199$ | $231 / 186$ |
| 7.5 | $340 / 323$ | $300 / 268$ | $279 / 241$ | $265 / 224$ | $246 / 203$ | $224 / 181$ | $210 / 169$ |
| 8 | $311 / 300$ | $274 / 249$ | $255 / 223$ | $242 / 208$ | $225 / 188$ | $205 / 167$ | $192 / 155$ |
| 8.5 | $285 / 281$ | $252 / 232$ | $234 / 208$ | $222 / 193$ | $206 / 174$ | $188 / 154$ | $177 / 143$ |
| 9 | $264 / 264$ | $232 / 218$ | $216 / 195$ | $205 / 181$ | $190 / 163$ | $174 / 144$ | $163 / 133$ |
| 9.5 | $245 / 248$ | $215 / 205$ | $200 / 183$ | $190 / 170$ | $176 / 153$ | $161 / 134$ | $151 / 124$ |
| 10 | $228 / 235$ | $200 / 193$ | $186 / 173$ | $177 / 160$ | $164 / 144$ | $150 / 126$ | $141 / 117$ |
| 10.5 | $213 / 222$ | $187 / 183$ | $174 / 164$ | $165 / 151$ | $153 / 136$ | $140 / 119$ | $132 / 110$ |
| 11 | $200 / 211$ | $175 / 174$ | $163 / 155$ | $154 / 143$ | $144 / 129$ | $131 / 113$ | $123 / 104$ |
| 11.5 | $188 / 201$ | $165 / 165$ | $153 / 148$ | $145 / 136$ | $135 / 122$ | $123 / 107$ | $116 / 98$ |
| 12 | $177 / 192$ | $155 / 158$ | $144 / 141$ | $137 / 130$ | $127 / 116$ | $116 / 102$ | $109 / 93$ |
| 12.5 | $168 / 183$ | $147 / 151$ | $136 / 135$ | $129 / 124$ | $120 / 111$ | $109 / 97$ | $103 / 89$ |
| 13 | $159 / 176$ | $139 / 144$ | $129 / 129$ | $122 / 119$ | $113 / 106$ | $103 / 93$ | $97 / 85$ |
| 13.5 | $152 / 168$ | $132 / 138$ | $122 / 123$ | $116 / 114$ | $107 / 102$ | $98 / 89$ | $92 / 81$ |
| 14 | $144 / 162$ | $125 / 133$ | $116 / 118$ | $110 / 109$ | $102 / 98$ | $93 / 85$ | $88 / 78$ |

Table 20.12 Equivalent Stress Values for Single Axles and Tandem Axles (with concrete shoulder)
$k$ of Subgrade-Subbase (lb/in $\left.{ }^{3}\right)$ (Single Axle/Tandem Axle)

|  | Slab <br> Thickness (in.) |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 50 | 100 | 150 | 200 | 300 | 500 | 700 |
| 4 | $640 / 534$ | $559 / 468$ | $517 / 439$ | $489 / 422$ | $452 / 403$ | $409 / 388$ | $383 / 384$ |
| 4.5 | $547 / 461$ | $479 / 400$ | $444 / 372$ | $421 / 356$ | $390 / 338$ | $355 / 322$ | $333 / 316$ |
| 5 | $475 / 404$ | $417 / 349$ | $387 / 323$ | $367 / 308$ | $341 / 290$ | $311 / 274$ | $294 / 267$ |
| 5.5 | $418 / 360$ | $368 / 309$ | $342 / 285$ | $324 / 271$ | $302 / 254$ | $276 / 238$ | $261 / 231$ |
| 6 | $372 / 325$ | $327 / 277$ | $304 / 255$ | $289 / 241$ | $270 / 225$ | $247 / 210$ | $234 / 203$ |
| 6.5 | $334 / 295$ | $294 / 251$ | $274 / 230$ | $260 / 218$ | $243 / 203$ | $223 / 188$ | $212 / 180$ |
| 7 | $302 / 270$ | $266 / 230$ | $248 / 210$ | $236 / 198$ | $220 / 184$ | $203 / 170$ | $192 / 162$ |
| 7.5 | $275 / 250$ | $243 / 211$ | $226 / 193$ | $215 / 182$ | $201 / 168$ | $185 / 155$ | $176 / 148$ |
| 8 | $252 / 232$ | $222 / 196$ | $207 / 179$ | $197 / 168$ | $185 / 155$ | $170 / 142$ | $162 / 135$ |
| 8.5 | $232 / 216$ | $205 / 182$ | $191 / 166$ | $182 / 156$ | $170 / 144$ | $157 / 131$ | $150 / 125$ |
| 9 | $215 / 202$ | $190 / 171$ | $177 / 155$ | $169 / 146$ | $158 / 134$ | $146 / 122$ | $139 / 116$ |
| 9.5 | $200 / 190$ | $176 / 160$ | $164 / 146$ | $157 / 137$ | $147 / 126$ | $136 / 114$ | $129 / 108$ |
| 10 | $186 / 179$ | $164 / 151$ | $153 / 137$ | $146 / 129$ | $137 / 118$ | $127 / 107$ | $121 / 101$ |
| 10.5 | $174 / 170$ | $154 / 143$ | $144 / 130$ | $137 / 121$ | $128 / 111$ | $119 / 101$ | $113 / 95$ |
| 11 | $164 / 161$ | $144 / 135$ | $135 / 123$ | $129 / 115$ | $120 / 105$ | $112 / 95$ | $106 / 90$ |
| 11.5 | $154 / 153$ | $136 / 128$ | $127 / 117$ | $12 / 109$ | $113 / 100$ | $105 / 90$ | $100 / 85$ |
| 12 | $145 / 146$ | $128 / 122$ | $120 / 111$ | $114 / 104$ | $107 / 95$ | $99 / 86$ | $95 / 81$ |
| 12.5 | $137 / 139$ | $121 / 117$ | $113 / 106$ | $108 / 99$ | $101 / 91$ | $94 / 82$ | $90 / 77$ |
| 13 | $130 / 133$ | $115 / 112$ | $107 / 101$ | $102 / 95$ | $96 / 86$ | $89 / 78$ | $85 / 73$ |
| 13.5 | $124 / 127$ | $109 / 107$ | $102 / 97$ | $97 / 91$ | $91 / 83$ | $85 / 74$ | $81 / 70$ |
| 14 | $118 / 122$ | $104 / 103$ | $97 / 93$ | $93 / 87$ | $87 / 79$ | $81 / 71$ | $77 / 67$ |

Table 20.13 Erosion Factors for Single Axles and Tandem Axles (doweled joints, without concrete shoulder)

| Slab <br> Thickness (in.) | $k$ of Subgrade-Subbase (lb/in$)$ (Single Axle/Tandem Axle) |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 50 | 100 | 200 | 300 | 500 | 700 |
| 4 | $3.74 / 3.83$ | 3.73/3.79 | $3.72 / 3.75$ | $3.71 / 3.73$ | $3.70 / 3.70$ | 3.68/3.67 |
| 4.5 | $3.59 / 3.70$ | $3.57 / 3.65$ | $3.56 / 3.61$ | 3.55/3.58 | 3.54/3.55 | 3.52/3.53 |
| 5 | 3.45/3.58 | 3.43/3.52 | 3.42/3.48 | 3.41/3.45 | 3.40/3.42 | 3.38/3.40 |
| 5.5 | 3.33/3.47 | 3.31/3.41 | 3.29/3.36 | 3.28/3.33 | 3.27/3.30 | $3.26 / 3.28$ |
| 6 | $3.22 / 3.38$ | $3.19 / 3.31$ | 3.18/3.26 | $3.17 / 3.23$ | $3.15 / 3.20$ | 3.14/3.17 |
| 6.5 | $3.11 / 3.29$ | 3.09/3.22 | $3.07 / 3.16$ | 3.06/3.13 | $3.05 / 3.10$ | 3.03/3.07 |
| 7 | 3.02/3.21 | 2.99/3.14 | 2.97/3.08 | 2.96/3.05 | 2.95/3.01 | 2.94/2.98 |
| 7.5 | 2.93/3.14 | 2.91/3.06 | 2.88/3.00 | 2.87/2.97 | 2.86/2.93 | 2.84/2.90 |
| 8 | 2.85/3.07 | 2.82/2.99 | 2.80/2.93 | 2.79/2.89 | 2.77/2.85 | 2.76/2.82 |
| 8.5 | 2.77/3.01 | 2.74/2.93 | 2.72/2.86 | 2.71/2.82 | 2.69/2.78 | 2.68/2.75 |
| 9 | $2.70 / 2.96$ | 2.67/2.87 | 2.65/2.80 | 2.63/2.76 | $2.62 / 2.71$ | 2.61/2.68 |
| 9.5 | 2.63/2.90 | 2.60/2.81 | 2.58/2.74 | 2.56/2.70 | 2.55/2.65 | 2.54/2.62 |
| 10 | 2.56/2.85 | 2.54/2.76 | 2.51/2.68 | $2.50 / 2.64$ | 2.48/2.59 | $2.47 / 2.56$ |
| 10.5 | 2.50/2.81 | 2.47/2.71 | 2.45/2.63 | $2.44 / 2.59$ | 2.42/2.54 | 2.41/2.51 |
| 11 | 2.44/2.76 | 2.42/2.67 | 2.39/2.58 | 2.38/2.54 | 2.36/2.49 | 2.35/2.45 |
| 11.5 | 2.38/2.72 | $2.36 / 2.62$ | $2.33 / 2.54$ | 2.32/2.49 | 2.30/2.44 | $2.29 / 2.40$ |
| 12 | 2.33/2.68 | 2.30/2.58 | 2.28/2.49 | 2.26/2.44 | 2.25/2.39 | 2.23/2.36 |
| 12.5 | 2.28/2.64 | $2.25 / 2.54$ | 2.23/2.45 | 2.21/2.40 | 2.19/2.35 | 2.18/2.31 |
| 13 | 2.23/2.61 | $2.20 / 2.50$ | 2.18/2.41 | 2.16/2.36 | 2.14/2.30 | 2.13/2.27 |
| 13.5 | 2.18/2.57 | 2.15/2.47 | 2.13/2.37 | 2.11/2.32 | 2.09/2.26 | 2.08/2.23 |
| 14 | 2.13/2.54 | 2.11/2.43 | 2.08/2.34 | 2.07/2.29 | 2.05/2.23 | 2.03/2.19 |

Table 20.14 Erosion Factors for Single Axles and Tandem Axles (aggregate interlock joints, without concrete shoulder)

|  | kof Subgrade-Subbase (lb/in ${ }^{3}$ ) (Single Axle/ Tandem Axle) |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Slab <br> Thickness (in.) | 50 | 100 | 200 | 300 | 500 | 700 |
| 4 | $3.94 / 4.03$ | $3.91 / 3.95$ | $3.88 / 3.89$ | $3.86 / 3.86$ | $3.82 / 3.83$ | $3.77 / 3.80$ |
| 4.5 | $3.79 / 3.91$ | $3.76 / 3.82$ | $3.73 / 3.75$ | $3.71 / 3.72$ | $3.68 / 3.68$ | $3.64 / 3.65$ |
| 5 | $3.66 / 3.81$ | $3.63 / 3.72$ | $3.60 / 3.64$ | $3.58 / 3.60$ | $3.55 / 3.55$ | $3.52 / 3.52$ |
| 5.5 | $3.54 / 3.72$ | $3.51 / 3.62$ | $3.48 / 3.53$ | $3.46 / 3.49$ | $3.43 / 3.44$ | $3.41 / 3.40$ |
| 6 | $3.44 / 3.64$ | $3.40 / 3.53$ | $3.37 / 3.44$ | $3.35 / 3.40$ | $3.32 / 3.34$ | $3.30 / 3.30$ |
| 6.5 | $3.34 / 3.56$ | $3.30 / 3.46$ | $3.26 / 3.36$ | $3.25 / 3.31$ | $3.22 / 3.25$ | $3.20 / 3.21$ |
| 7 | $3.26 / 3.49$ | $3.21 / 3.39$ | $3.17 / 3.29$ | $3.15 / 3.24$ | $3.13 / 3.17$ | $3.11 / 3.13$ |
| 7.5 | $3.18 / 3.43$ | $3.13 / 3.32$ | $3.09 / 3.22$ | $3.07 / 3.17$ | $3.04 / 3.10$ | $3.02 / 3.06$ |
| 8 | $3.11 / 3.37$ | $3.05 / 3.26$ | $3.01 / 3.16$ | $2.99 / 3.10$ | $2.96 / 3.03$ | $2.94 / 2.99$ |
| 8.5 | $3.04 / 3.32$ | $2.98 / 3.21$ | $2.93 / 3.10$ | $2.91 / 3.04$ | $2.88 / 2.97$ | $2.87 / 2.93$ |
| 9 | $2.98 / 3.27$ | $2.91 / 3.16$ | $2.86 / 3.05$ | $2.84 / 2.99$ | $2.81 / 2.92$ | $2.79 / 2.87$ |
| 9.5 | $2.92 / 3.22$ | $2.85 / 3.11$ | $2.80 / 3.00$ | $2.77 / 2.94$ | $2.75 / 2.86$ | $2.73 / 2.81$ |
| 10 | $2.86 / 3.18$ | $2.79 / 3.06$ | $2.74 / 2.95$ | $2.71 / 2.89$ | $2.68 / 2.81$ | $2.66 / 2.76$ |
| 10.5 | $2.81 / 3.14$ | $2.74 / 3.02$ | $2.68 / 2.91$ | $2.65 / 2.84$ | $2.62 / 2.76$ | $2.60 / 2.72$ |
| 11 | $2.77 / 3.10$ | $2.69 / 2.98$ | $2.63 / 2.86$ | $2.60 / 2.80$ | $2.57 / 2.72$ | $2.54 / 2.67$ |
| 11.5 | $2.72 / 3.06$ | $2.64 / 2.94$ | $2.58 / 2.82$ | $2.55 / 2.76$ | $2.51 / 2.68$ | $2.49 / 2.63$ |
| 12 | $2.68 / 3.03$ | $2.60 / 2.90$ | $2.53 / 2.78$ | $2.50 / 2.72$ | $2.46 / 2.64$ | $2.44 / 2.59$ |
| 12.5 | $2.64 / 2.99$ | $2.55 / 2.87$ | $2.48 / 2.75$ | $2.45 / 2.68$ | $2.41 / 2.60$ | $2.39 / 2.55$ |
| 13 | $2.60 / 2.96$ | $2.51 / 2.83$ | $2.44 / 2.71$ | $2.40 / 2.65$ | $2.36 / 2.56$ | $2.34 / 2.51$ |
| 13.5 | $2.56 / 2.93$ | $2.47 / 2.80$ | $2.40 / 2.68$ | $2.36 / 2.61$ | $2.32 / 2.53$ | $2.30 / 2.48$ |
| 14 | $2.53 / 2.90$ | $2.44 / 2.77$ | $2.36 / 2.65$ | $2.32 / 2.58$ | $2.28 / 2.50$ | $2.25 / 2.44$ |

## Example Designing a Rigid Pavement Using the PCA Method:

The following project and traffic data are available:
Four-lane interstate highway
Rolling terrain in rural location
Design period $=20 \mathrm{yr}$
Axle loads and expected repetitions are shown in table below
Subbase-subgrade k=130 lb/in ${ }^{3}$
Concrete modulus of rupture $=650 \mathrm{lb} / \mathrm{in}^{2}$
Determine minimum thickness of a pavement with doweled joints and without concrete shoulders.

| Axle load kips | Expected repetitions |
| :--- | :--- |
| Single axles |  |
| 30 | 6310 |
| 28 | 14690 |
| 26 | 30140 |
| 24 | 64410 |
| 22 | 106900 |
| 20 | 235800 |
| 18 | 307200 |
| 16 | 422500 |
| 14 | 586900 |
| 12 | 1837000 |
| Tandem axles |  |
| 52 | 21320 |
| 48 | 42810 |
| 44 | 124900 |
| 40 | 372900 |
| 36 | 885800 |
| 32 | 930700 |
| 28 | 1656000 |
| 24 | 984900 |
| 20 | 1227000 |
| 16 | 1356000 |
|  |  |

## Answer: Step 1. Fatigue Analysis:

1. Select a trial thickness (10 in).
2. Complete columns 1,2 , and 3 as shown ( $1 \& 3$ are given):

LSF $=1.2$ (interstate highway)

| 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} \text { Axle } \\ \text { load } \\ \text { (kips) } \end{gathered}$ | $\begin{aligned} & (1) \times \\ & \text { LSF } \end{aligned}$ | Expected repetitions | Fatigue Analysis |  | Erosion Analysis |  |
|  |  |  | Allowable repetitions | $\begin{gathered} \text { Fatigue \% } \\ {[(3) \div(4)] \times 100} \end{gathered}$ | Allowable repetitions | $\begin{gathered} \text { Damage \% } \\ {[(3) \div(6)] \times 100} \end{gathered}$ |
| Single Axles |  |  |  |  |  |  |
| 30 | 36 | 6310 | 75000 | 8.4 | 2300000 | 0.3 |
| 28 | 33.6 | 14690 | 240000 | 6.1 | 3500000 | 0.4 |
| 26 | 31.2 | 30140 | 900000 | 3.3 | 5600000 | 0.5 |
| 24 | 28.8 | 64410 | 10000000 | 0.6 | 9100000 | 0.7 |
| 22 | 26.4 | 106900 | unlimited | 0 | 19500000 | 0.5 |
| 20 | 24 | 235800 | unlimited | 0 | 43000000 | 0.5 |
| 18 | 21.6 | 307200 | unlimited | 0 | unlimited | 0 |
| 16 | 19.2 | 422500 | unlimited | 0 | unlimited | 0 |
| 14 | 16.8 | 586900 | unlimited | 0 | unlimited | 0 |
| 12 | 14.4 | 1837000 | unlimited | 0 | unlimited | 0 |
| Tandem Axles |  |  |  |  |  |  |
| 52 | 62.4 | 21320 | 6000000 | 0.36 | 1400000 | 1.5 |
| 48 | 57.6 | 42810 | unlimited | 0 | 2000000 | 2.1 |
| 44 | 52.8 | 124900 | unlimited | 0 | 3500000 | 3.6 |
| 40 | 48 | 372900 | unlimited | 0 | 7000000 | 5.3 |
| 36 | 43.2 | 885800 | unlimited | 0 | 15000000 | 5.9 |
| 32 | 38.4 | 930700 | unlimited | 0 | 40000000 | 2.3 |
| 28 | 33.6 | 1656000 | unlimited | 0 | unlimited | 0 |
| 24 | 28.8 | 984900 | unlimited | 0 | unlimited | 0 |
| 20 | 24 | 1227000 | unlimited | 0 | unlimited | 0 |
| 16 | 19.2 | 1356000 | unlimited | 0 | unlimited | 0 |
| Total |  |  |  | 18.76 |  | 23.6 |

3. Complete column (4): Determine the equivalent stresses for single axle and tandem axle.

Table 20.11 is used in this case since there is no concrete shoulder. Interpolating for $\mathrm{k}=$ 130

## For single axles and 10 in. thick slab:

Equivalent stress $=200-\frac{200-186}{50} \times 30=191.6 \mathrm{Ib} / \mathrm{in}^{2}$ (Interpolation)

## For tandem axles and 10 in. thick slab:

Equivalent stress $=193-\frac{193-173}{50} \times 30=181 \mathrm{Ib} / \mathrm{in}^{2}$ (Interpolation)
4. Determine the stress ratio, which is the equivalent stress divided by the modulus of rupture:

For single axles: Stress ratio $=\frac{\text { equivalent stress }}{\text { modulus of rupture }}=\frac{191.6}{650}=0.295$
For tandem axles: Stress ratio $=\frac{\text { equivalent stress }}{\text { modulus of rupture }}=\frac{181}{650}=0.278$
5. Using Figure 20.15, determine the allowable load repetitions for each axle load based on fatigue analysis.
6. Determine the fatigue percentage for each axle load, which is an indication of the resistance consumed by the expected number of axle load repetitions:

$$
\text { Fatigue percentage }=\frac{\text { Column (3) }}{\text { Column (4) }} \times 100
$$

7. Determine total fatigue resistance consumed by summing up column 5 (single and tandem axles) which is $18.76 \%$. If this total does not exceed $100 \%$, the assumed thickness is adequate for fatigue resistance for the design period.

## Step 2. Erosion Analysis:

1. Determine the erosion factor for the single and tandem axle loads using Table 20.13.

For single axles: Erosion factor $=2.54-\frac{2.54-2.51}{100} \times 30=2.531$
For tandem axles: Erosion factor $=2.76-\frac{2.76-2.68}{100} \times 30=2.736$
2. Determine the allowable axle repetitions for each axle load based on erosion analysis using either Figure 20.16 or Figure 20.17. In this problem, Figure 20.16 will be used as the pavement has no concrete shoulder. Enter these values under column 6.
3. Determine erosion damage percentage for each axle load; that is, divide column 3 by column 6. Enter these values in column 7.
4. Determine the total erosion damage by summing column 7 (single and tandem axles).

In this problem, total damage is $19.08 \%$.
The results indicate that 10 in . is adequate for both fatigue and erosion analysis. Since the total fatigue and erosion damages for each analysis are much lower than $100 \%$. In order to achieve the most economic section for the design period, trial runs should be made until the minimum pavement thickness that satisfies both analyses is obtained.

## Now let's try 9.5 in

| 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Axle load (kips) | $\begin{aligned} & (1) \times \\ & \text { LSF } \end{aligned}$ | Expected repetitions | Fatigue Analysis |  | Erosion Analysis |  |
|  |  |  | Allowable repetitions | $\begin{gathered} \text { Fatigue \% } \\ {[(3) \div(4)] \times 100} \end{gathered}$ | Allowable repetitions | $\begin{gathered} \text { Damage \% } \\ {[(3) \div(6)] \times 100} \end{gathered}$ |
| Single Axles |  |  |  |  |  |  |
| 30 | 36 | 6310 | 27000 | 23.3 | 1500000 | 0.4 |
| 28 | 33.6 | 14690 | 77000 | 19.1 | 2200000 | 0.7 |
| 26 | 31.2 | 30140 | 230000 | 13.1 | 3500000 | 0.9 |
| 24 | 28.8 | 64410 | 1200000 | 5.4 | 5900000 | 1.1 |
| 22 | 26.4 | 106900 | Unlimited | 0 | 11000000 | 1.0 |
| 20 | 24 | 235800 | Unlimited | 0 | 23000000 | 1.0 |
| 18 | 21.6 | 307200 | Unlimited | 0 | 64000000 | 0.5 |
| 16 | 19.2 | 422500 | Unlimited | 0 | Unlimited | 0 |
| 14 | 16.8 | 586900 | Unlimited | 0 | Unlimited | 0 |
| 12 | 14.4 | 1837000 | Unlimited | 0 | Unlimited | 0 |
| Tandem Axles |  |  |  |  |  |  |
| 52 | 62.4 | 21320 | 1100000 | 1.9 | 920000 | 2.3 |
| 48 | 57.6 | 42810 | Unlimited | 0 | 1500000 | 2.9 |
| 44 | 52.8 | 124900 | Unlimited | 0 | 2500000 | 5.0 |
| 40 | 48 | 372900 | Unlimited | 0 | 4600000 | 8.1 |
| 36 | 43.2 | 885800 | Unlimited | 0 | 9500000 | 9.3 |
| 32 | 38.4 | 930700 | Unlimited | 0 | 24000000 | 3.9 |
| 28 | 33.6 | 1656000 | Unlimited | 0 | 92000000 | 1.8 |
| 24 | 28.8 | 984900 | Unlimited | 0 | Unlimited | 0 |
| 20 | 24 | 1227000 | Unlimited | 0 | Unlimited | 0 |
| 16 | 19.2 | 1356000 | Unlimited | 0 | Unlimited | 0 |
| Total |  |  |  | 62.8 |  | 38.9 |

The results indicate that 9.5 in . is adequate for both fatigue and erosion analysis and it is more economic than 10 in . Since the total fatigue and erosion damages for each analysis are much lower than $100 \%$. In order to achieve the most economic section for the design period, trial runs should be made until the minimum pavement thickness that satisfies both analyses is obtained.

## Now let's try 9 in

| 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Axle |  |  | Fatigue Analysis |  | Erosion Analysis |  |
| load (kips) | $\begin{aligned} & \text { (1) } \times \\ & \text { LSF } \end{aligned}$ | repetitions | Allowable repetitions | Fatigue \% $[(3) \div(4)] \times 100$ | Allowable repetitions | $\begin{gathered} \text { Damage \% } \\ {[(3) \div(6)] \times 100} \end{gathered}$ |
| Single Axles |  |  |  |  |  |  |
| 30 | 36 | 6310 | 5900 | 106.9 |  |  |
| 28 | 33.6 | 14690 | 21500 |  |  |  |
| 26 | 31.2 | 30140 | 61000 |  |  |  |
| 24 | 28.8 | 64410 | 190000 |  |  |  |
| 22 | 26.4 | 106900 | 900000 |  |  |  |
| 20 | 24 | 235800 | Unlimited |  |  |  |
| 18 | 21.6 | 307200 | Unlimited |  |  |  |
| 16 | 19.2 | 422500 | Unlimited |  |  |  |
| 14 | 16.8 | 586900 | Unlimited |  |  |  |
| 12 | 14.4 | 1837000 | Unlimited |  |  |  |
| Tandem Axles |  |  |  |  |  |  |
| 52 | 62.4 | 21320 | 280000 |  |  |  |
| 48 | 57.6 | 42810 | 1300000 |  |  |  |
| 44 | 52.8 | 124900 | Unlimited |  |  |  |
| 40 | 48 | 372900 | Unlimited |  |  |  |
| 36 | 43.2 | 885800 | Unlimited |  |  |  |
| 32 | 38.4 | 930700 | Unlimited |  |  |  |
| 28 | 33.6 | 1656000 | Unlimited |  |  |  |
| 24 | 28.8 | 984900 | Unlimited |  |  |  |
| 20 | 24 | 1227000 | Unlimited |  |  |  |
| 16 | 19.2 | 1356000 | Unlimited |  |  |  |
| Total |  |  |  |  |  |  |

## Step 1. Fatigue Analysis:

## For single axles and 9 in. thick slab:

$$
\text { Equivalent stress }=232-\frac{232-216}{50} \times 30=222.4 \mathrm{Ib} / \mathrm{in}^{2} \text { (Interpolation) }
$$

For tandem axles and 9 in. thick slab:
Equivalent stress $=218-\frac{218-195}{50} \times 30=204.2 \mathrm{Ib} / \mathrm{in}^{2}$ (Interpolation)
For single axles: Stress ratio $=\frac{\text { equivalent stress }}{\text { modulus of rupture }}=\frac{222.4}{650}=0.342$
For tandem axles: Stress ratio $=\frac{\text { equivalent stress }}{\text { modulus of rupture }}=\frac{204.2}{650}=0.314$

## 9 in is not adequate thickness. Select 9.5 in.

## Lecture 10-13/07/2020

## Thickness Design of Rigid Pavements

## AASHTO Rigid Pavement Design

Design Considerations:
The factors considered in the AASHTO procedure for the design of rigid pavements as presented in the 1993 guide are:

- Pavement performance
- Subgrade strength
- Subbase strength
- Traffic
- Concrete properties
- Drainage
- Reliability


## Joint load transfer coefficient ( $\mathbf{J}$ ):

The load transfer coefficient (J) is a factor used in rigid pavement design to account for the ability of a concrete pavement to distribute (transfer) load across discontinuities, such as longitudinal and transverse joints.

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Table 2.6. Recommended Load Transfer Coefficient for Various Pavement Types and Design Conditions

| Shoulder | Asphalt |  |  | Tied P.C.C. |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Load Transfer <br> Devices | Yes | No | Yes | No |  |
| Pavement Type |  |  |  |  |  |
| 1.Plain jointed and <br> jointed reinforced | 3.2 | $3.8-4.4$ | $2.5-3.1$ | $3.6-4.2$ |  |
| 2. | CRCP | $2.9-3.2$ | N/A | $2.3-2.9$ |  |


| Pavement Type <br> (no tied shoulders) | $\boldsymbol{J}$ |
| :--- | :---: |
| JCP/JRCP <br> w/ load transfer devices | 3.2 |
| JCP/JRCP <br> w/out load transfer devices | $3.8-4.4$ |
| CRCP | 2.9 |

## Drainage coefficient $\mathrm{C}_{\mathrm{d}}$ :

Table 20.9 Recommended Values for Drainage Coefficient, $C_{d}$ for Rigid Pavements

|  | Percent of Time Pavement Structure is Exposed <br> to Moisture Levels Approaching Saturation |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
| Quality of |  |  | $5-25 \%$ | Greater Than |
| Drainage | Less Than $1 \%$ | $1-5 \%$ | $1.15-1.10$ | 1.10 |
| Excellent | $1.2-1.20$ | $1.20-1.15$ | $1.10-1.00$ | 1.00 |
| Good | $1.20-1.15$ | $1.15-1.10$ | $1.00-0.90$ | 0.90 |
| Fair | $1.15-1.10$ | $1.10-1.00$ | $0.90-0.80$ | 0.80 |
| Poor | $1.10-1.00$ | $1.00-0.90$ | $0.80-0.70$ | 0.70 |
| Very poor | $1.00-0.90$ | $0.90-0.80$ |  |  |

## PCC Modulus of Elasticity $E_{c}$

- Measure directly per ASTM C469
- Correlation w/ compressive strength:

$$
E_{c}=57,000\left(f_{c}^{\prime}\right)^{0.5}
$$

$E_{c}=$ elastic modulus (psi)
$f_{c}^{\prime}$ ' $=$ compressive strength (psi) per AASHTO T22, T140, or ASTM C39

## Modulus of Subgrade Reaction (k)

-Required for rigid pavement design.

$$
K=\frac{P}{\Delta}
$$

$\mathrm{K}=$ modulus of subgrade reaction
$\mathrm{P}=$ unit load on the plate (stress) (psi)
$\Delta=$ deflection of the plate (in)


Deformation, in

- For design use stress $P=10 \mathrm{psi}\left(68.95 \mathrm{kN} / \mathrm{m}^{2}\right)$



## Tensile Strength

Tensile strength $\sim 8 \%$ to $15 \%$ of $f^{\prime}{ }_{c}$

- Modulus of Rupture, $\mathrm{f}_{\mathrm{r}}$
- For deflection calculations, use:

$$
f_{\mathrm{A}}=0.7 \sqrt{f^{\prime}{ }_{\mathrm{C}}(M P a)} \quad \text { ACI Eq. 9-10 }
$$

$\mathrm{S}_{\mathrm{c}}$ or $\mathrm{f}_{\mathrm{r}}=$ Modulus of rupture (psi)

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Example: Designing a Rigid Pavement Using the AASHTO Method
Effective modulus of subgrade reaction, $\mathrm{k}=72 \mathrm{lb} / \mathrm{in}^{3}$
Concrete Elastic Modulus $\mathrm{E}_{\mathrm{c}}=5 \times 10^{6} \mathrm{lb} / \mathrm{in}^{2}$
Mean concrete modulus of rupture, $\mathrm{S}_{\mathrm{c}}=650 \mathrm{lb} / \mathrm{in}^{2}$
Load transfer coefficient, $\mathrm{J}=3.2$
Drainage coefficient, $\mathrm{C}_{\mathrm{d}}=1.0$
Design serviceability loss, $\Delta \mathrm{PSI}=4.5-2.5=2.0$
Reliability, $\mathrm{R} \%=95 \%(\mathrm{ZR}=1.645)$
Overall standard deviation, $\mathrm{S}_{\mathrm{o}}=0.29$
Cumulative 18 kip ESAL $=\left(5 * 10^{6}\right)$

