

AL-MUTHANNA UNIVERSITY
COLLEGE OF ENGINEERING
DEPARTMENT OF ARCHITECTURE

Mathematics

Class 1

Syllabus

- Functions; Domain and Range
- Intervals
- Inequalities
- Functions
- Parametric Functions
- Limits and Continuity
- Derivatives
- Application of Derivatives
- Conical Sections.

Functions; Domain and Range

- The temperature at which water boils depends on the elevation above sea level (the boiling point drops as you ascend).
- The area of a circle depends on the radius of the circle.
- The distance an object travels at constant speed along a straight-line path depends on the elapsed time.

In each case, the value of one variable quantity, say y , depends on the value of another variable quantity, which we might call x .

Functions; Domain and Range

We say that “ y is a function of x ” and write this symbolically as

$$y = f(x) \text{ (“}y \text{ equals } f \text{ of } x\text{”).}$$

- f represents the function
- x is the independent variable representing the input value of f
- y is the dependent variable or output value of f at x .

DEFINITION A function f from a set D to a set Y is a rule that assigns a *unique* (single) element $f(x) \in Y$ to each element $x \in D$.

Functions; Domain and Range

- The set D of all possible input values (X) is called the **domain** of the function.
- The **range** may not include every element in the set (Y).
- A value of $f(x)$ as x varies throughout D is called the range of the function.
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Functions; Domain and Range

A function f is like a machine that produces an output value $f(x)$ in its range whenever we feed it an input value x from its domain (Figure 1.1). The function keys on a calculator give an example of a function as a machine.



FIGURE 1.1 A diagram showing a function as a kind of machine.

Functions; Domain and Range

Example :- Let's verify the natural domains and associated ranges of some simple functions. The domains in each case are the values of x for which the formula makes sense.

No	Function	Domain (x)	Range (y)
1	$y = x^2$	$(-\infty, \infty)$	$[0, \infty)$
2	$y = 1/x$	$(-\infty, 0) \cup (0, \infty)$	$(-\infty, 0) \cup (0, \infty)$
3	$y = \sqrt{x}$	$[0, \infty)$	$[0, \infty)$
4	$y = \sqrt{4-x}$	$(-\infty, 4]$	$[0, \infty)$
5	$y = \sqrt{1-x^2}$	$[-1, 1]$	$[0, 1]$

Solution:-

•The formula $y = x^2$ gives a real y -value for any real number x .

The range of $y = x^2$ is $[0, \infty)$ because the square of any real number is nonnegative .

•The formula $y = 1/x$ gives a real y -value for every x except $x = 0$ because if $x = 0$ result will be ∞ . Thus, range of $y = 1/x$, the set of reciprocals of all nonzero real numbers.

Functions; Domain and Range

Solution:-

1. The formula $y = \sqrt{x}$ gives a real y -value only if $x \geq 0$. The range of $y = \sqrt{x}$ is $[0, \infty)$.
2. In $y = \sqrt{4 - x}$, the quantity $4 - x$ cannot be negative. That is, $4 - x \geq 0$, or $x \leq 4$. The formula gives real y -values for all $x \leq 4$. The range of $\sqrt{4 - x}$ is $[0, \infty)$, the set of all nonnegative numbers.
3. The formula $y = \sqrt{1 - x^2}$ gives a real y -value for every x in the closed interval from -1 to 1 . Outside this domain, $1 - x^2$ is negative and its square root is not a real number. The values of $1 - x^2$ vary from 0 to 1 on the given domain, and the square roots of these values do the same. The range of $\sqrt{1 - x^2}$ is $[0, 1]$.
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